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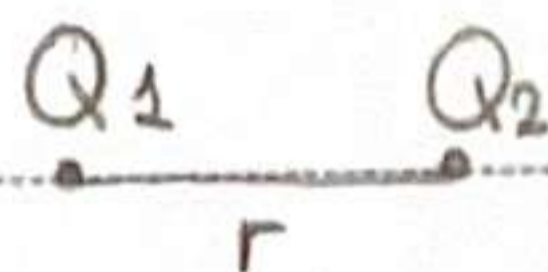
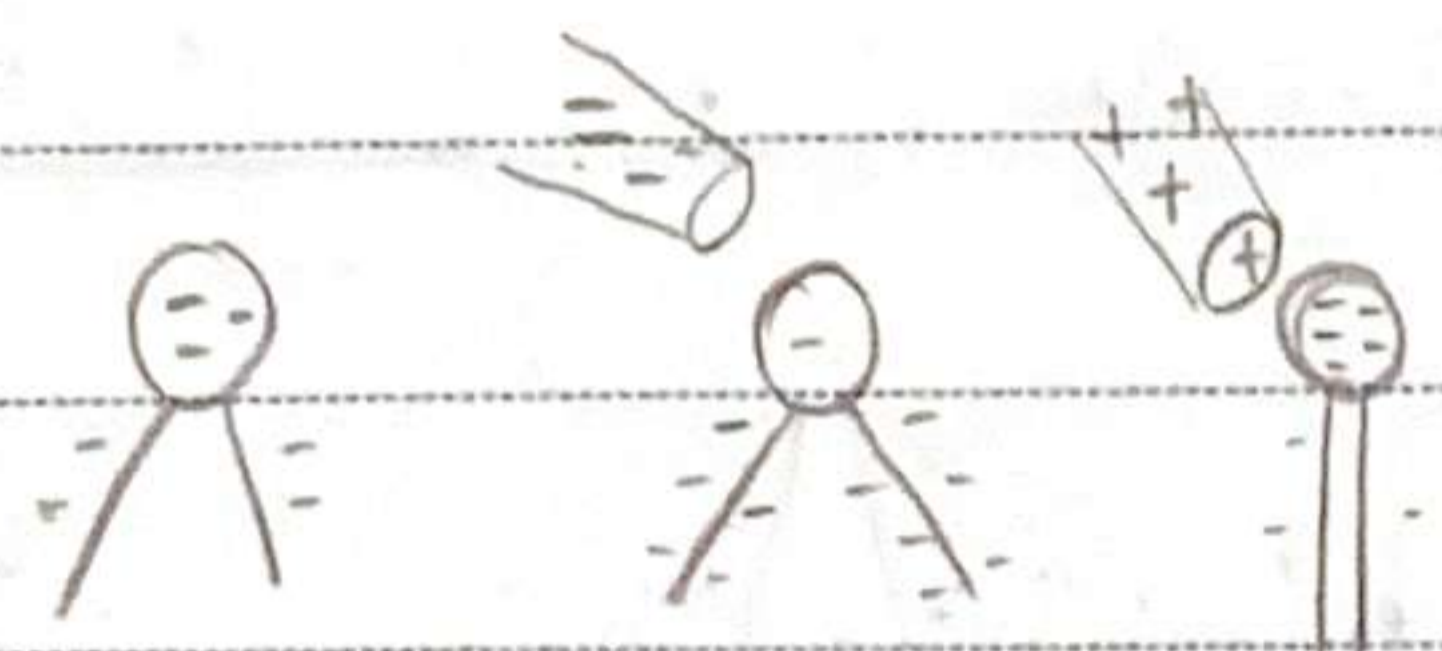
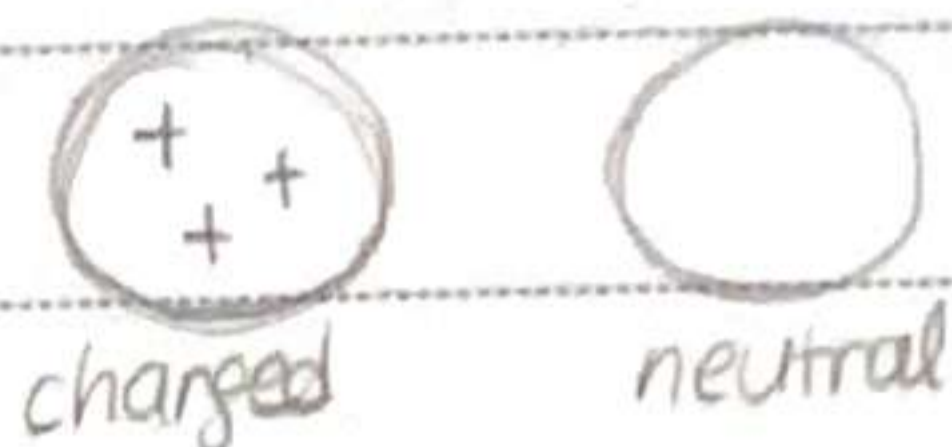
## CHAPTER 21 ELECTRIC CHARGE AND ELECTRIC FIELD

~ electric charge is conserved

conductor : charge flows freely metals

Insulator = almost no charge flows

some materials are semiconductors (silicon and germanium)



$$F = k \cdot \frac{Q_1 \cdot Q_2}{r^2}$$

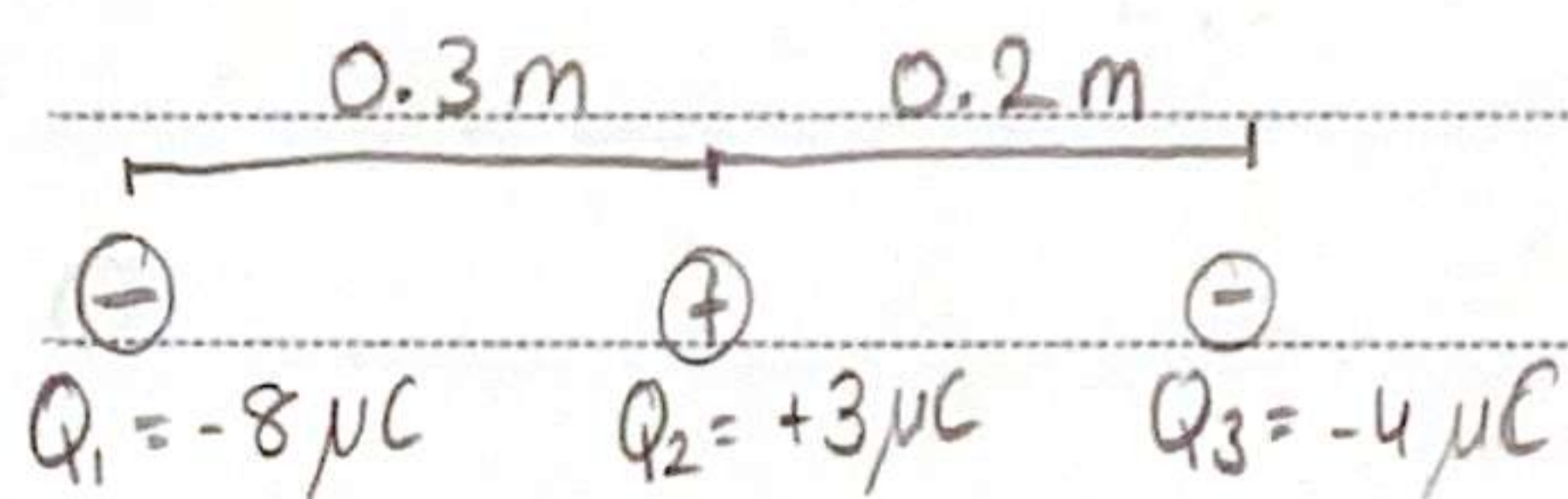
Coulomb's law

**ex 21-1** // Two positive point charges,  $Q_1 = 50 \mu\text{C}$  and  $Q_2 = 1 \mu\text{C}$ , are separated by a distance  $l$ . Which is larger in magnitude, the force that  $Q_1$  exerts on  $Q_2$  or the force that  $Q_2$  exerts on  $Q_1$ ?

$$\text{the force on } Q_1 = F_{12} = k \cdot \frac{Q_1 \cdot Q_2}{l^2} \quad \text{on } Q_2 = F_{21} = k \cdot \frac{Q_1 \cdot Q_2}{l^2}$$

$\approx F_{12} = F_{21}$  } they are same.

**ex 21-2** // Three charged particles are arranged in a line, as shown. Calculate the net electrostatic force on particle 3 due to the other two.



$$F_{31} = k \cdot \frac{Q_1 \cdot Q_3}{r^2} = \frac{(9 \cdot 10^9 \text{ N} \cdot \text{m}^2 / \text{C}^2) (4 \cdot 10^{-6}) (8 \cdot 10^{-6})}{(0.5 \text{ m})^2}$$

$$F_{31} = 1.2 \text{ N} //$$

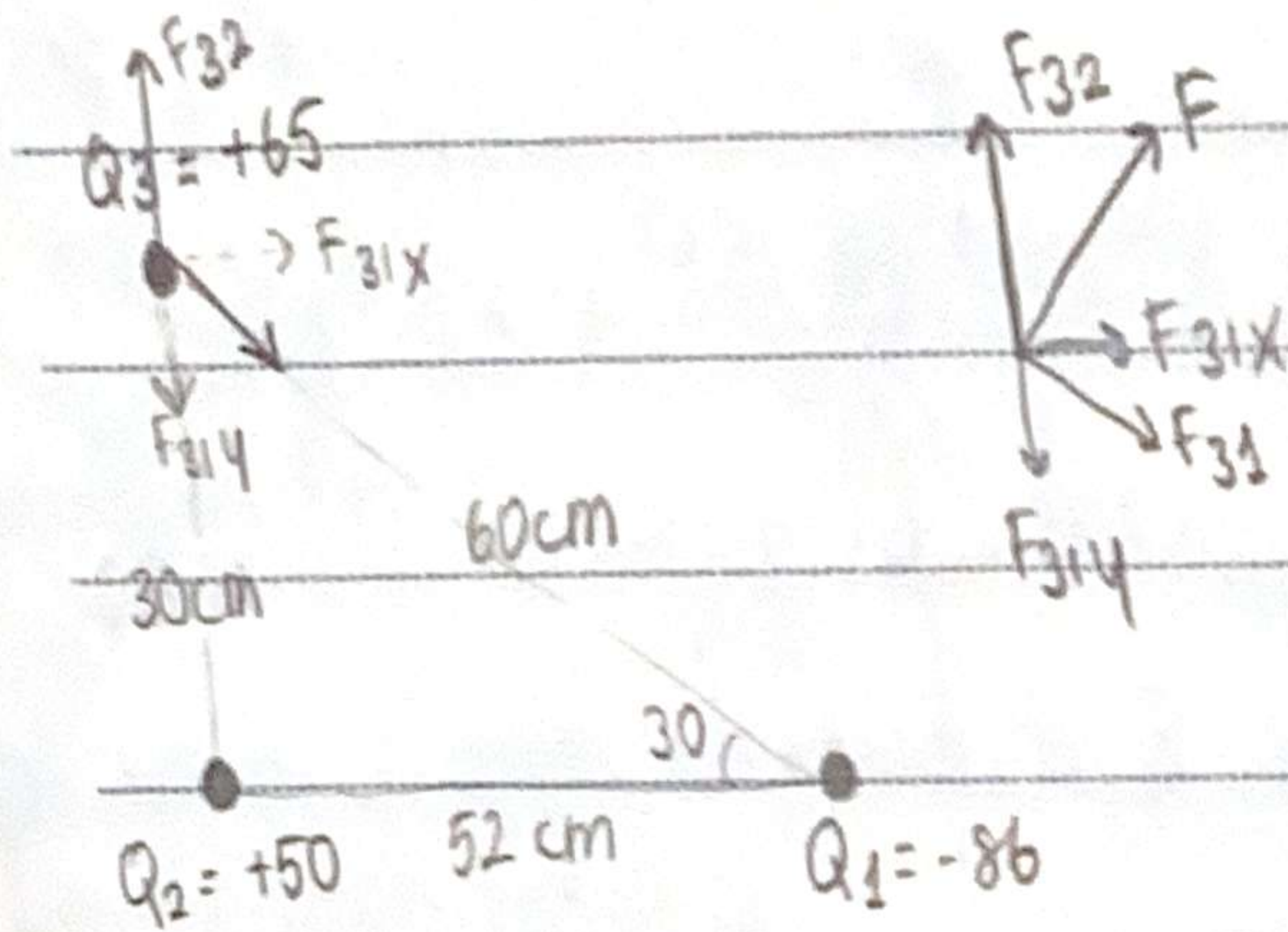
$$F_{32} = k \cdot \frac{Q_3 \cdot Q_2}{r^2} = \frac{(9 \cdot 10^9 \text{ N} \cdot \text{m}^2 / \text{C}^2) (-4 \cdot 10^{-6}) (3 \cdot 10^{-6})}{(0.2)^2} = -2.7 \text{ N} //$$

$$F = (-2.7) + (1.2) = -1.5 \text{ N} //$$

Express

Record :

ex 21-3 // Calculate the net electrostatic force on charge  $Q_3$  shown in the figure due to the charges  $Q_1$  and  $Q_2$ .



$$F_{31} = \frac{k \cdot Q_1 \cdot Q_3}{r^2} = \frac{(9 \cdot 10^9)(6.5 \cdot 10^{-5})(8.6 \cdot 10^{-5})}{(0.6 \text{ m})^2} = 140 \text{ N}$$

$$F_{32} = \frac{k \cdot Q_2 \cdot Q_3}{r^2} = \frac{(9 \cdot 10^9)(6.5 \cdot 10^{-5})(5 \cdot 10^{-5})}{(0.3 \text{ m})^2} = 325 \text{ N}$$

$$F_{31x} = F_{31} \cdot \cos 30 = 121 \text{ N}$$

$$F_{31y} = F_{31} \cdot \sin 30 = 70 \text{ N}$$

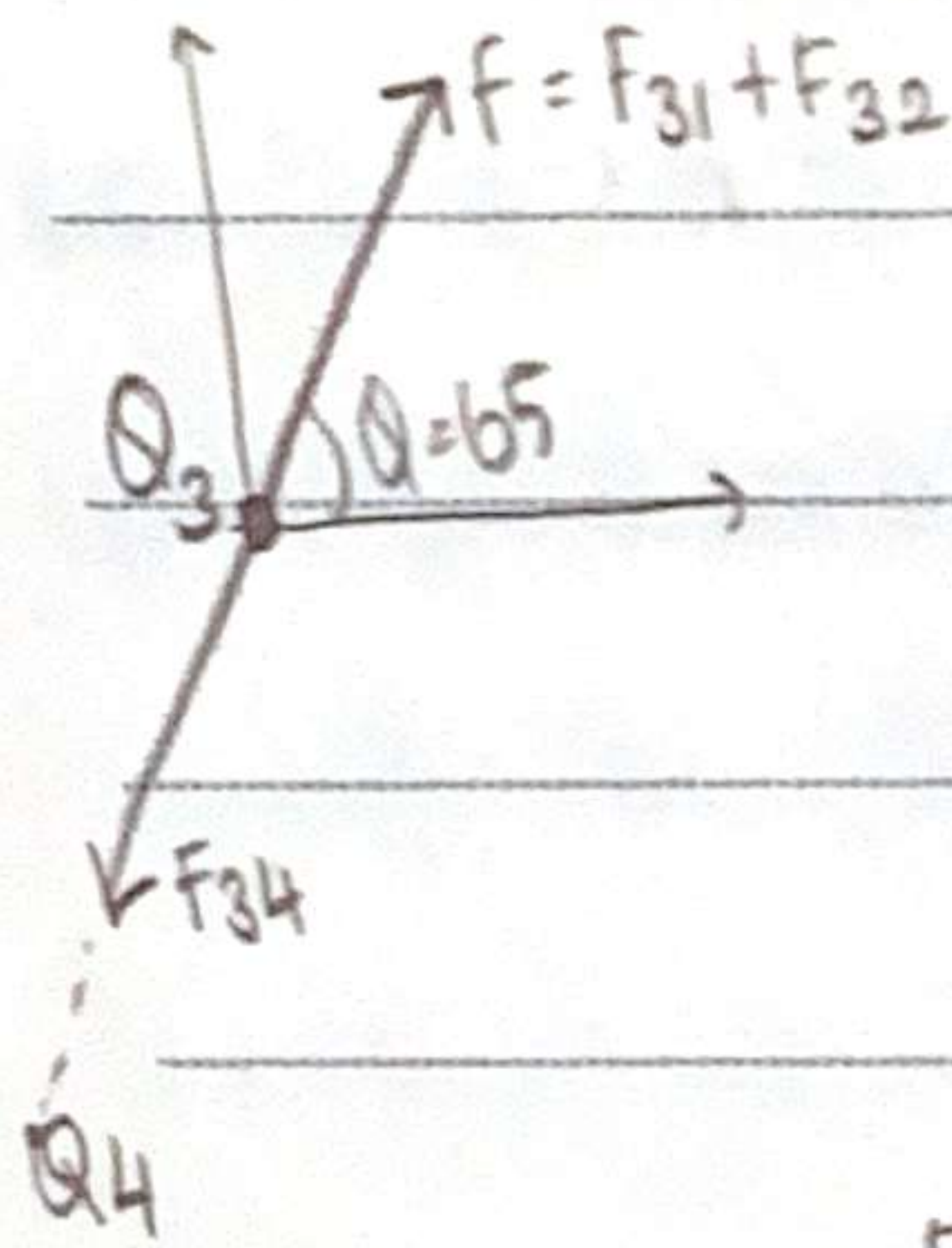
$$F = \sqrt{121^2 + 255^2}$$

$$= 280 \text{ N}$$

ex 21-4 // Where could you place a fourth charge

$Q_4 = -50$ , so that the net force on  $Q_3$  would be zero?

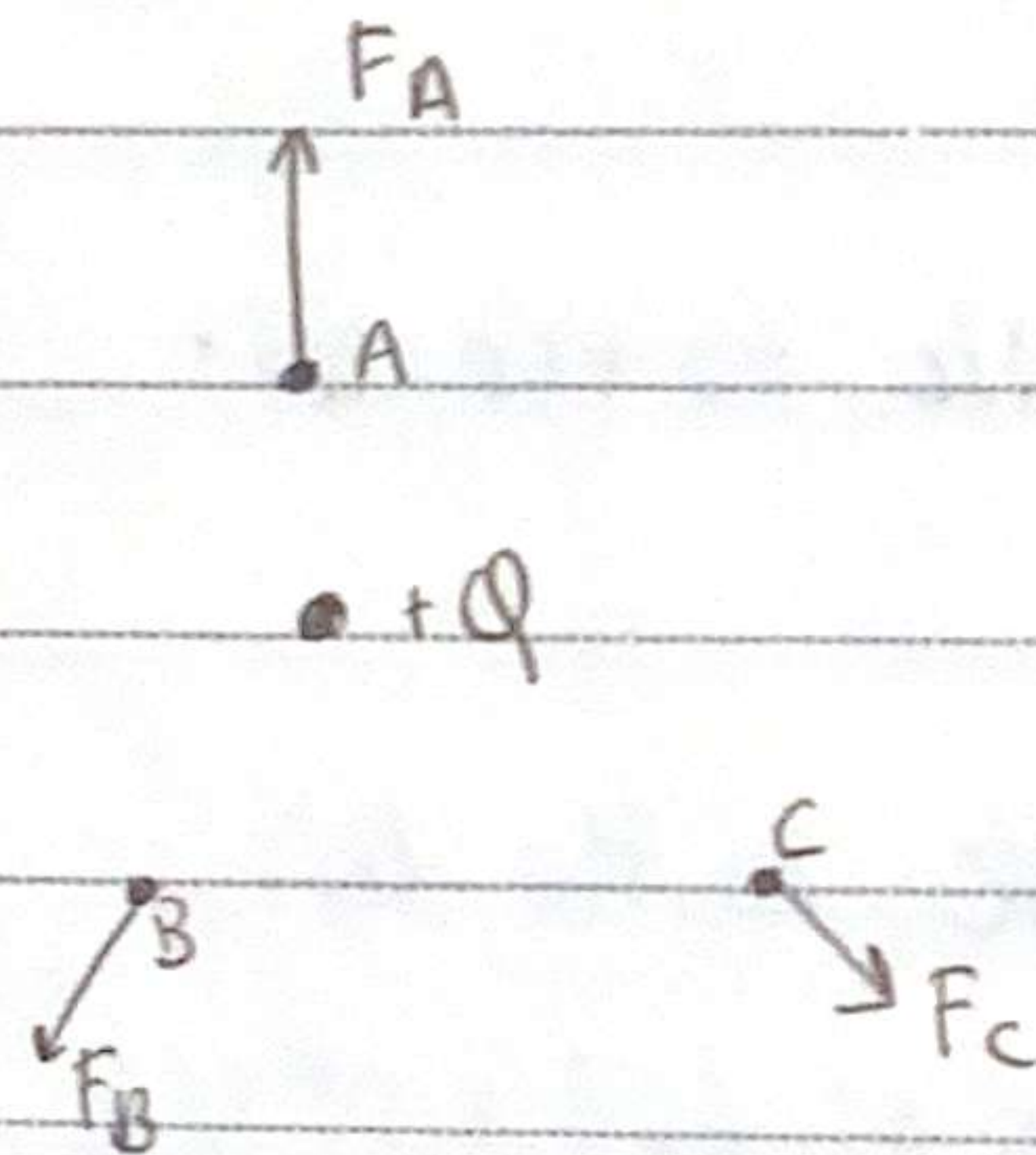
$$\theta = \tan^{-1}\left(\frac{E_y}{E_x}\right) = 65^\circ$$



$$F_{34} = \frac{k \cdot Q_3 \cdot Q_4}{r^2}$$

$$|F_{34}| = |F| \Rightarrow F_{34} = 280 \text{ N} = \frac{(9 \cdot 10^9)(5 \cdot 10^{-5})(6.5 \cdot 10^{-5})}{r^2}$$

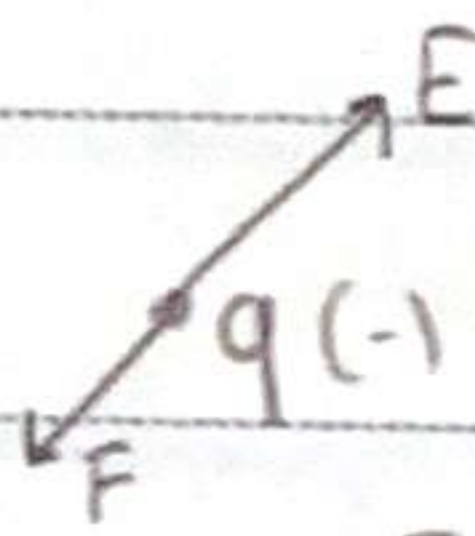
$$r \approx 0.320 \text{ m}$$



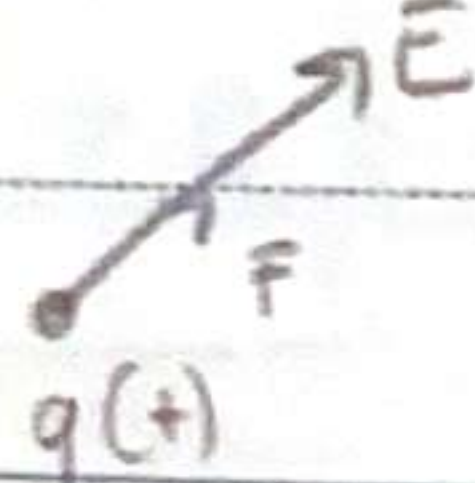
$$E = \frac{F}{q} = \frac{k \cdot q \cdot Q}{r^2 \cdot q} = \frac{k \cdot Q}{r^2}$$

electric field

if  $q$  is negative  $\rightarrow$

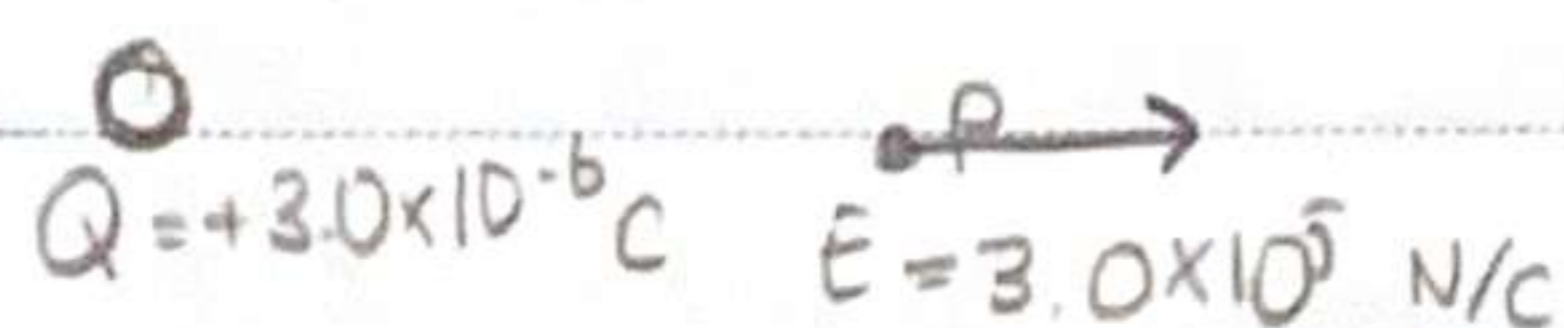
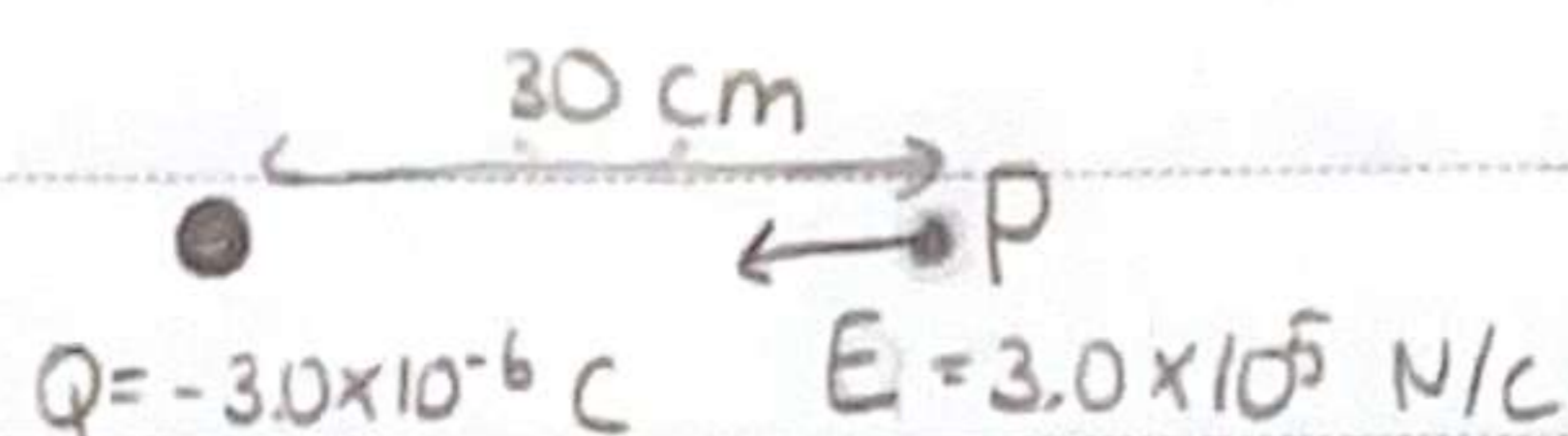


if  $q$  is positive  $\rightarrow$



Record :

**ex 21-6** // calculate the magnitude and direction of the  $E$  field at a point  $P$  which is 30 cm to the right of a point charge  $Q = -3.0 \times 10^{-6} \text{ C}$



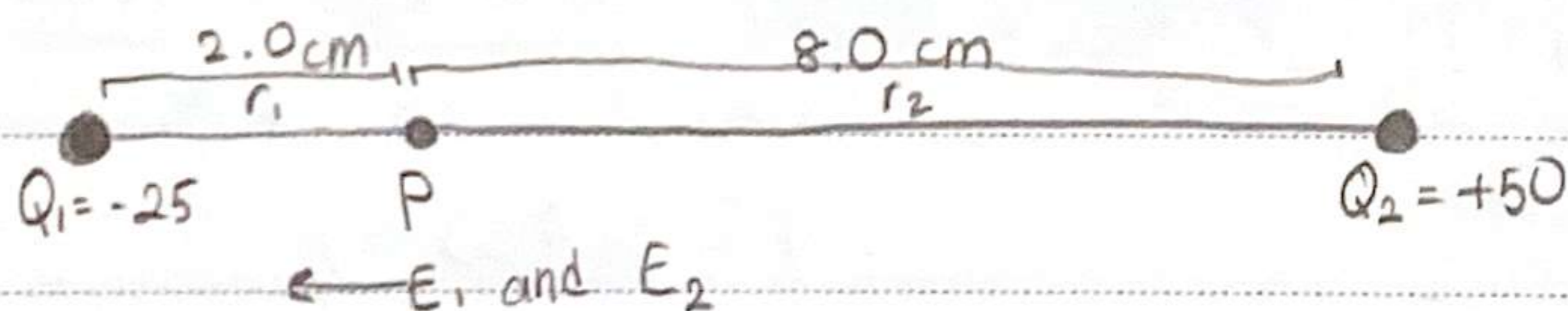
$$E = \frac{k \cdot Q}{r^2} = \frac{(9 \cdot 10^9)(3 \cdot 10^{-6})}{(0.3)^2} = 3 \cdot 10^5 \text{ N/C}$$

magnitude

a) direction of  $E$  is toward the charge  $Q$ , to the left  
b) to the right, outward

**ex 21-7** // two point charges are separated by a distance of 10.0 cm. One has a charge of  $-25 \mu\text{C}$  and the other  $+50 \mu\text{C}$  (a) determine the direction and magnitude of the electric field at a point  $P$  between the two charges that is 2.0 cm from the negative charge

b) if an electron (mass =  $9.11 \times 10^{-31} \text{ kg}$ ) is placed at rest at  $P$  and then released. What will be its initial acceleration? (direction and mag)



a) For  $Q_1$

$$E_1 = k \cdot \frac{Q_1}{r_1^2} = \frac{(9 \cdot 10^9)(25 \times 10^{-6})}{(0.02 \text{ m})^2} = 5.62 \times 10^8 \text{ N/C to the left}$$

For  $Q_2$

$$E_2 = k \cdot \frac{Q_2}{r_2^2} = \frac{(9 \cdot 10^9)(50 \times 10^{-6})}{(0.08)^2} = 7 \times 10^7 \text{ N/C to the left}$$

$$E = E_1 + E_2 = 6.3 \times 10^8 \text{ N/C to the left}$$

b)  $F = m \cdot a$   $E = \frac{F}{q}$   $F = E \cdot q$

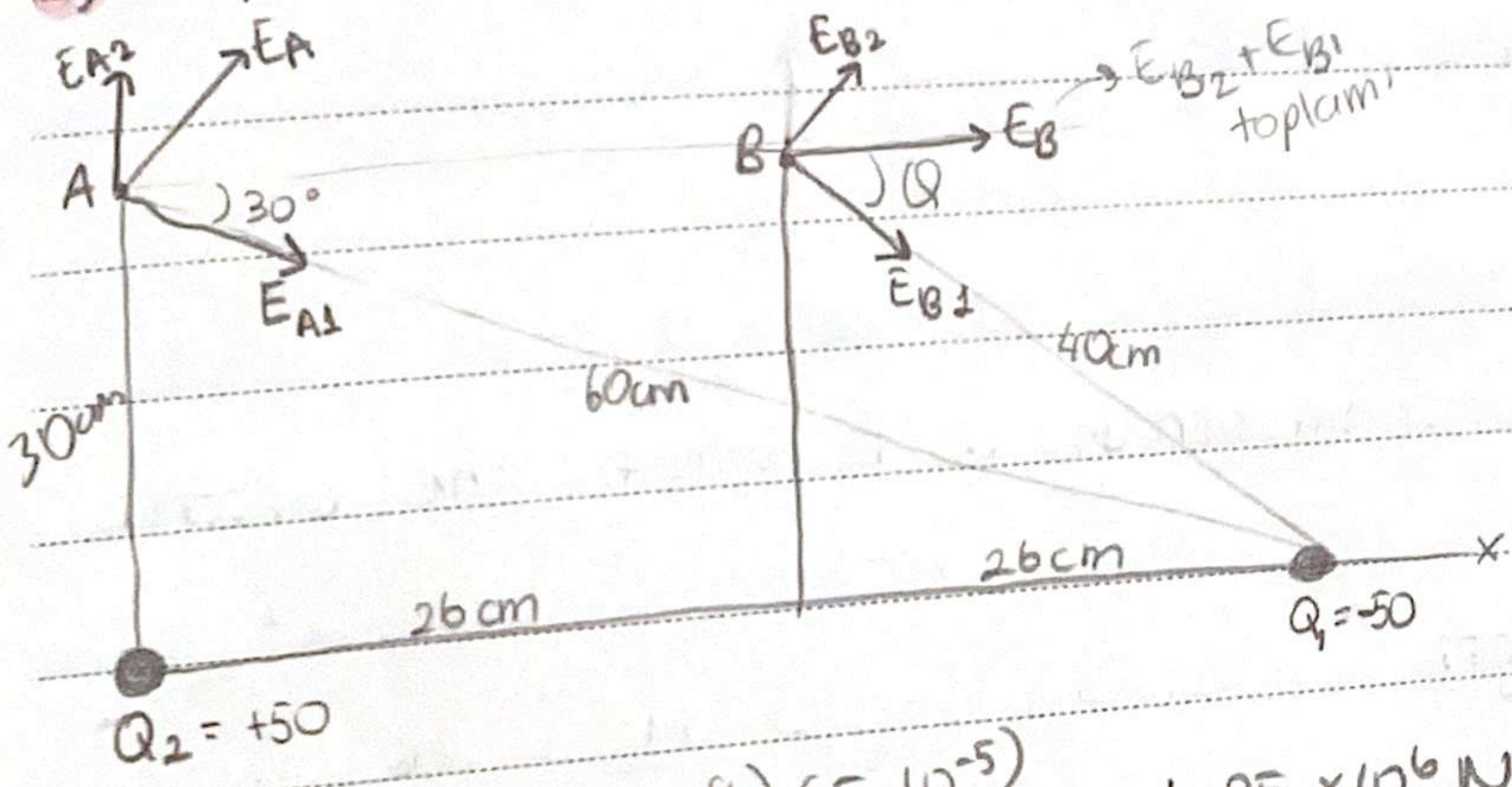
$$a = \frac{F}{m} = \frac{q \cdot E}{m} = \frac{(1.602 \times 10^{-19} \text{ C})(6.3 \times 10^8)}{(9.11 \times 10^{-31})} = 1.1 \times 10^{20} \text{ m/s}^2$$

Express

Record :



ex 21-8 // calculate the total electric field a) at point A  
 b) at point B in the figure due to both charges  $Q_1$  and  $Q_2$ ?



a)  $E_{A1} = \frac{k \cdot Q_1}{r_1^2} = \frac{(9 \cdot 10^9)(5 \cdot 10^{-5})}{(60 \cdot 10^{-2})^2} = 1.25 \times 10^6 \text{ N/C}$   
 $E_{A2} = k \cdot \frac{Q_2}{r_2^2} = \frac{(9 \cdot 10^9)(5 \cdot 10^{-5})}{(0.03)^2} = 5 \times 10^6 \text{ N/C}$

$E_{Ax} = E_{A1} \cdot \cos 30 = 1.08 \times 10^6 \text{ N/C}$   
 $E_{Ay} = E_{A1} \cdot \sin 30 = -6.25 \times 10^5 \text{ N/C}$

$E_{Ax} = 0$   
 $E_{Ay} = 5 \cdot 10^6 \text{ N/C}$   
 $E_{Ax} = E_{Ax} + E_{Ax} = 1.08 \times 10^6$   
 $E_{Ay} = 4.34 \times 10^6$

b)  $|E_{B1}| = |E_{B2}|$  ( $r_1 = r_2$ )  
 $\theta = \tan^{-1}(\frac{30 \text{ cm}}{26 \text{ cm}}) = 49^\circ$

$E_{B1x} = E_{B1} \cdot \cos 49 = 1.8 \times 10^6$   
 $E_{B1} = E_{B2} = k \cdot \frac{Q_2}{r^2} = 2.8 \cdot 10^6$   
 $E_{B1y} = -E_{B1} \cdot \sin 49 = -2.1 \times 10^6$   
 $E_{B2x} = E_{B2} \cdot \cos 49 = 1.8 \times 10^6$   
 $E_{B2y} = E_{B2} \cdot \sin 49 = +2.1 \times 10^6$   
 $E_{B4} = 0$ ,  $E_{Bx} = 3.6 \times 10^6$   
 $E = \sqrt{E_{Bx}^2} = 3.6 \times 10^6$

Record :

The linear charge density  $\lambda = \frac{Q}{l}$

The surface charge density  $\sigma = \frac{Q}{A}$

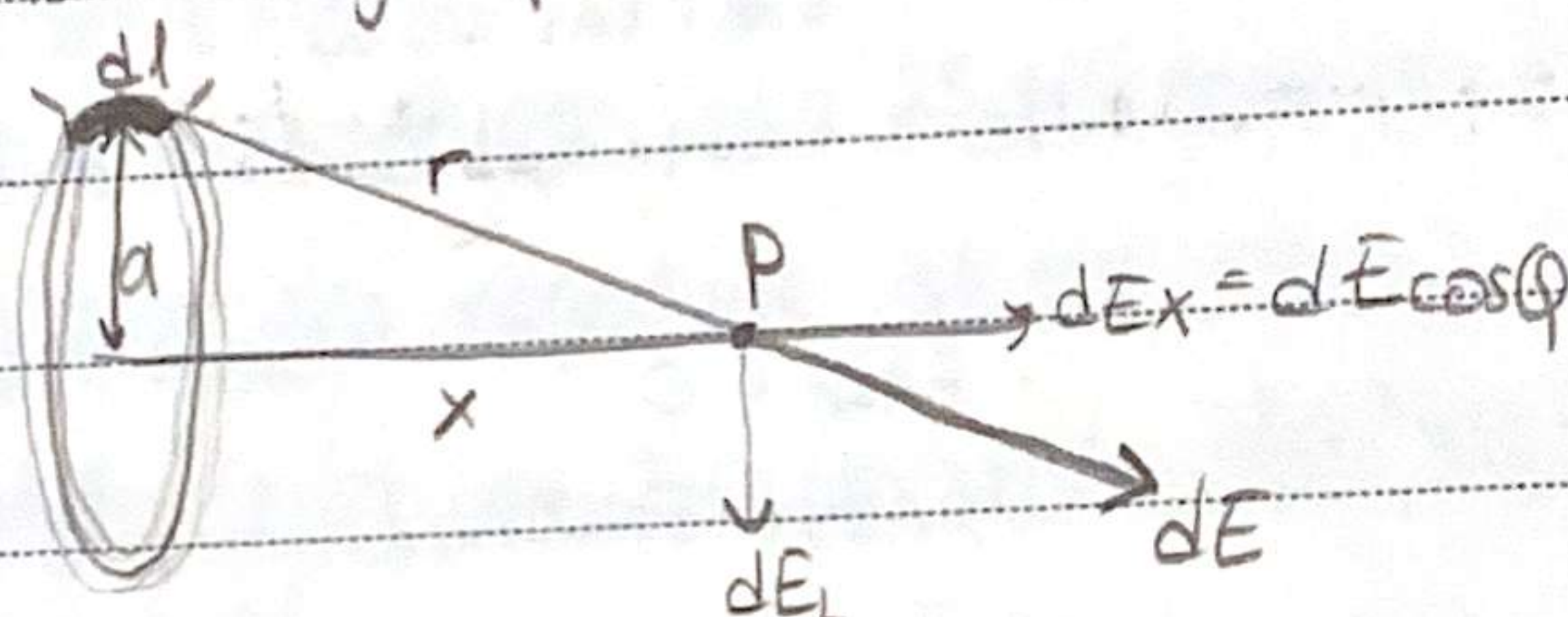
The volume charge density  $\rho = \frac{Q}{V}$

$$dE = \frac{1}{4\pi\epsilon_0} \cdot \frac{dQ}{r^2}$$

ex 21-9 // A thin, ring-shaped object of radius  $a$  holds a total charge  $+Q$  distributed uniformly around it. Determine the electric field at a point  $P$  on its axis a distance  $x$  from the center. Let  $\lambda$  be the charge per unit length

$$dE = \frac{1}{4\pi\epsilon_0} \cdot \frac{dQ}{r^2}$$

$$\lambda = \frac{Q}{2\pi a} = \frac{dQ}{dl} \Rightarrow dQ = \lambda \cdot dl$$



The whole rings length =  $2\pi a$

$$dE = \frac{1}{4\pi\epsilon_0} \cdot \frac{\lambda \cdot dl}{r^2}$$

$$E_x = \int dE_x = \int dE \cos\theta = \frac{1}{4\pi\epsilon_0} \cdot \lambda \int \frac{dl \cos\theta}{r^2}$$

$E_y = 0$  (due to symmetry)

$$E = E_x = \frac{1}{4\pi\epsilon_0} \cdot \lambda \cdot \int \frac{dl \cos\theta}{r^2}$$

$$\cos\theta = \frac{x}{r} = \frac{x}{(x^2+a^2)^{1/2}}$$

$$E = \frac{\lambda}{4\pi\epsilon_0} \cdot \frac{x}{(x^2+a^2)^{3/2}} \int_0^{2\pi a} dl = \frac{1}{4\pi\epsilon_0} \cdot \frac{\lambda \times 2\pi a}{(x^2+a^2)^{3/2}} = \frac{1}{4\pi\epsilon_0} \cdot \frac{Qx}{(x^2+a^2)^{3/2}}$$

For  $x \gg a$

For  $x=0$

$$E = \frac{Q}{4\pi\epsilon_0 x^2}$$

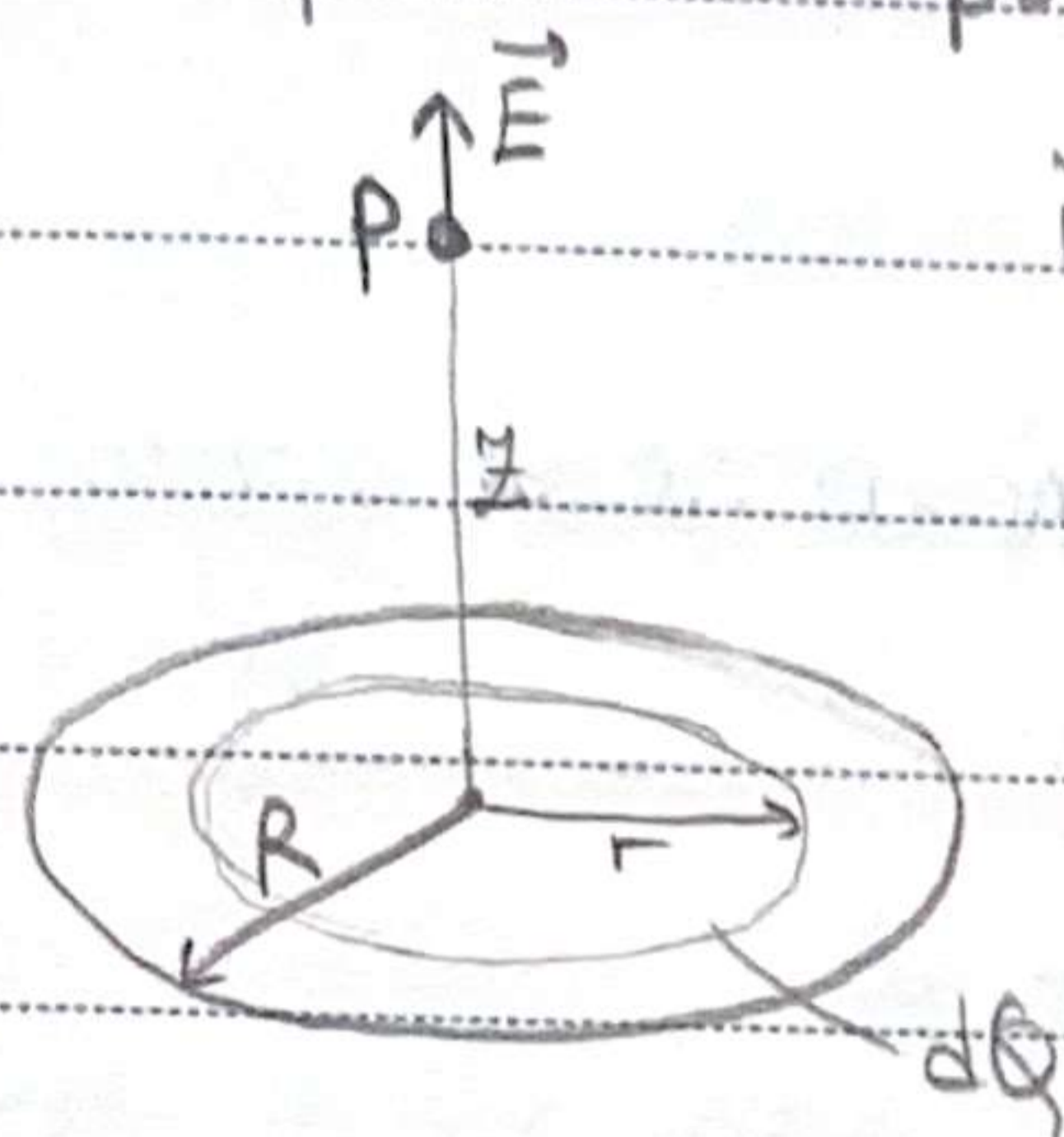
$$E = 0$$

all components will cancel at the center of ring.

Express

Record :

★ **ex 21.12** // Charge is distributed uniformly over a thin circular disk of radius  $R$ . The charge per unit area ( $C/m^2$ ) is  $\sigma$ . Calculate the electric field at a point  $P$  on the axis of the disk, a distance  $z$  above its center.



$$dE = \frac{1}{4\pi\epsilon_0} \cdot \frac{dQz}{(z^2+r^2)^{3/2}} \quad \text{for ex 21.9 //}$$

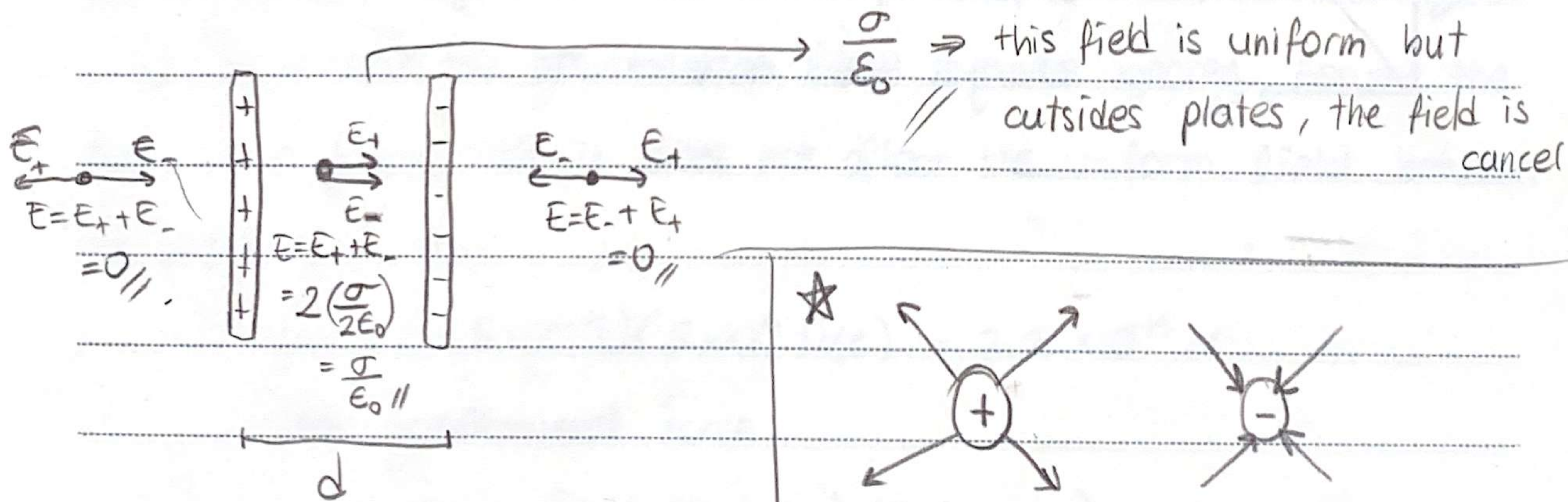
The ring has area  $(dr)(2\pi r)$

$$\sigma = \frac{dQ}{dA} = \frac{dQ}{(dr)(2\pi r)} \quad dE = \frac{1}{4\pi\epsilon_0} \cdot \frac{z\sigma 2\pi r dr}{(z^2+r^2)^{3/2}}$$

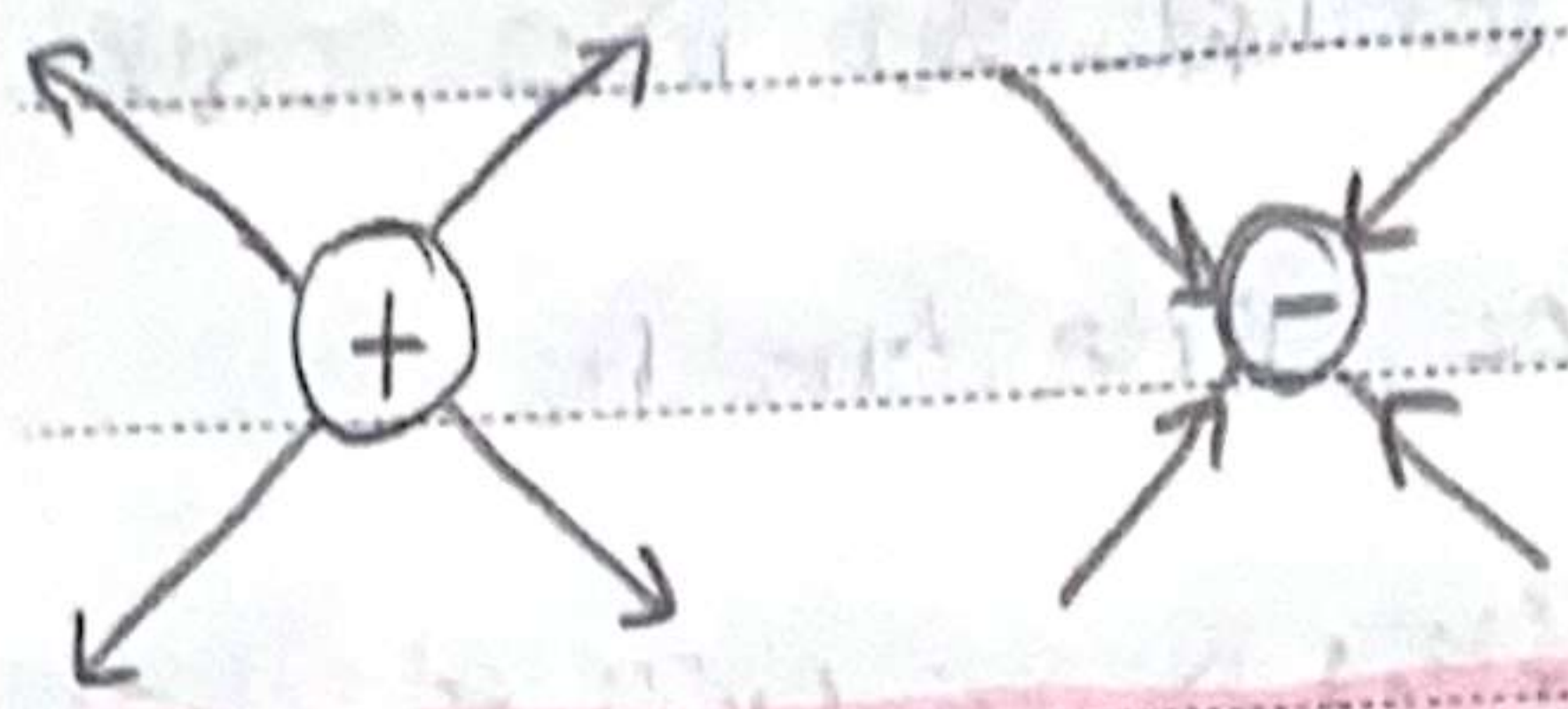
$$E = \frac{z\sigma}{2\epsilon_0} \int_0^R \frac{r dr}{(z^2+r^2)^{3/2}} = \frac{z\sigma}{2\epsilon_0} \left[ -\frac{1}{(z^2+r^2)^{1/2}} \right]_0^R = \frac{\sigma}{2\epsilon_0} \left[ 1 - \frac{z}{(z^2+R^2)^{1/2}} \right]$$

$E = \frac{\sigma}{2\epsilon_0}$  } This result is valid for any point above on infinite plane at any shapes.

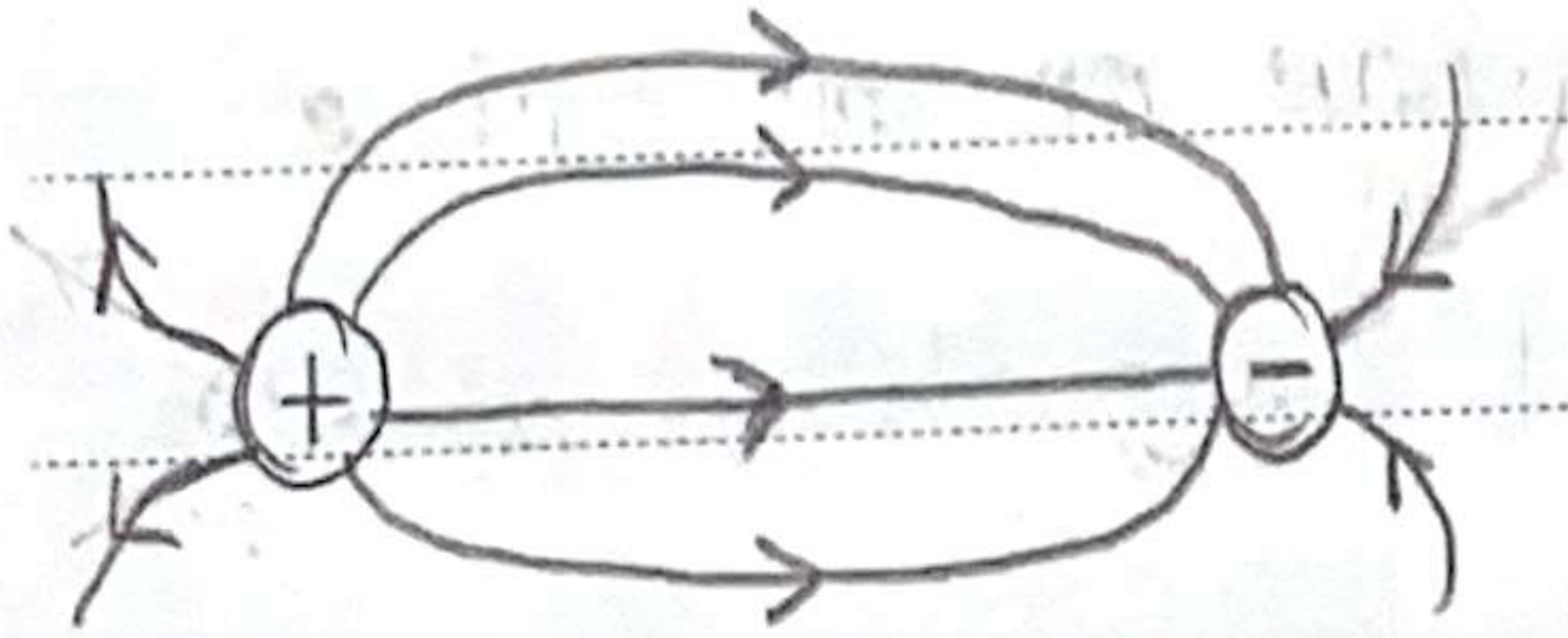
**ex 21.13** // Determine the electric field between two large parallel plates or sheets, which are very thin and are separated by a distance  $d$  which is small compared to their height and width. One plate carries a uniform surface charge density  $\sigma$  and the other carries a uniform surface charge  $-\sigma$  as shown.



Record :

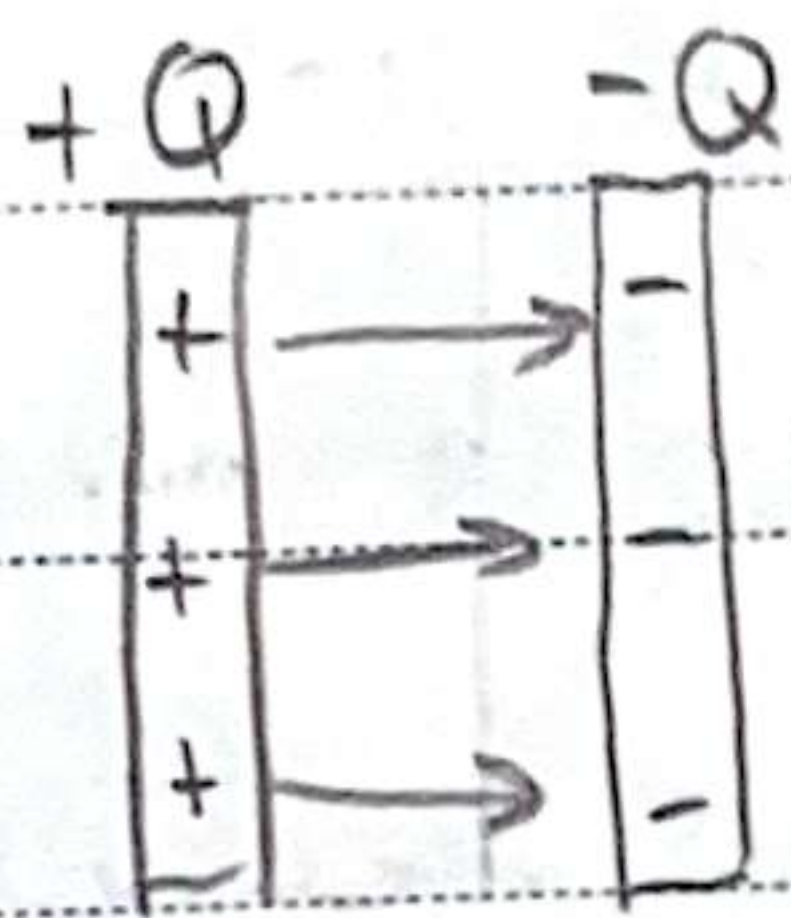


→ these lines start on a positive charge and on a negative charge.



⇒ this combination known as an electric dipole

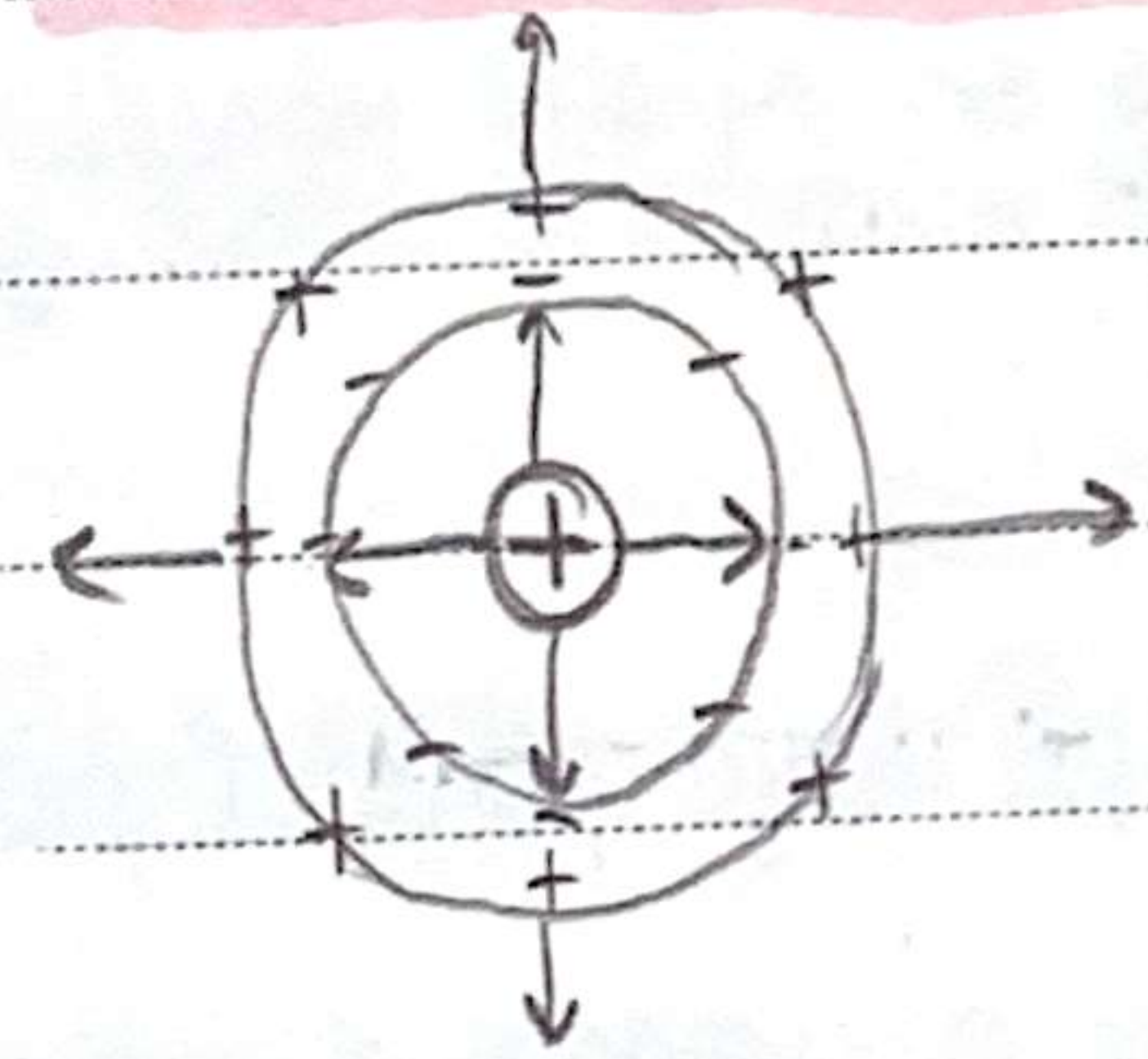
dipol = iki kutuplu sey



⇒ The electric field between two closely spaced, oppositely charged parallel is constant.

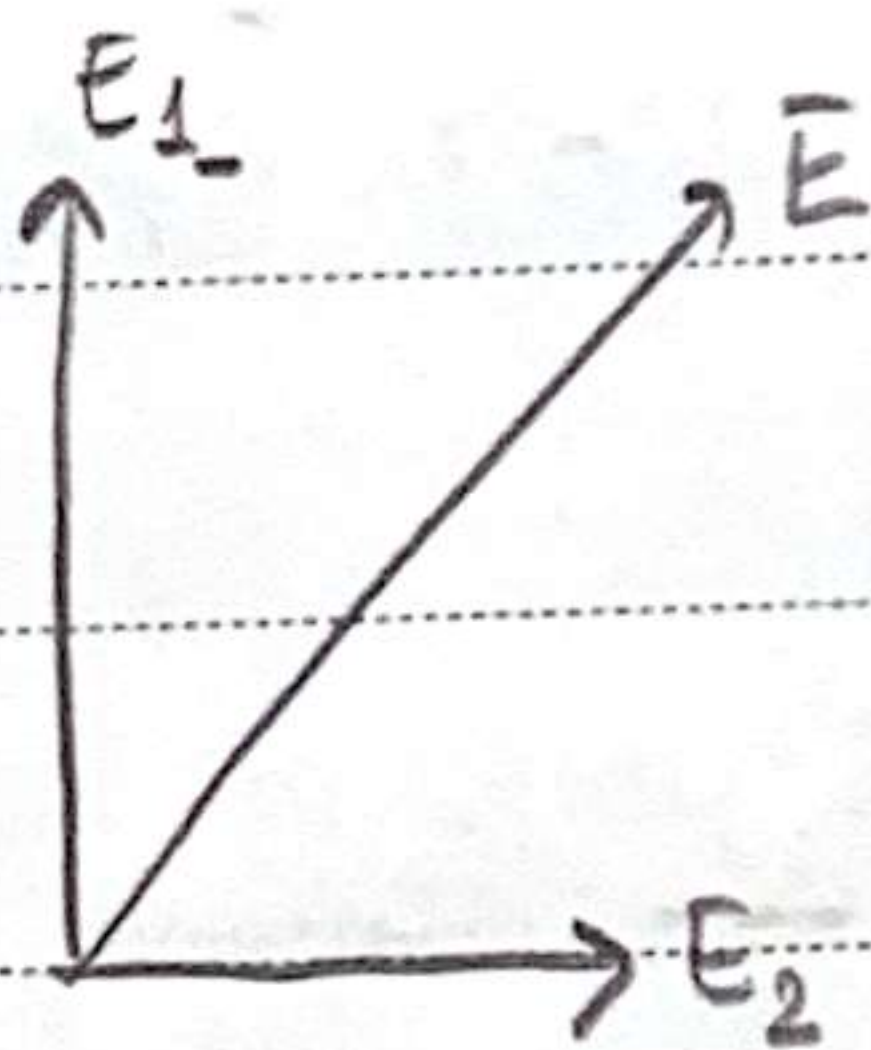
⇒ The electric field has the same magnitude at all points.

$$E = \text{constant} = \frac{\sigma}{\epsilon_0}$$



⇒ the static electric field inside a conductor is zero, if it is not zero, the charges would move.

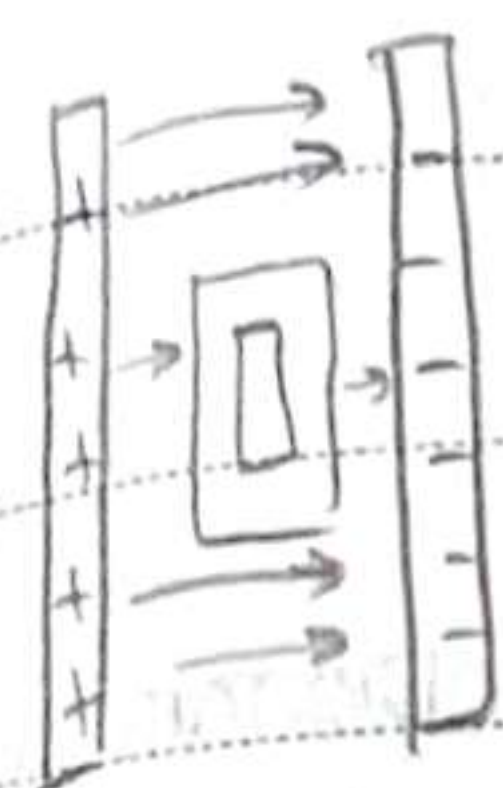
⇒ The net charge on a conductor resides on its outer surface



⇒ The electric field is perpendicular to the surface of a conductor - again, if it were not, charges would move.

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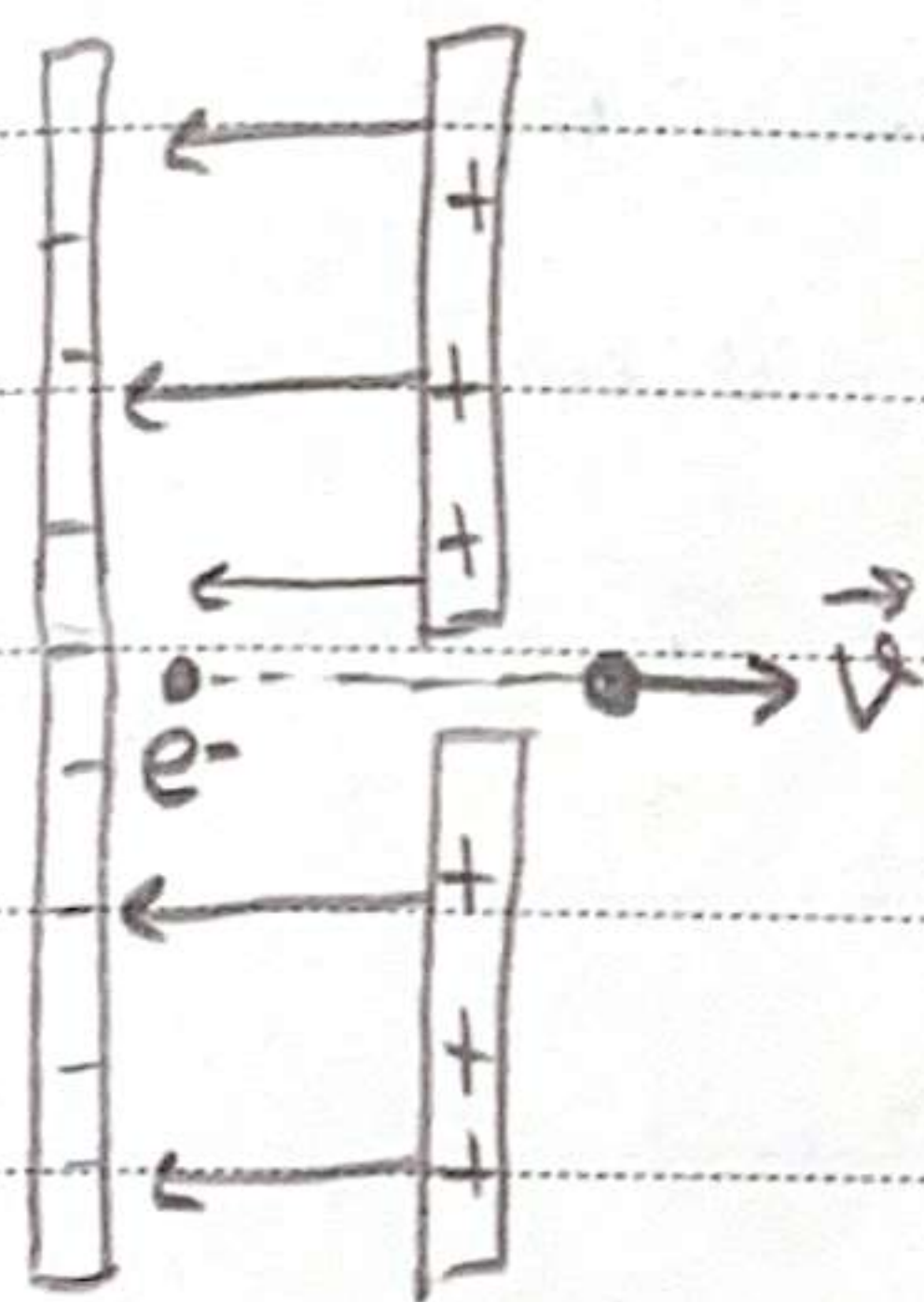
ex 21.14 // A neutral hollow metal box is placed between two parallel charged plates as shown. What is the field like inside the box.



⇒ For hollow box, the external field is not changed because electrons in the metal can only move on the surface

⇒ The person or object inside the cage is not affected

ex 21.15 // An electron (mass  $m = 9.11 \times 10^{-31}$  kg) is accelerated in the uniform field  $E$  ( $E = 2.0 \times 10^4$  N/C) between two parallel charged plates. The separation of the plates is 1.5 cm. The electron is accelerated from rest near the negative plate and passes through a tiny hole in the positive plate. a) With what speed does it leave the hole?



$$F = qE = m \cdot a$$

$$(1.6 \times 10^{-19} \text{ C})(2 \times 10^4 \text{ N/C}) = (9.11 \times 10^{-31} \text{ kg}) \cdot a$$

$$a = 3.5 \times 10^{15} \text{ m/s}^2$$

$$x = 1.5 \times 10^{-2} \text{ m}$$

$$\star v^2 = v_0^2 + 2ax = 2ax \Rightarrow v = \sqrt{2 \cdot (3.5 \times 10^{15}) \cdot (1.5 \times 10^{-2})}$$
$$v = 1.07 \text{ m/s}$$

b) Show that the gravitational force can be ignored. Assume the hole is so small that it does not affect the uniform field between the plates.

$$F = qE = (1.6 \times 10^{-19} \text{ C})(2 \times 10^4 \text{ N/C}) = 3.2 \times 10^{-15} \text{ N}$$

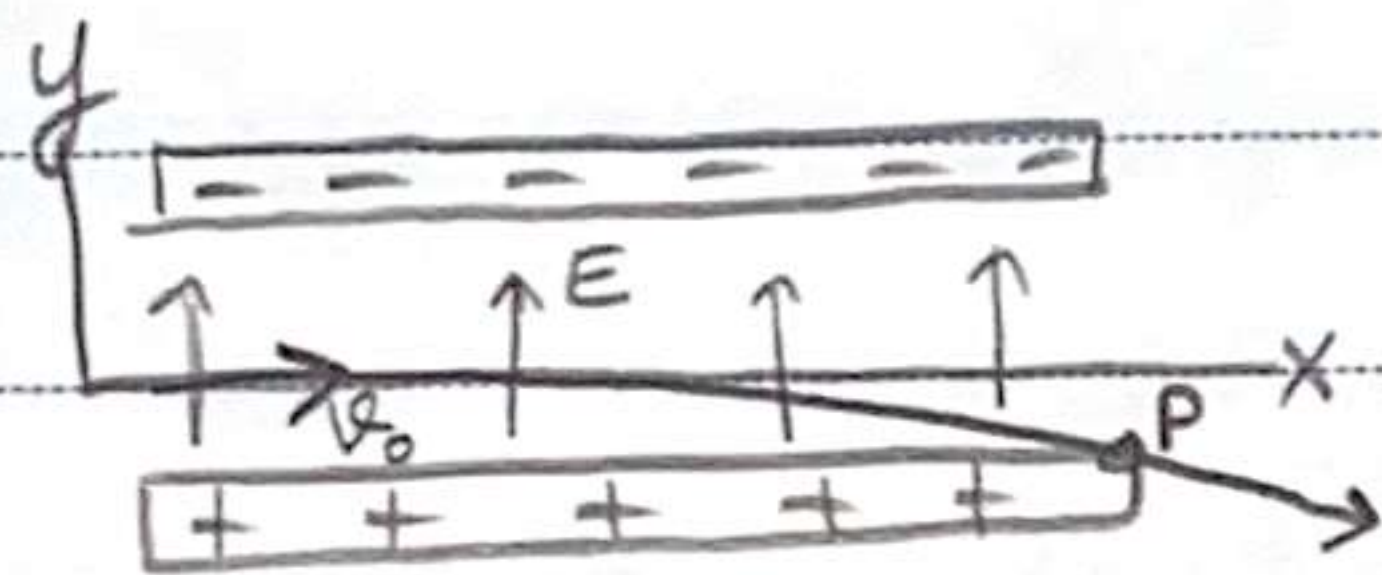
the gravitational force

$$mg = (9.11 \times 10^{-31} \text{ kg})(9.8 \text{ m/s}^2) = 8.9 \times 10^{-30} \text{ N}$$



Record :

**ex 21.16** // Suppose an electron travelling with speed  $v_0 = 1.0 \times 10^7$  m/s enters a uniform electric field  $\vec{E}$ , which is at right angles to  $v_0$  as shown. Describe its motion by giving an equation of its path while in the electric field. Ignore gravity.



x direction = no force  $\rightarrow v_{0x} = \text{constant} = v_0$

y direction =  $F = Eq = m \cdot a_y$

$$q = e = -1.6 \times 10^{-19} \text{ C}$$

$$a_y = \frac{-E \cdot e}{m}$$

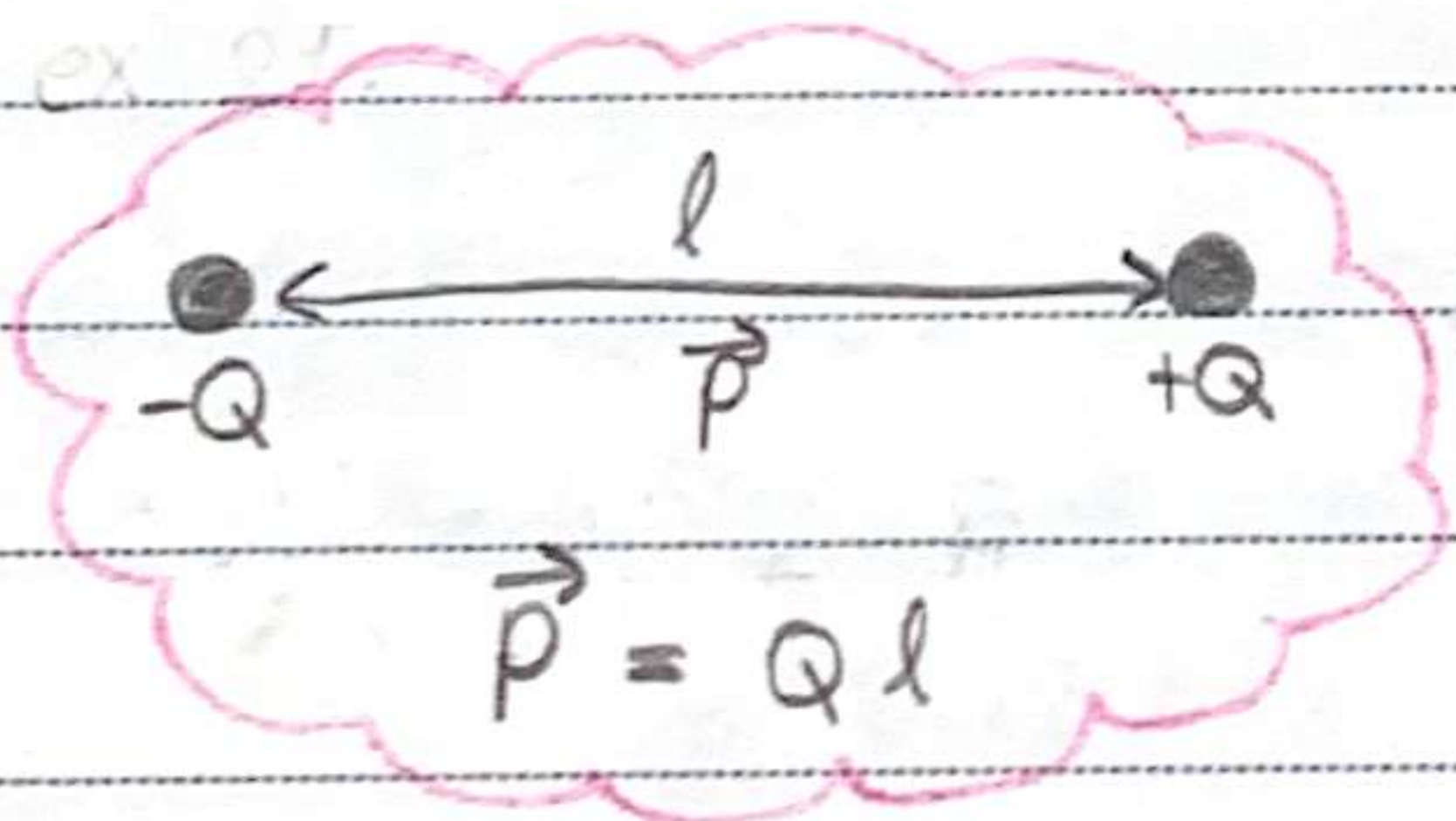
$$y = \frac{at^2}{2} = -\frac{Ee}{2m} \cdot \frac{x^2}{v_0^2}$$

$$x = v_{0x} \cdot t \Rightarrow t = \frac{x}{v_0}$$

$$y = -\frac{Eex^2}{2mv_0^2} \Rightarrow \text{projectile motion}$$

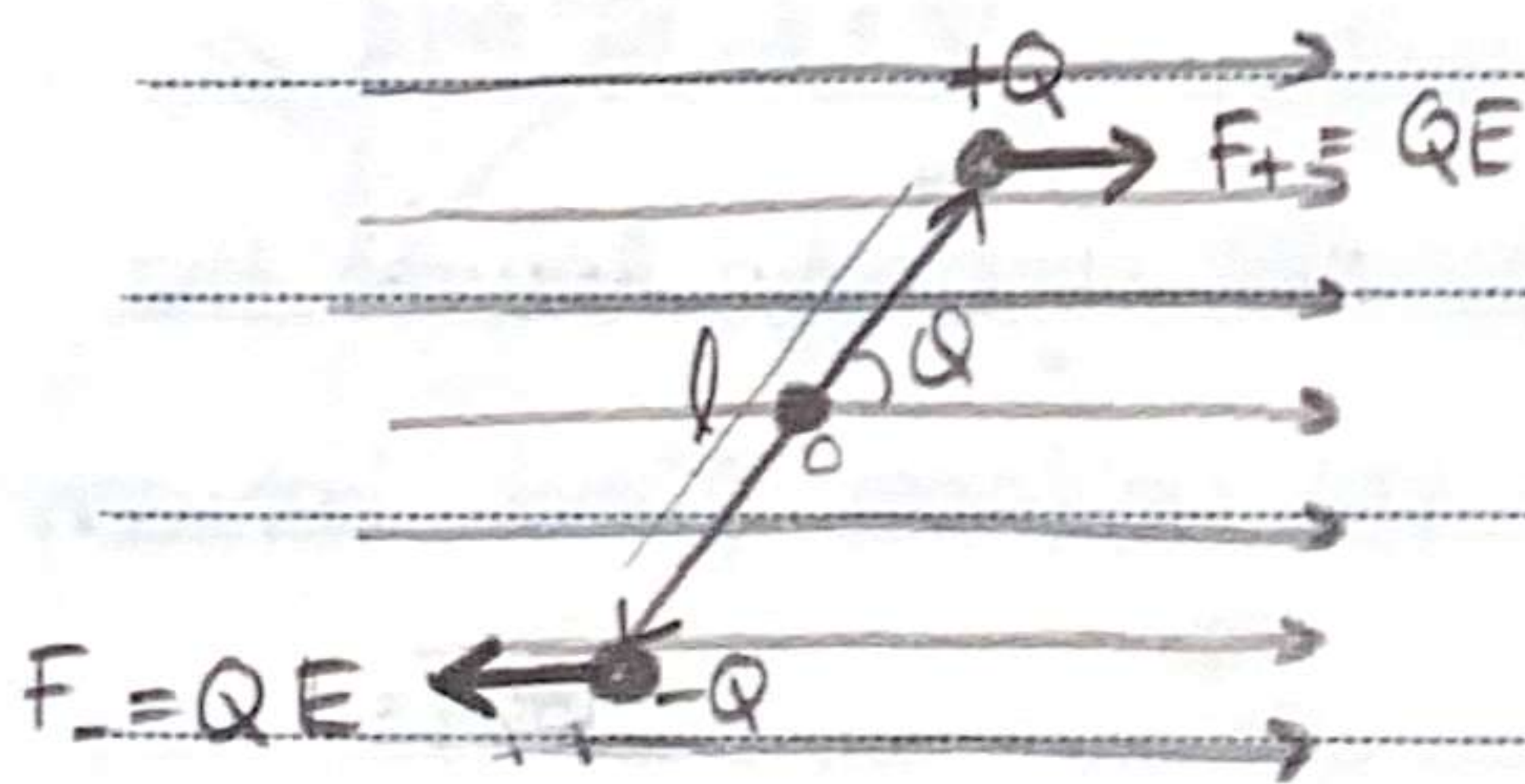
$$y = y_0 + v_{0y}t + \frac{1}{2}a_y t^2 \quad (y_0=0, v_{0y}=0)$$

ex 21.17



$\Rightarrow$  dipole moment

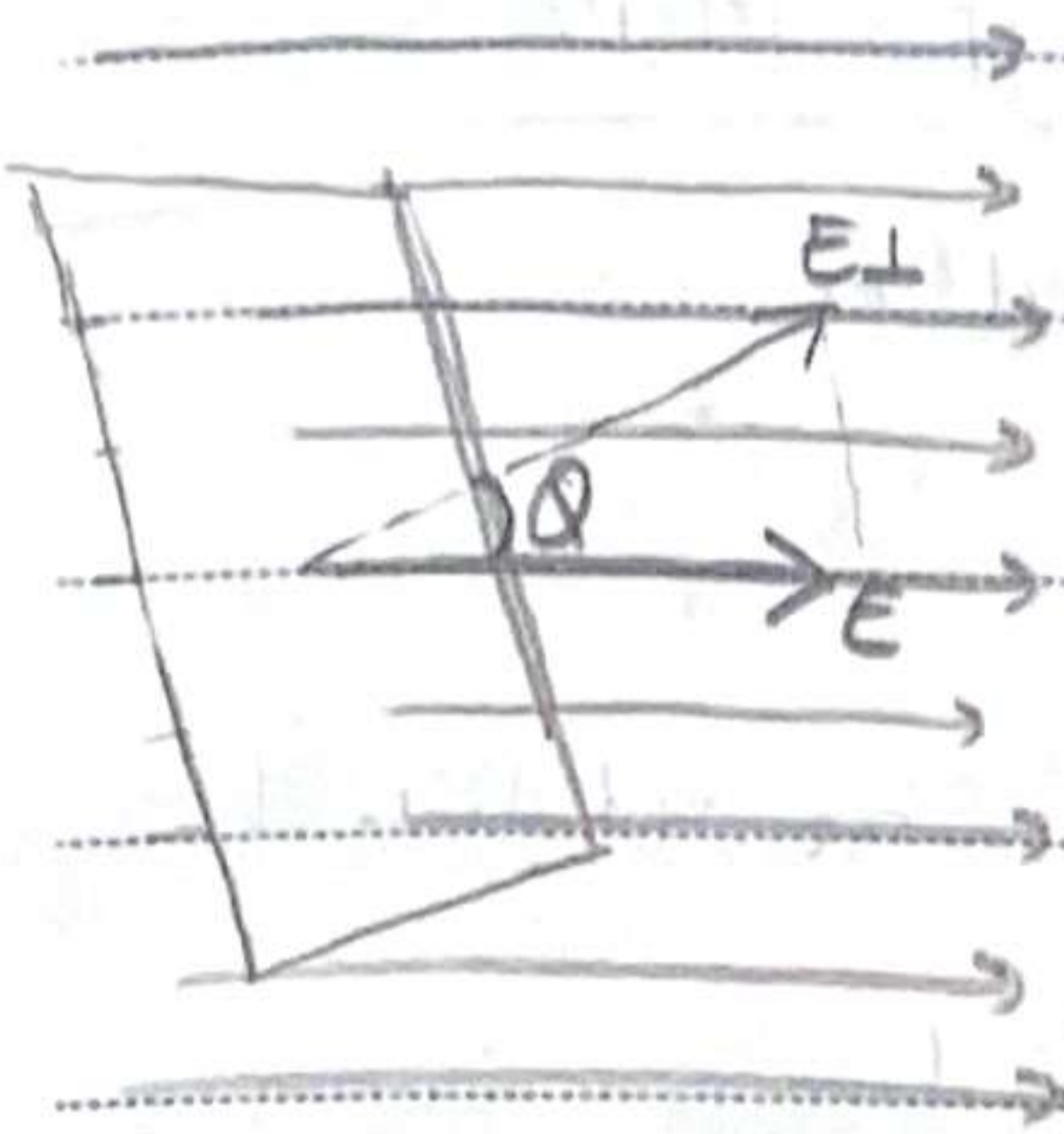
$$\vec{p} = Ql$$



$$\tau = \vec{p} E \sin(\theta) = \vec{p} \times E$$

$$\tau = \vec{p} \times E$$

## CHAPTER 22 GAUSS'S LAW



flux

$$\Phi_E = E \cdot A \cdot \cos \theta = E_{\perp} A$$

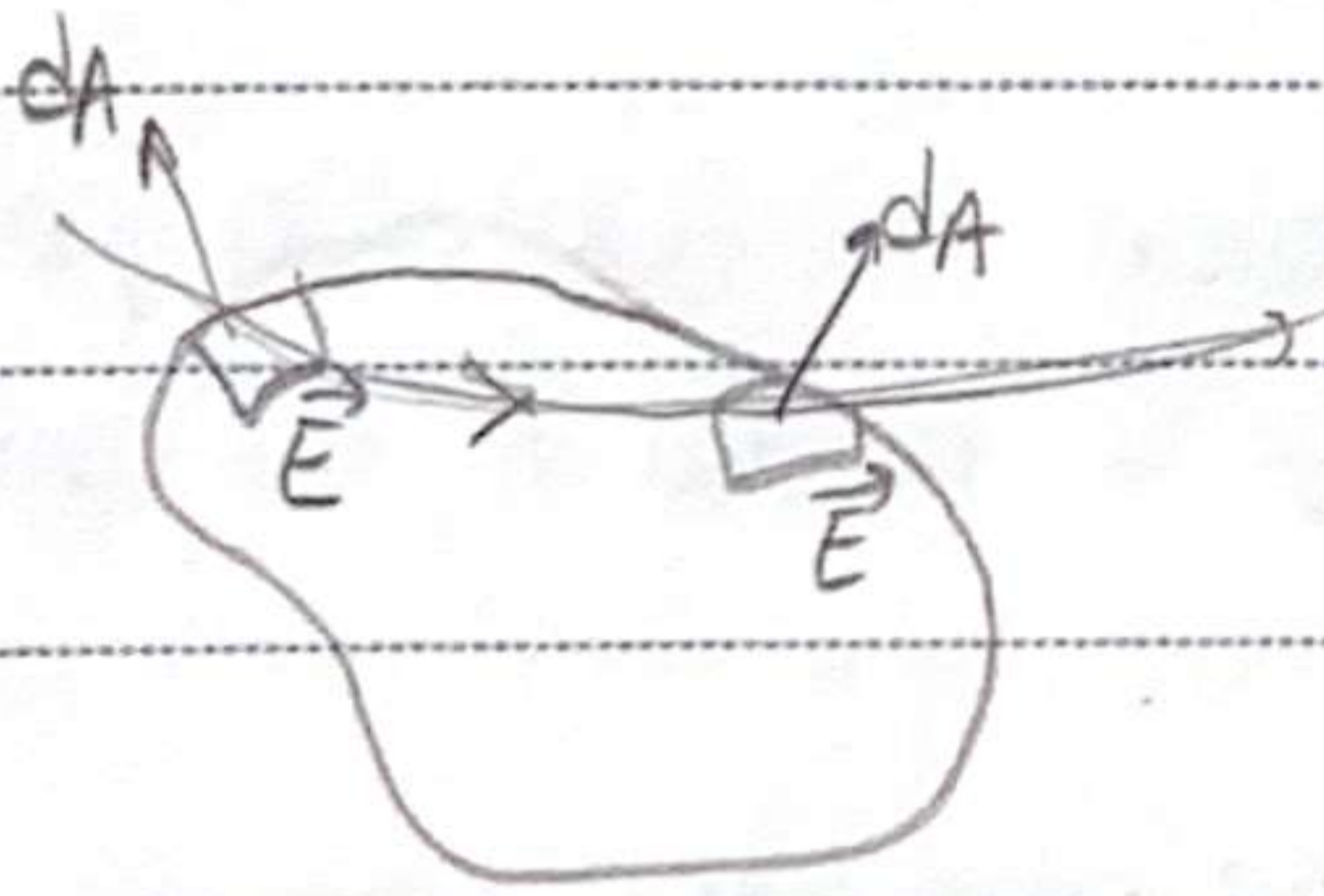
**ex 22.1** // Calculate the electric flux through the rectangle shown.

The rectangle is 10 cm by 20 cm. The electric field is uniform at 200 N/C, and the angle is  $30^\circ$  (görsel yukarıdaki gibi aynı ki daha asla çizemem.)

$$\Phi = \vec{E} \cdot \vec{A} = E \cdot A \cdot \cos \theta$$

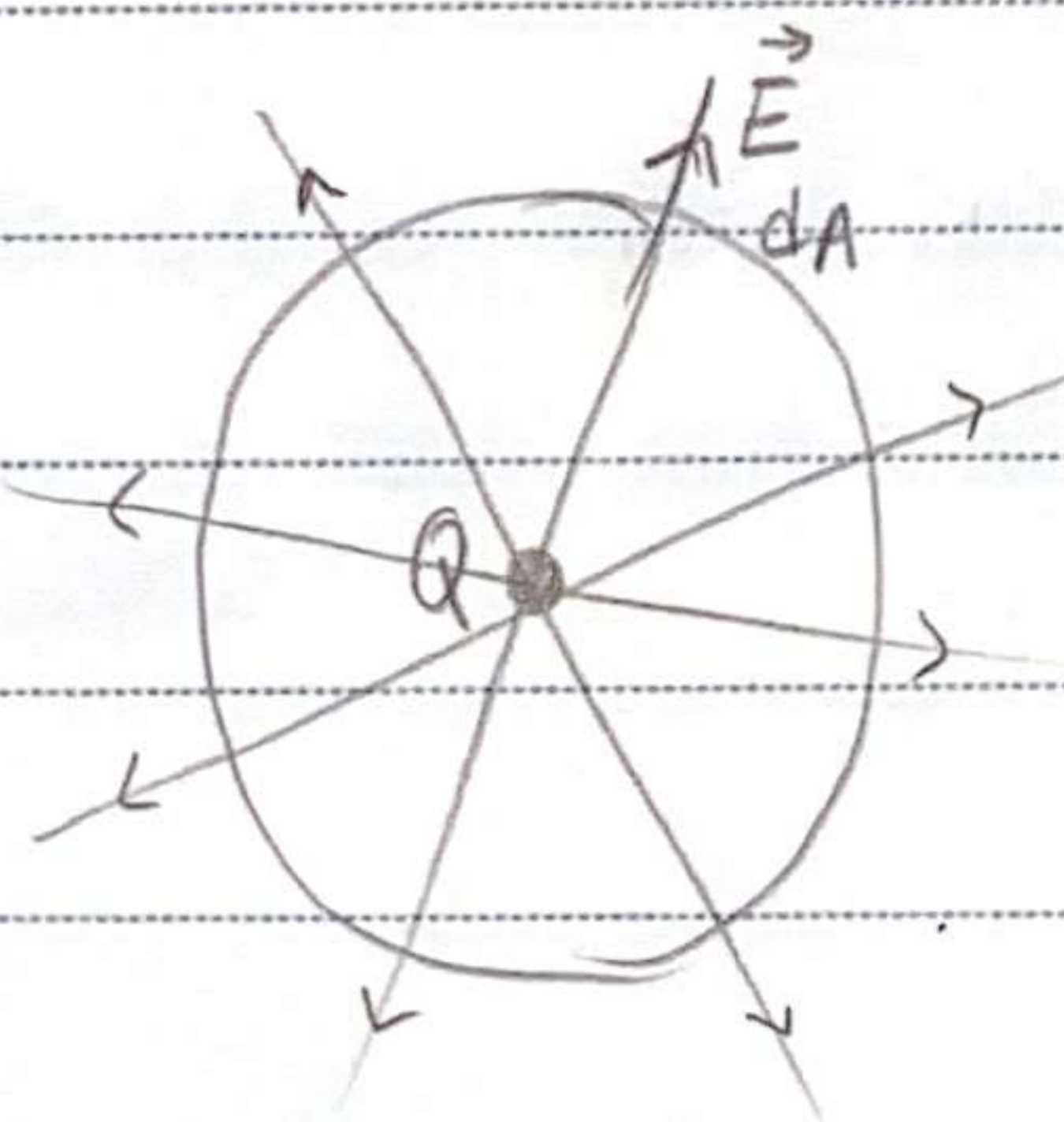
$$= (200 \text{ N/C}) (0.1 \text{ m} \times 0.2 \text{ m}) \cos 30 = 3.5 \text{ N} \cdot \text{m}^2 / \text{C}$$

(unit of  $\Phi = \frac{\text{N} \cdot \text{m}^2}{\text{C}}$ )



$$\Phi = \oint \vec{E} \cdot d\vec{A}$$

$$\Phi = \oint \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0}$$



$$E = \frac{Q}{4\pi \epsilon_0 r^2}$$

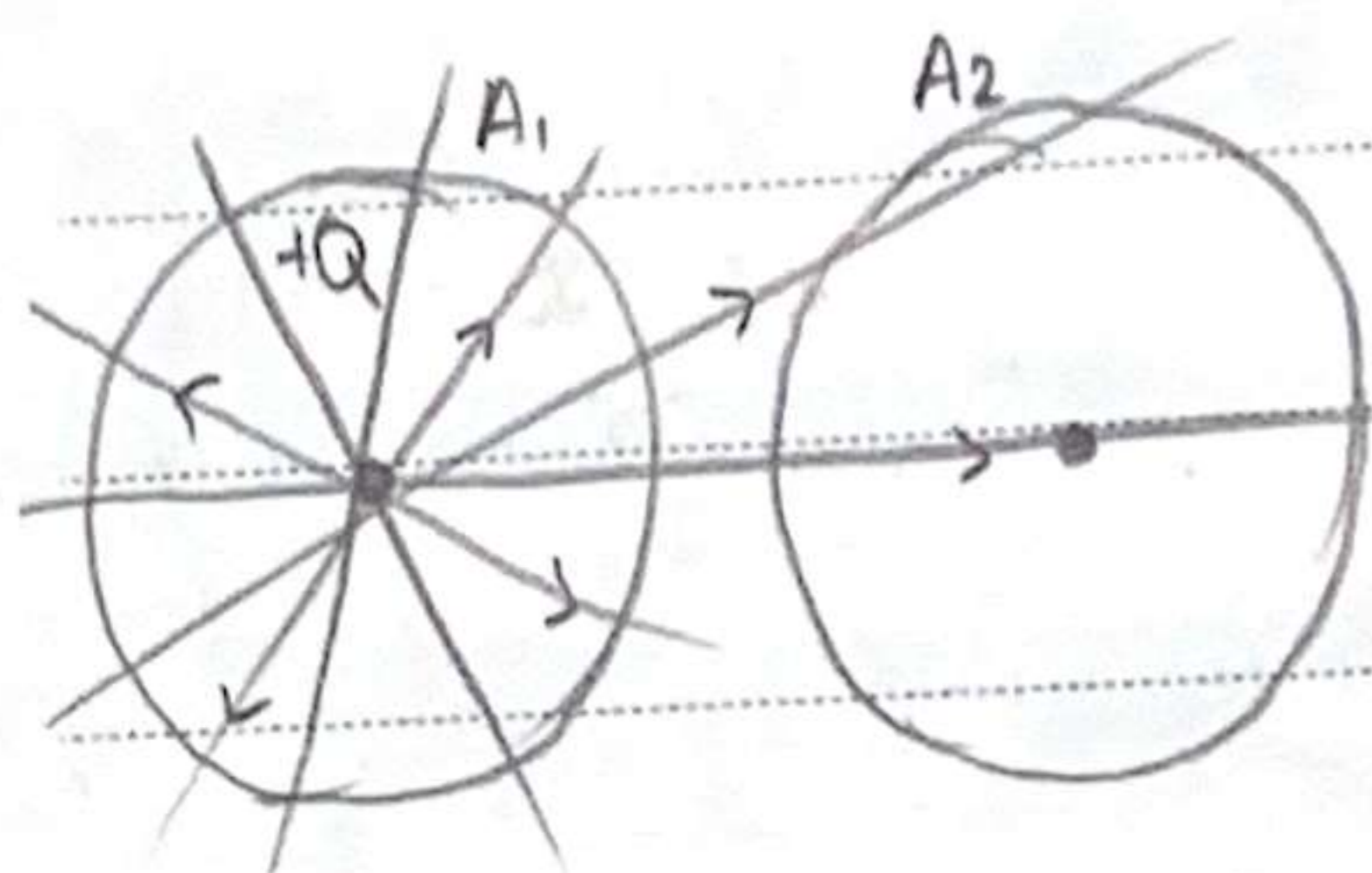
the electric field form of  
Coulomb's law

$$\sum Q_i = Q_{\text{encl}}$$

Record :

**ex 22.2** // Consider the two gaussian surfaces,  $A_1$  and  $A_2$  as shown. The only charge present is the charge  $Q$  at the center of surface  $A_1$ .

What is the net flux through each surface,  $A_1$  and  $A_2$ ?



For surface  $A_1$ ,

the net flux through  $A_1$

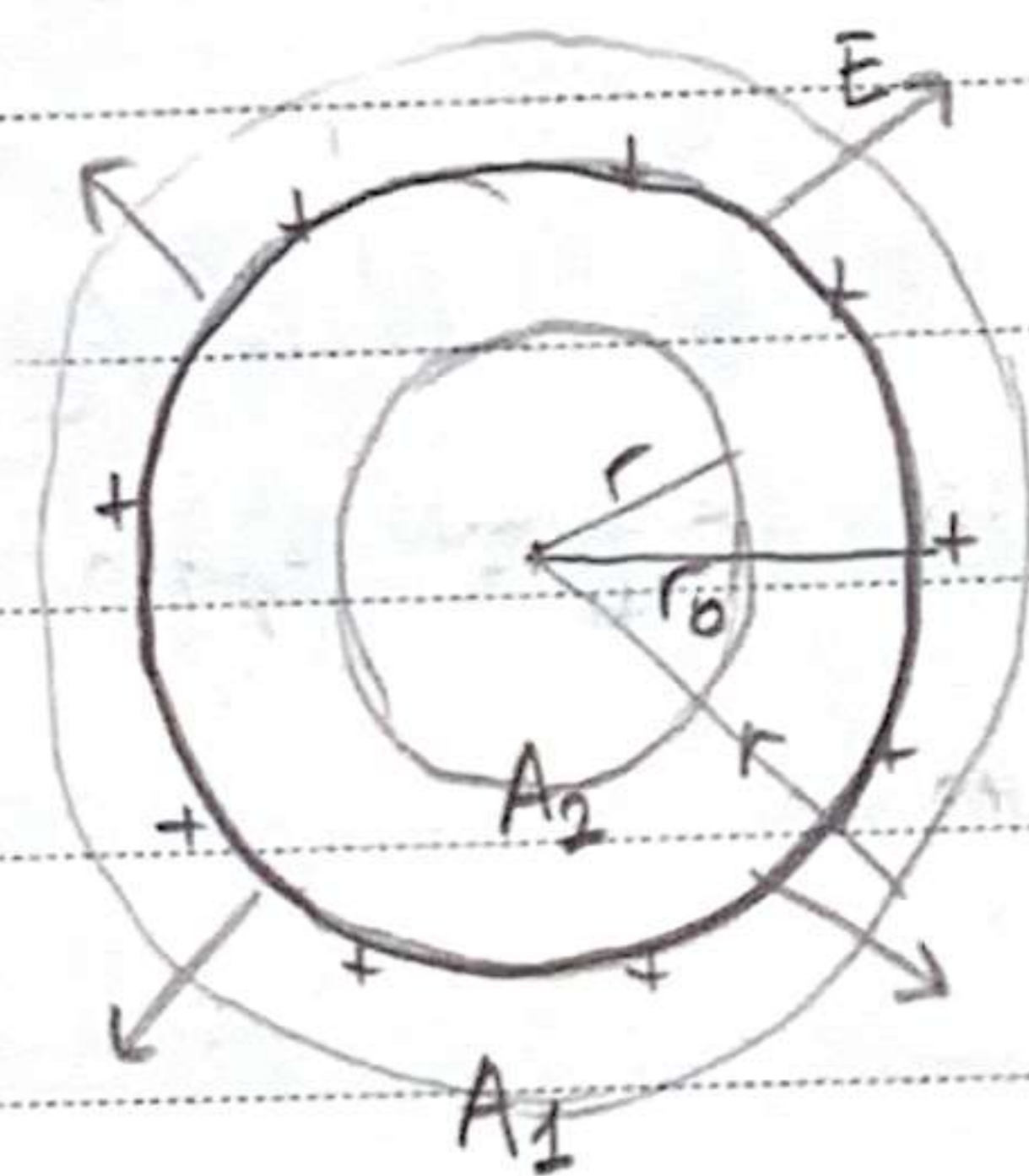
$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0} = \frac{+Q}{\epsilon_0}$$

For surface  $A_2$

the net flux through  $A_2$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0} = \frac{0}{\epsilon_0} = 0 //$$

**ex 22.3** // A thin spherical shell of radius  $r_0$  possesses a total charge  $Q$  that is uniformly distributed on it. Determine the electric field at points **a)** outside the shell



for  $r > r_0$ ,  $\vec{E}$  is parallel to  $d\vec{A}$

cosine of the angle between  $\vec{E}$  and  $d\vec{A}$  is always 1 //

$$\oint \vec{E} \cdot d\vec{A} = E \cdot (4\pi r^2) = \frac{Q_{\text{enc}}}{\epsilon_0} = \frac{Q}{\epsilon_0}$$

$$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r^2} \quad \left. \vphantom{E} \right\} \text{ is equivalent to the field of a point charge } Q \text{ located at the center.}$$

$$E \cdot 4\pi r^2 = \frac{Q}{\epsilon_0} \Rightarrow E = \frac{1}{4\pi r^2} \cdot \frac{Q}{\epsilon_0}$$

**b)** within (inside) the shell

$Q_{\text{enc}} = 0$  inside the shell

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0} = 0$$

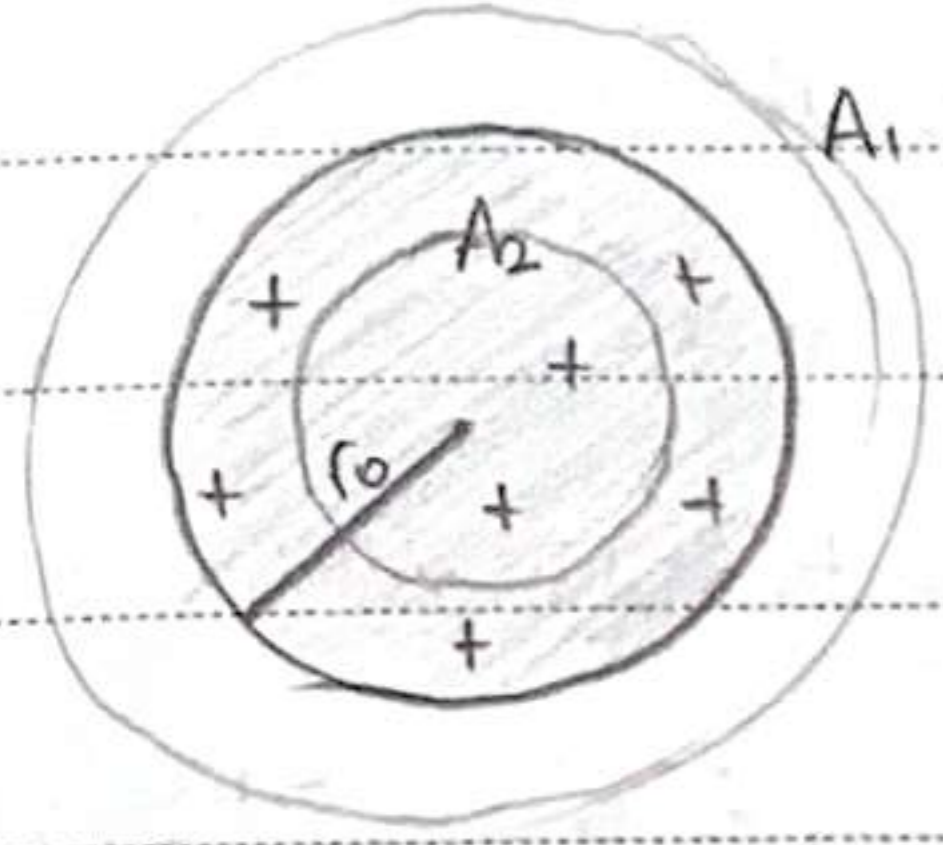
$$\Rightarrow E = 0 //$$

**c)** What if the conductor were a solid sphere?

$\Rightarrow$  We obtain same results because all charge would lie in a thin layer at the surface.

Record :

**ex 22.4** // An electric charge Q is distributed uniformly throughout a nonconducting sphere of radius r<sub>0</sub>. Determine the electric field



a) outside the sphere (r > r<sub>0</sub>)    b) inside the sphere (r < r<sub>0</sub>)

For r > r<sub>0</sub>

$$\oint \vec{E} \cdot d\vec{A}' = \frac{Q_{encl}}{\epsilon_0}$$

$$E \cdot (4\pi r^2) = \frac{Q}{\epsilon_0} \Rightarrow E = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r^2}$$

obtain same results with a point charge located at the center of sphere

**b) inside the sphere (r < r<sub>0</sub>)**

for (r < r<sub>0</sub>)  $\Rightarrow \oint \vec{E} \cdot d\vec{A} = E \cdot (4\pi r^2) = \frac{Q_{encl}}{\epsilon_0} \rightarrow$  Q<sub>encl</sub> is the charge enclosed by A<sub>2</sub> the total charge Q is not equal to Q<sub>encl</sub> but only a portion of it.

$$\int E = \frac{dQ}{dV} ; \int E = \text{constant}$$

↓

the charge density

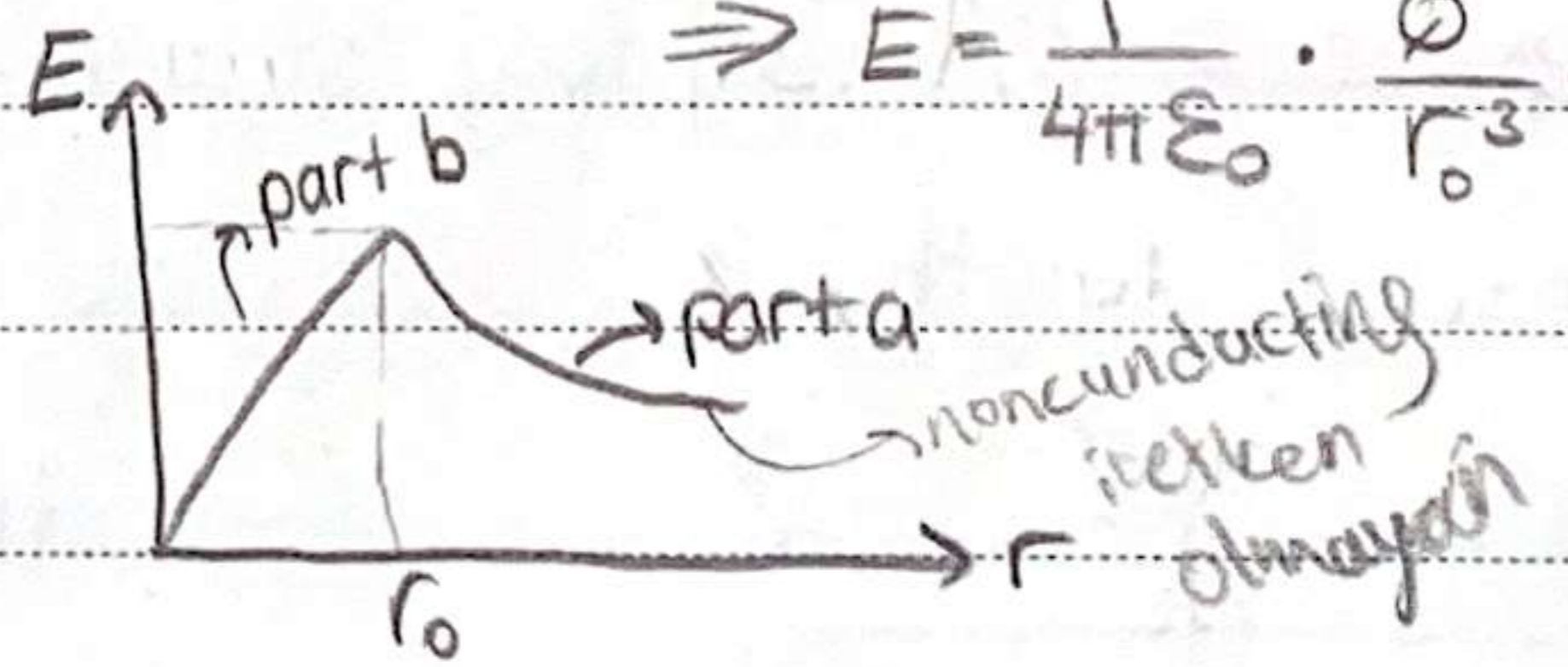
$$\frac{4}{3}\pi r_0^3 \quad Q$$

$$\frac{4}{3}\pi r^3 \quad Q_{encl}$$

$$Q_{encl} = \frac{\frac{4\pi r^3}{3} \rho}{\frac{4\pi r_0^3}{3}} = \frac{r^3}{r_0^3} \cdot Q$$

$$E \cdot 4\pi r^2 = \frac{r^3}{r_0^3} \cdot \frac{Q}{\epsilon_0}$$

$$\Rightarrow E = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r_0^3} \cdot r$$

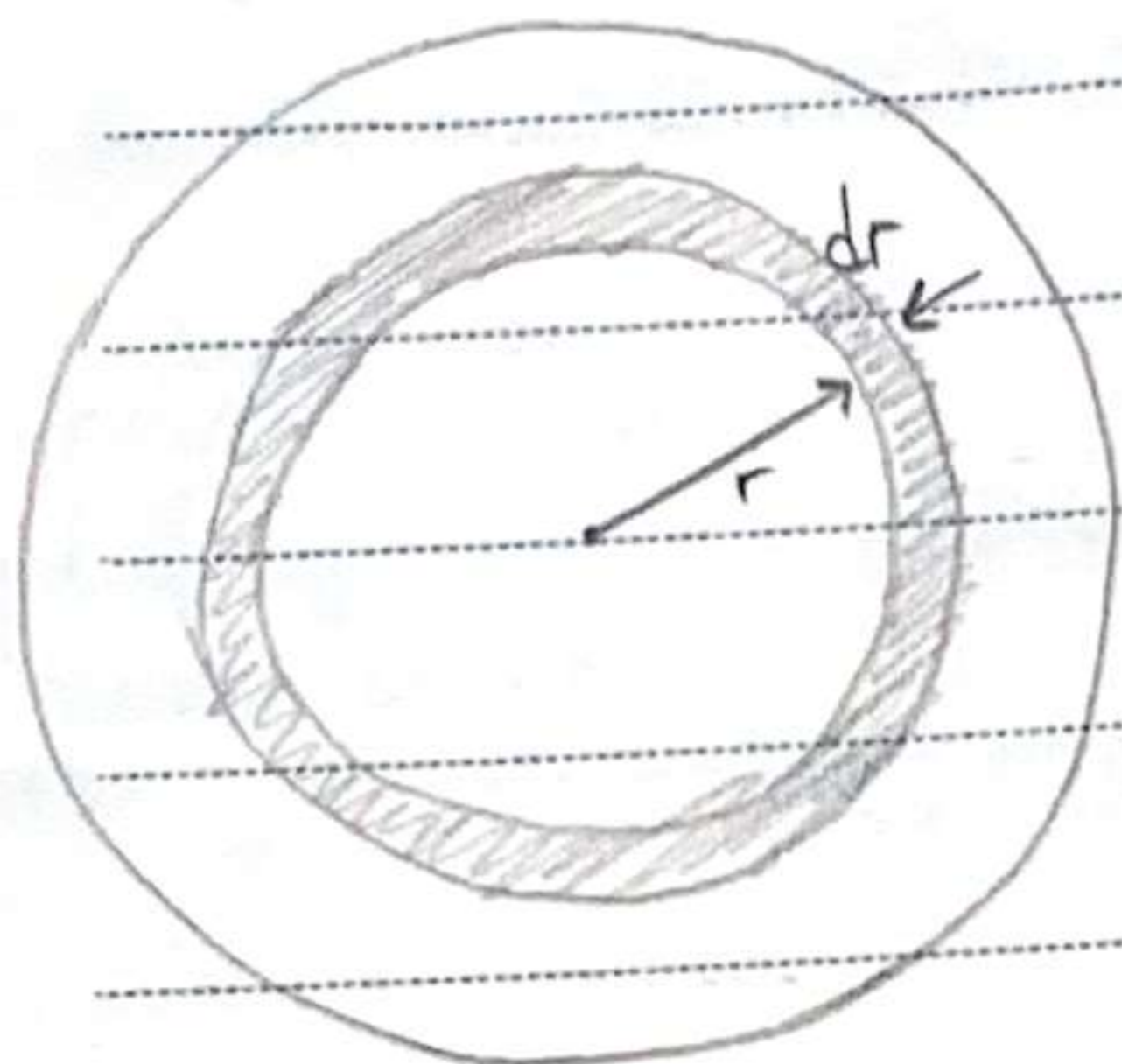


iletken

Record :

ex 22.5 // Suppose the charge density of a solid sphere is given

by  $\rho_E = a \cdot r^2$ , where  $a$  is constant.



a) Find  $a$  in terms of the total charge  $Q$  on the sphere and its radius  $r_0$ .

$$dQ = \rho_E \cdot dV$$

$$Q = \int \rho_E \cdot dV$$

$$dV = (4\pi r^2) dr$$

$$Q = \int_0^{r_0} (a \cdot r^2) \cdot (4\pi r^2) dr$$

$$Q = a \cdot 4\pi \int_0^{r_0} r^4 dr = \frac{4\pi a}{5} \cdot r_0^5$$

$$a = \frac{5Q}{4\pi r_0^5} //$$

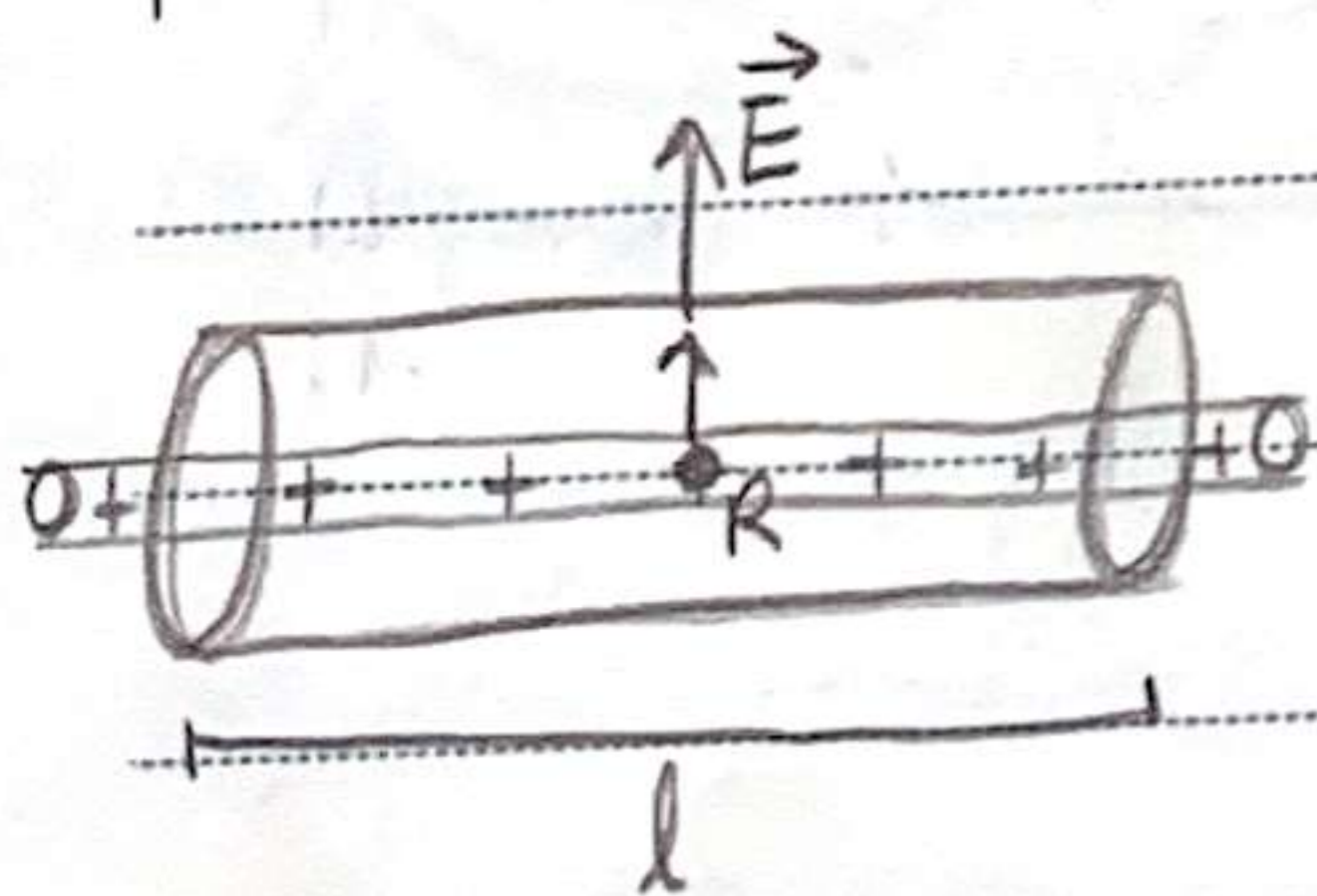
b) Find the electric field as a function of  $r$  inside the sphere.

$$Q_{encl} = \int \rho_E \cdot dV = \int_0^r (a \cdot r^2) \cdot (4\pi r^2) dr$$

$$\left. \begin{aligned} & \int_0^r \left( \frac{5Q r^2}{4\pi r_0^5} \right) (4\pi r^2) dr = \frac{Q r^5}{r_0^5} \end{aligned} \right\}$$

$$\Rightarrow \frac{Q r^5}{r_0^5} \Rightarrow \oint \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0} \Rightarrow E(4\pi r^2) = \frac{Q \cdot r^5}{r_0^5 \cdot \epsilon_0} \Rightarrow E = \frac{Q \cdot r^3}{4\pi r_0^5 \epsilon_0}$$

ex 22.6 // A very long straight wire possesses a uniform positive charge per unit length,  $\lambda$ . Calculate the electric field at points near (but outside) the wire, far from the ends.



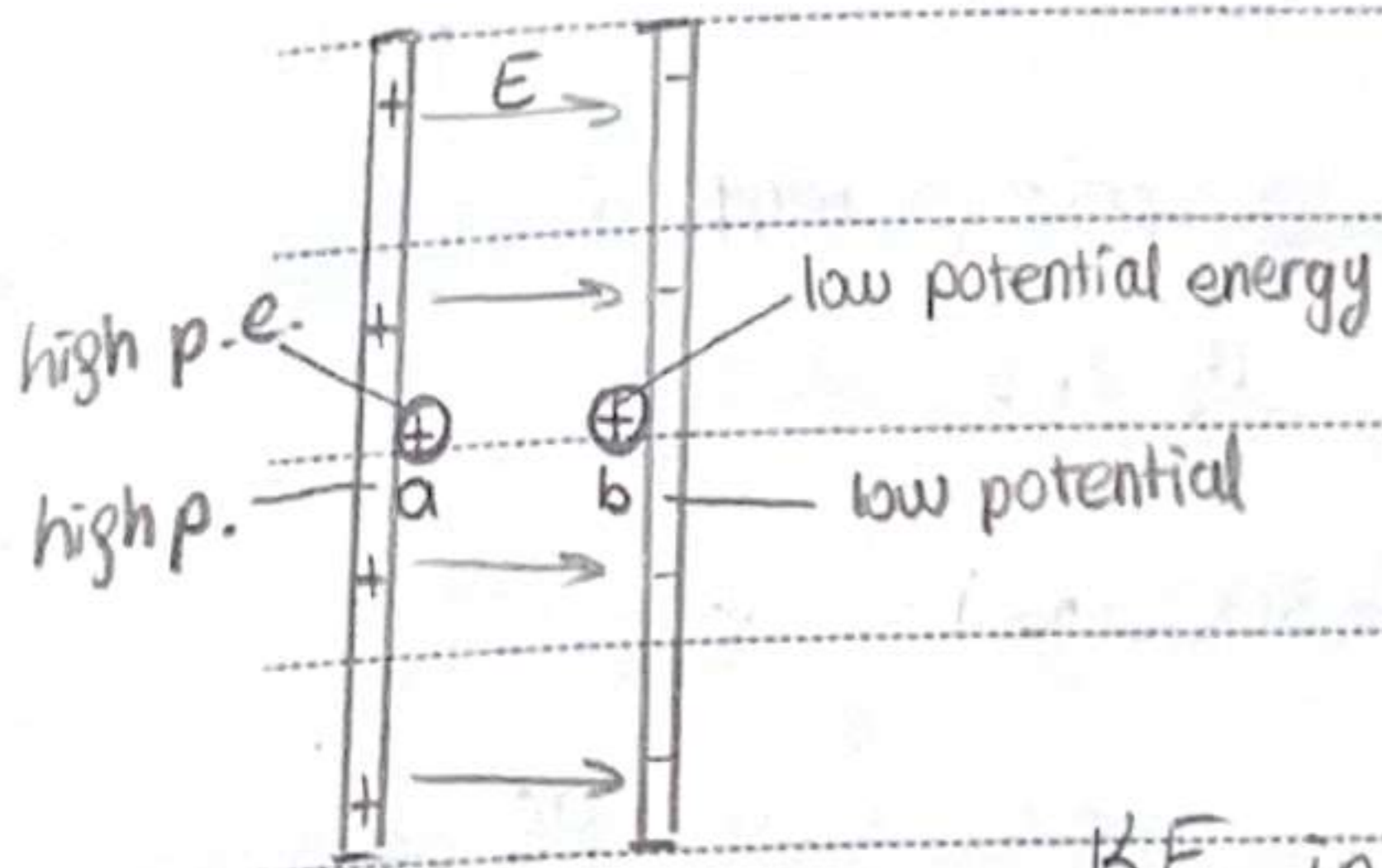
$\Rightarrow$  because of symmetry,  $\vec{E}$  to be directed radially outward.

$$\oint \vec{E} \cdot d\vec{A} = E(2\pi R l) = \frac{Q_{encl}}{\epsilon_0} = \frac{\lambda \cdot l}{\epsilon_0}$$

$$\hookrightarrow E = \frac{1}{2\pi \epsilon_0} \cdot \frac{\lambda}{R} \quad \text{where } l \ll \text{length of wire.}$$

Record :

CHAPTER 23 ~ ELECTRIC POTENTIAL



~ The electrostatic force is conservative

$$U_b - U_a = -W = -qEd$$

KE increases  
 $\Rightarrow$  PE decreases, and the charged particle accelerates from a to b.  
 $\Rightarrow$  electric PE is transformed into KE so total E conserved

$$V_a = \frac{U_a}{q}$$

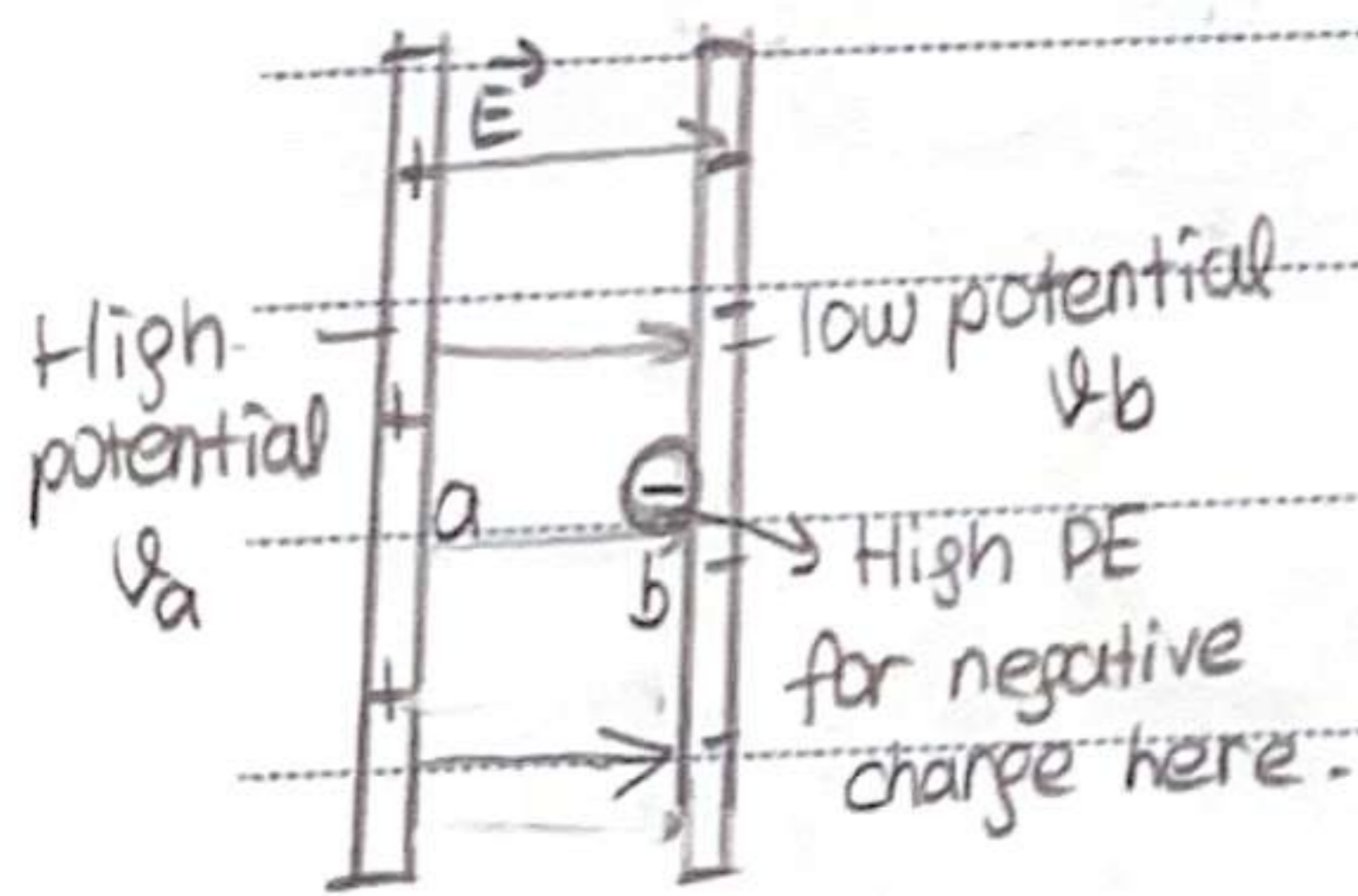
$$1 \text{ Volt} = 1 \text{ J/C}$$

$$V_{ba} = \Delta V = \frac{U_b - U_a}{q} = \frac{W_{ba}}{q}$$

$$U = V \cdot q$$

(-) charges move towards high electric potential  
 (+) " " " " low " "

**ex 23.1** // Suppose a negative charge, such as an electron, is placed near the negative plate at point b, as shown here. If the electron is free to move, will its electric potential energy



increase or decrease? How will the electric potential change?

$\Rightarrow$  PE decreases as its KE gets larger, so;

$$U_a < U_b$$

$$\Delta U = U_a - U_b < 0$$

$$\Rightarrow V_{ab} = V_a - V_b > 0$$

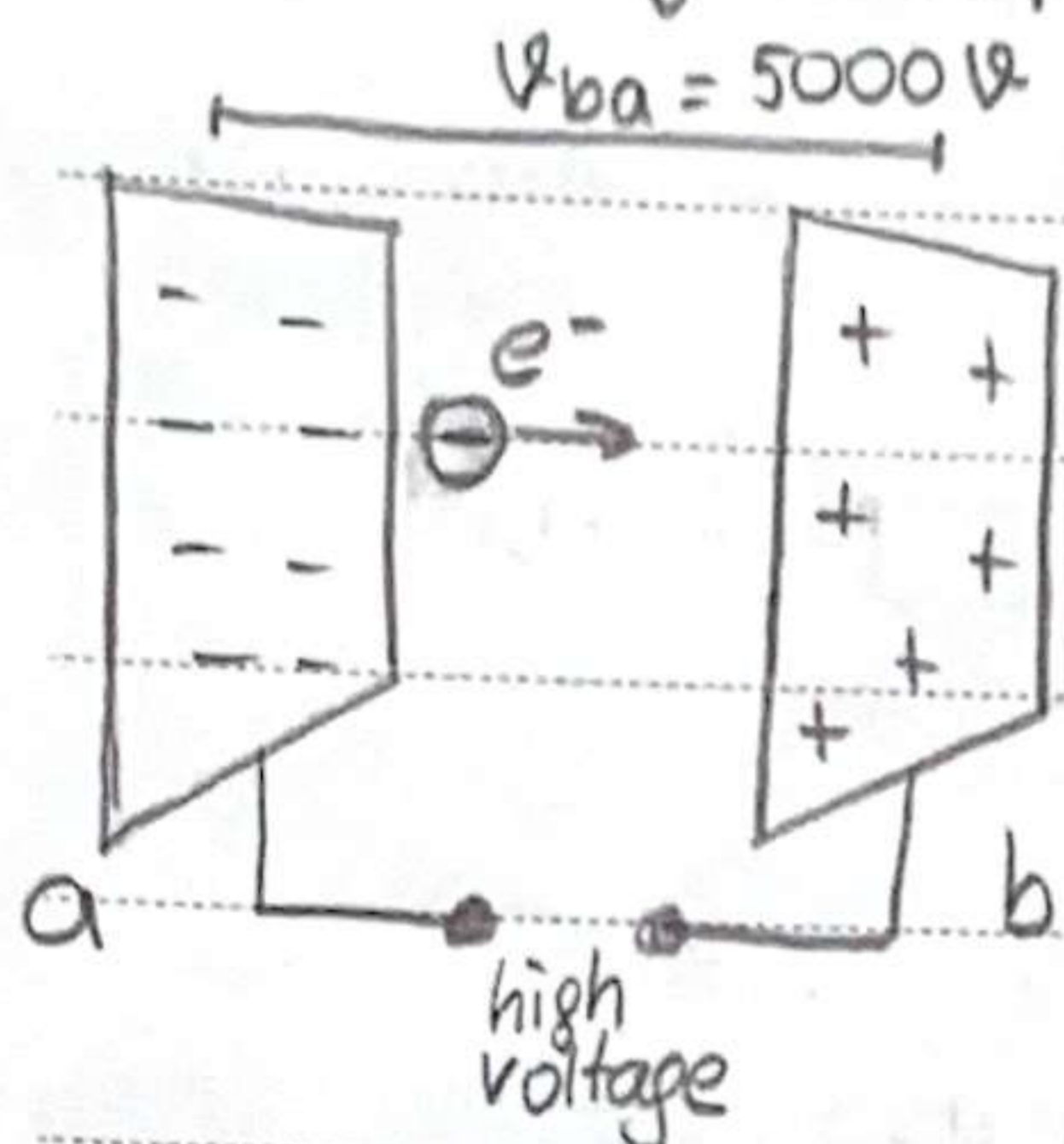
$\Rightarrow$  potential  $V_a$  and  $V_b$  are due to charges on the plates not due to electron.

$$\Delta U = U_b - U_a = q \cdot (V_b - V_a)$$

$$\Delta U = q \cdot V_{ba}$$

Record :

ex 23.2 // Suppose an electron in a cathode ray tube is accelerated from rest through a potential difference  $V_b - V_a = V_{ba} = +5000 \text{ V}$ .



a) What is the change in electric potential energy of the electron?

$$\Delta U = q \cdot V_{ba}$$

$$\Delta U = (-1.6 \times 10^{-19} \text{ C}) \cdot (+5000 \text{ V}) = -8 \cdot 10^{-16} \text{ J}$$

minus sign = PE decreases

b)  $\Delta K + \Delta U = 0$   
 $\Delta K = -\Delta U$  }  $\frac{1}{2}mv^2 - 0 = -q \cdot (V_b - V_a)$   
 $= -q \cdot V_{ba}$

$$v = \sqrt{\frac{-2qV_{ba}}{m}} = 4.2 \times 10^7 \text{ m/s}$$

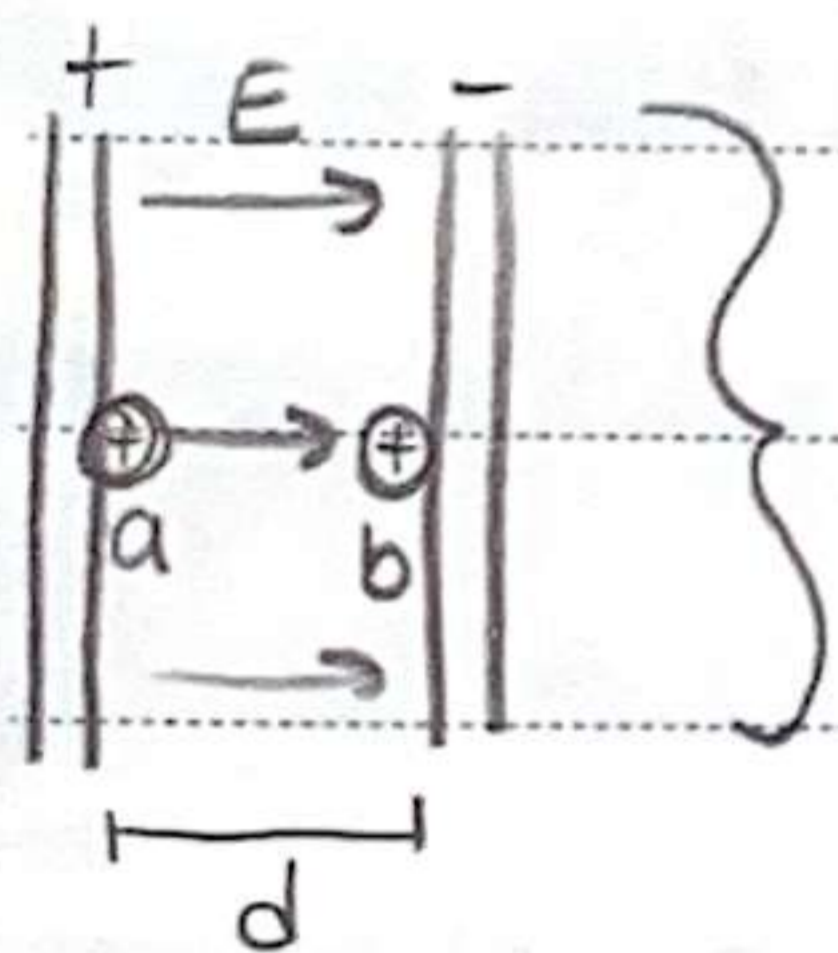
⇒ The difference in PE between

any two points ⇒  $U_b - U_a = -\int_a^b \vec{F} \cdot d\vec{l}$

$$V_b - V_a = \frac{U_b - U_a}{q}$$

$$\vec{E} = \frac{\vec{F}}{q}$$

$$\Rightarrow V_{ba} = -\int_a^b \vec{E} \cdot d\vec{l}$$



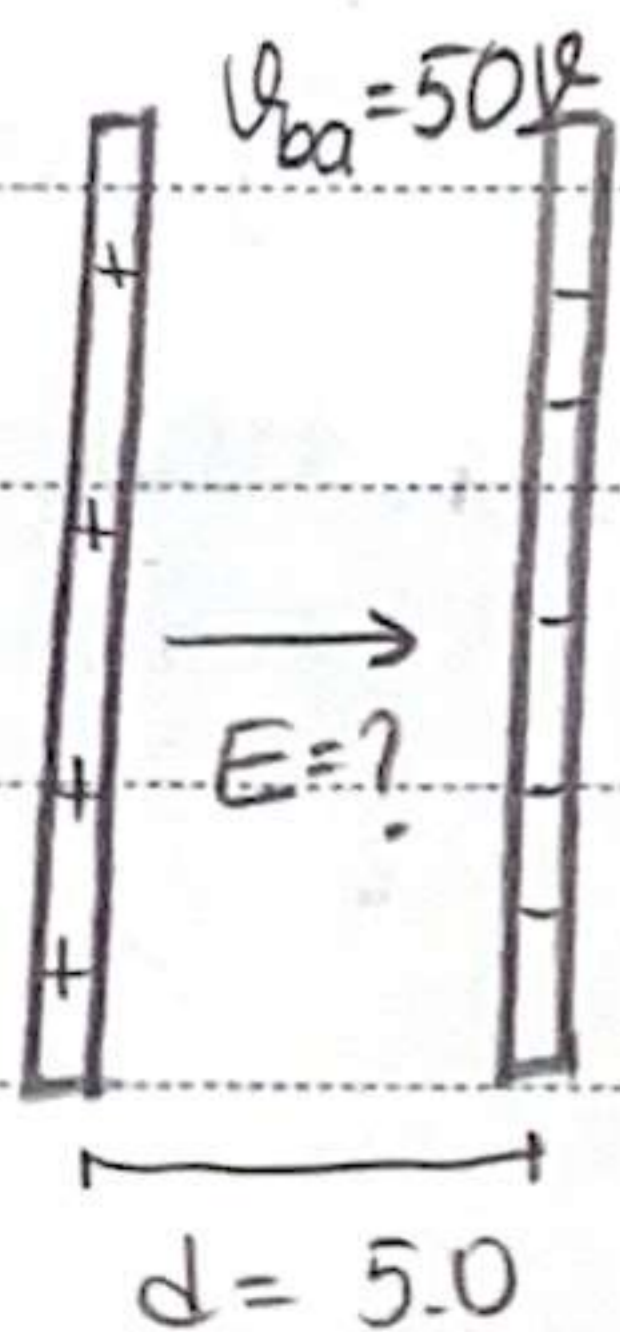
$$V_{ba} = -E \cdot d$$

ex 23.3 // two parallel plates are charged to produce a potential difference

of 50V, if the separation between the plates

is 0.050m, calculate the magnitude of the electric

field in the space between the plates.



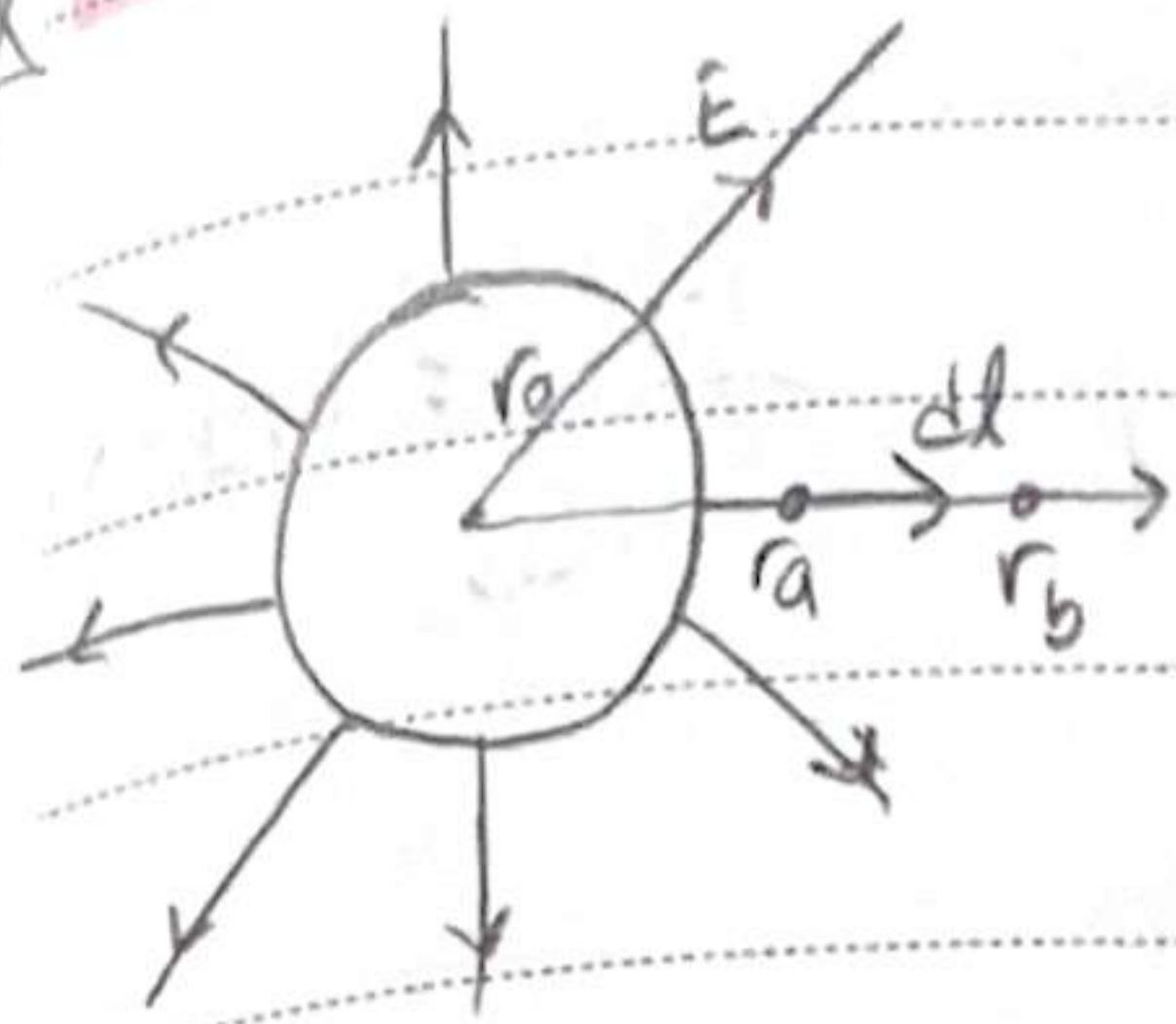
$$E = \frac{V_{ba}}{d} = \frac{50 \text{ V}}{0.05 \text{ m}} = 1000 \text{ V/m}$$

Express

Record:

ex 23.4

Determine the potential at a distance  $r$  from the center of a uniformly charged conducting sphere of radius  $r_0$ .



for a)  $r > r_0$ , b)  $r = r_0$ , c)  $r < r_0$ . The total charge on the sphere is  $Q$ .

$\rightarrow E = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r^2}$   $\rightarrow$  points radially outward if  $Q > 0$   
 $\rightarrow$  points radially inward if  $Q < 0$

$$V_b - V_a = - \int_{r_a}^{r_b} \vec{E} \cdot d\vec{l} = - \frac{Q}{4\pi\epsilon_0} \int_{r_a}^{r_b} \frac{dr}{r^2} \Rightarrow V_{ba} = \frac{Q}{4\pi\epsilon_0} \cdot \left( \frac{1}{r_b} - \frac{1}{r_a} \right)$$

a)  $\rightarrow$  lets choose  $V_b = 0$  at  $r_b = \infty \rightarrow V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r}$

b) as  $r$  approaches  $r_0$ , the potential difference at the surface of the conductor  $V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r_0}$ ,  $r_a = r_0$

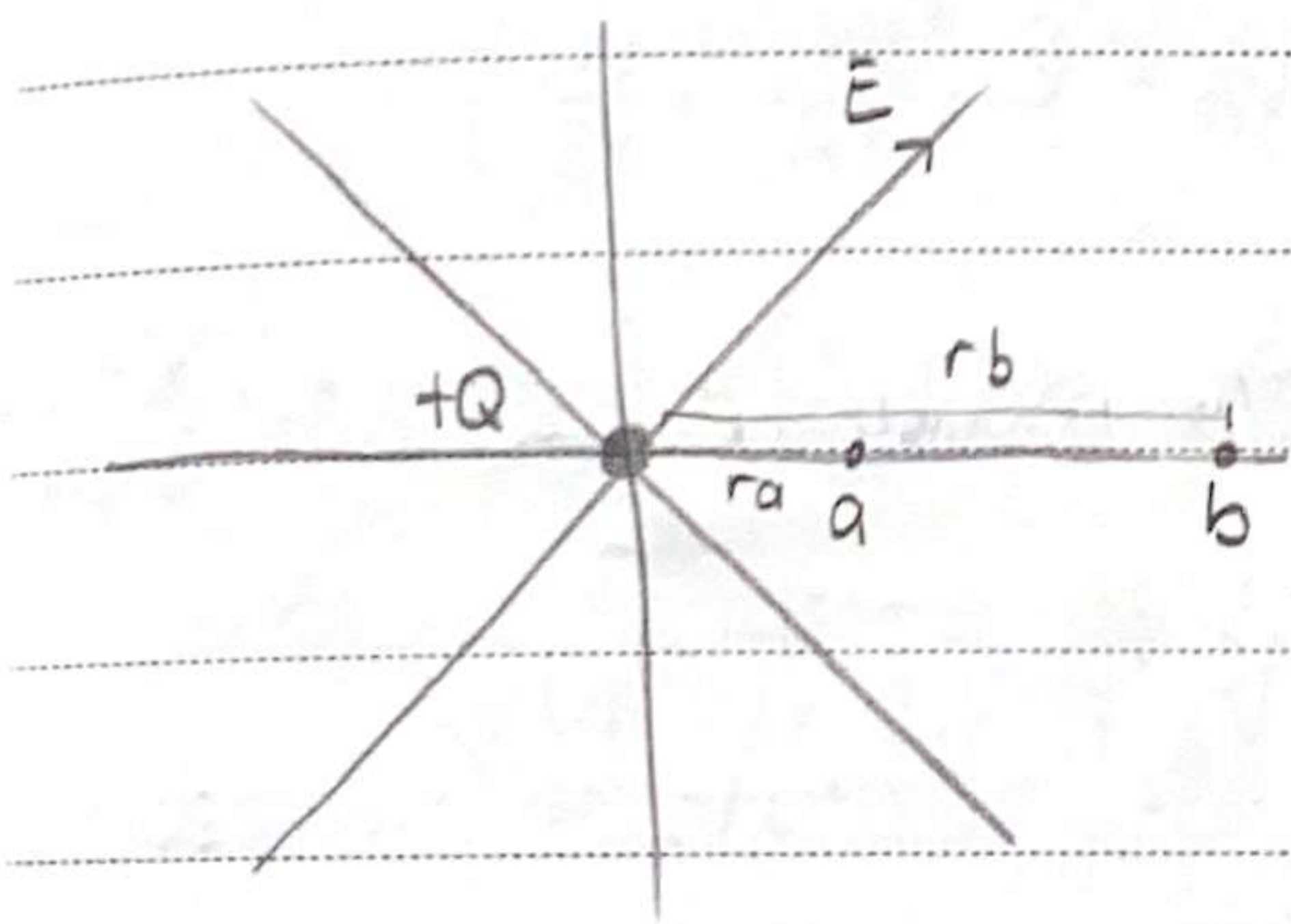
c) inside the conductor  $E = 0$   
 $\int \vec{E}' \cdot d\vec{l}' = 0$   
 $\downarrow$   
 the change in the potential }  $V$  is constant

for  $r < r_0$

$E = 0$     $V = \text{constant}$

for  $r > r_0$

$E \propto \frac{1}{r^2}$     $V \propto \frac{1}{r}$



$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r^2}$  } is directed radially outward from positive charge

$$V_b - V_a = - \int_{r_a}^{r_b} E' \cdot dl' = - \frac{Q}{4\pi\epsilon_0} \cdot \int_{r_a}^{r_b} \frac{1}{r^2} dr$$

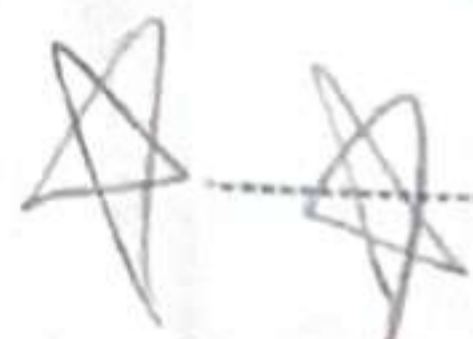
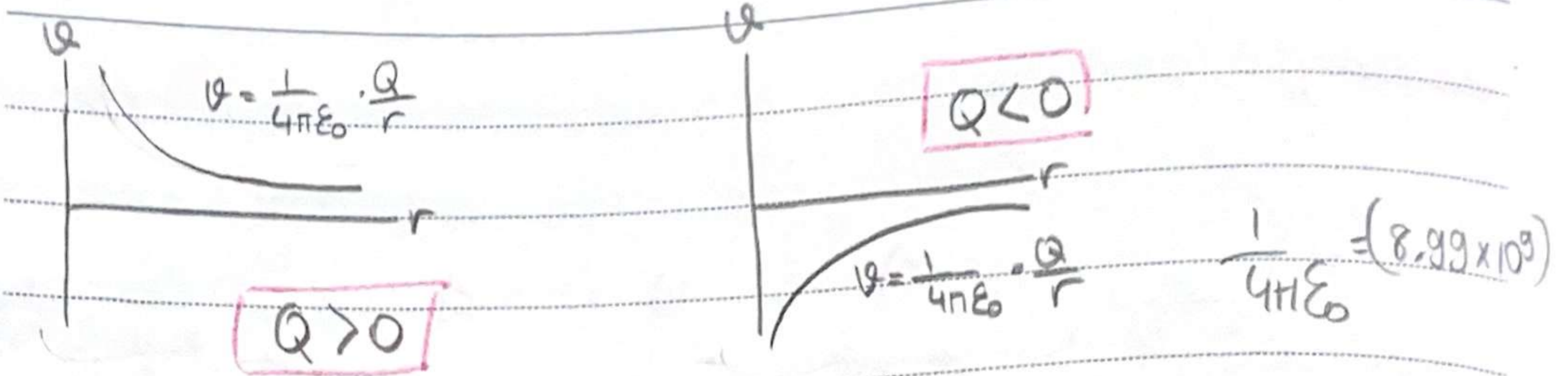
$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r}$

$V_{ba} = \frac{1}{4\pi\epsilon_0} \cdot \left( \frac{Q}{r_b} - \frac{Q}{r_a} \right)$

$\rightarrow$  the electric potential expression



Record :



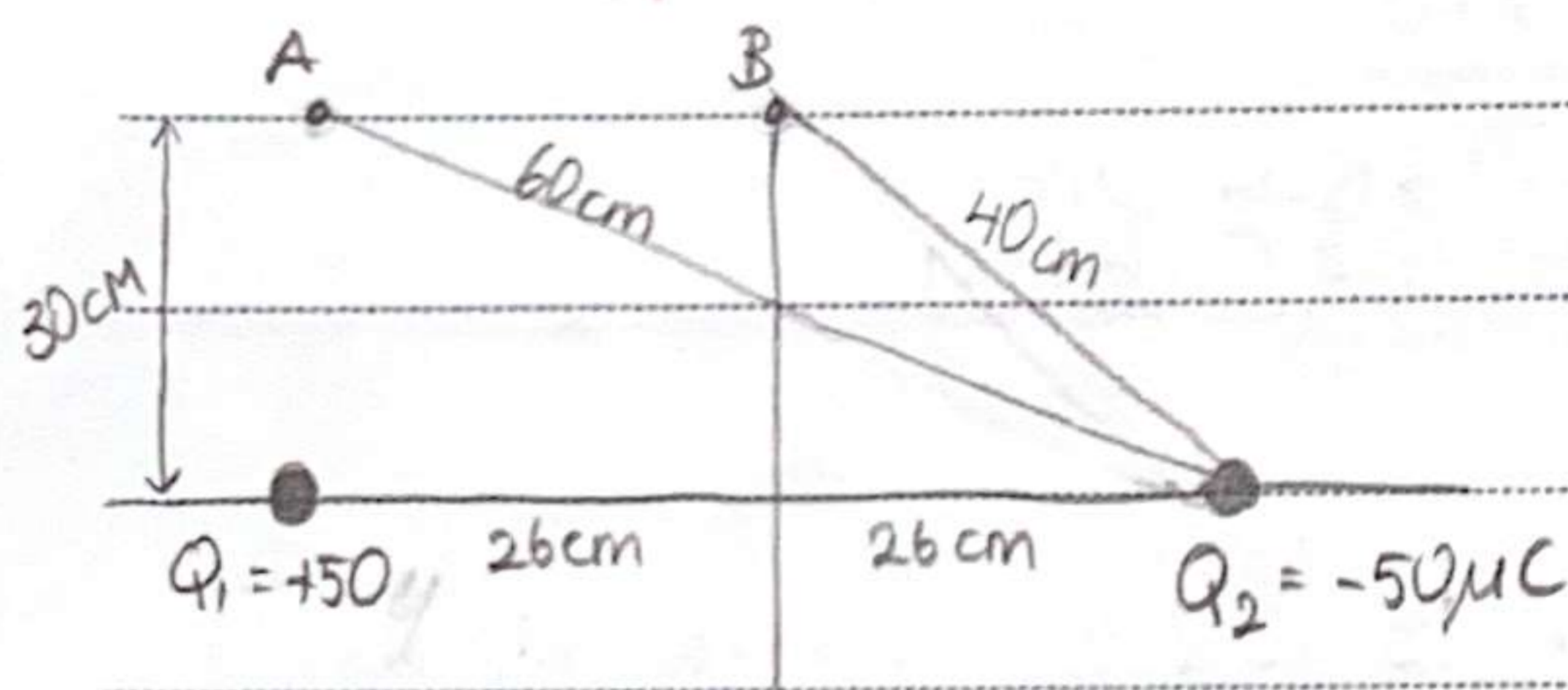
**ex 23.6** // What minimum work must be done by an external force to bring a charge  $q = 3.00 \mu\text{C}$  from a great distance away (take  $r = \infty$ ) to a point  $0.500 \text{ m}$  from a charge  $Q = 20.0 \mu\text{C}$ ?

$$W = q \cdot (V_b - V_a) \rightarrow \text{change in PE}$$

$$W = q \cdot \left( k \cdot \frac{Q}{r_b} - k \cdot \frac{Q}{r_a} \right) \rightarrow r_a = \infty, r_b = 0.5 \text{ m} \rightarrow W = \frac{(3 \cdot 10^{-6} \text{ C})(8.99 \times 10^9)(2 \cdot 10^{-5})}{(0.5) \text{ m}}$$

$W = 1.08 \text{ J}$

**ex 23.7** // Calculate the electric potential



a) at point A due to 2 charges

$$V_A = V_{A_2} + V_{A_1}$$

$$V_A = k \cdot \left( \frac{Q_2}{r_{A_2}} + \frac{Q_1}{r_{A_1}} \right)$$

$$V_A = (9 \times 10^9) \left( \frac{(5 \times 10^{-5} \text{ C})}{0.3 \text{ m}} + \frac{(-5 \times 10^{-5} \text{ C})}{0.6 \text{ m}} \right)$$

b) at point B

$$V_B = V_{B_1} + V_{B_2}$$

$$V_B = (9 \times 10^9 \text{ Nm}^2/\text{C}^2) \left( \frac{(5 \times 10^{-5} \text{ C})}{0.4 \text{ m}} + \frac{(-5 \times 10^{-5} \text{ C})}{0.4 \text{ m}} \right)$$

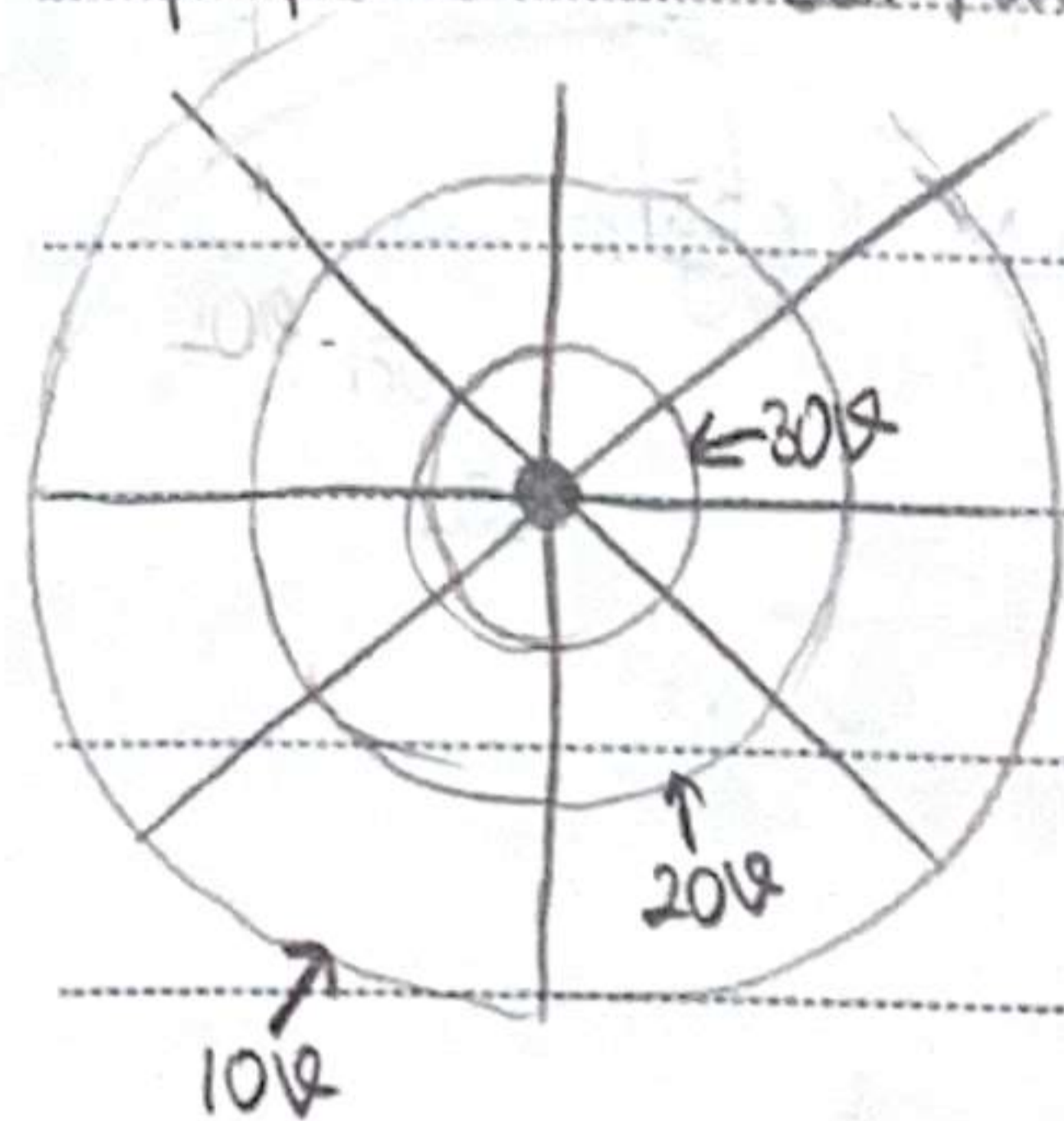
$$V_A = 7.5 \times 10^5 \text{ N}$$

$V_B = 0$  //  $\nabla$  the potential will be 0 everywhere on the plane

Record :

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r} \Rightarrow$$

ex 23.10 // For a single point charge with  $Q = 4.0 \times 10^{-9} \text{ C}$ , sketch the equipotential surfaces (or lines in a plane containing the charge) corresponding



to  $V_1 = 10 \text{ V}$ ,  $V_2 = 20 \text{ V}$  and  $V_3 = 30 \text{ V}$

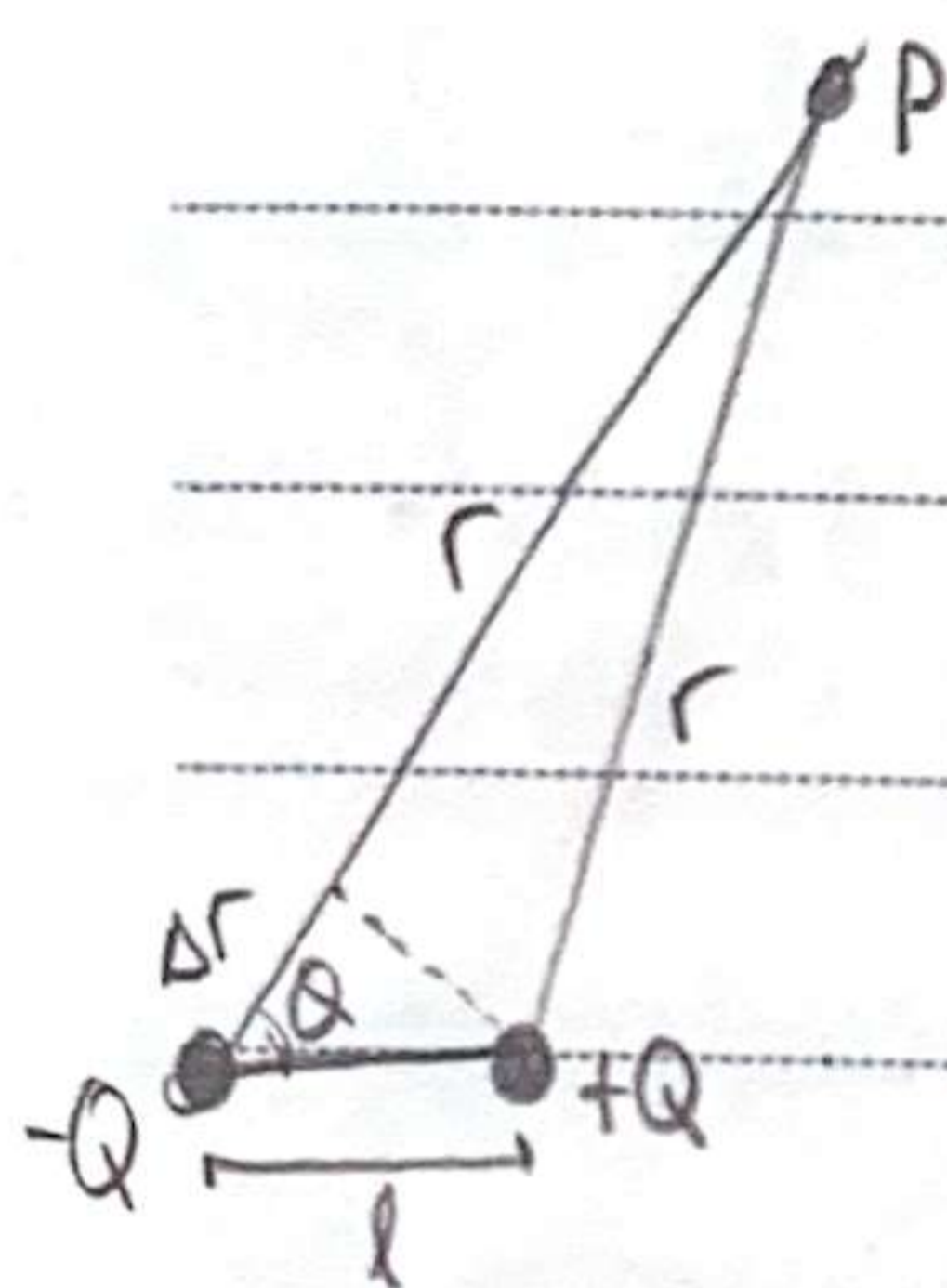
$$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r} \Rightarrow r = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{V}$$

$$\text{for } V_1 = 10 \text{ V} \rightarrow r_1 = \frac{(9 \cdot 10^9 \text{ Nm}^2/\text{C}^2)(4 \cdot 10^{-9} \text{ C})}{10 \text{ V}} = \boxed{3.6 \text{ M}}$$

$$\text{for } V_2 = 20 \text{ V} \rightarrow r_2 = \frac{(9 \cdot 10^9 \text{ Nm}^2/\text{C}^2)(4 \cdot 10^{-9} \text{ C})}{20 \text{ V}} = \boxed{1.8 \text{ M}}$$

$$\text{sooo } V_3 = 30 \rightarrow r_3 = \boxed{1.2 \text{ M}}$$

### electric dipole potential



$\Rightarrow$  the electric potential, point P due to a dipole;

$$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r} + \frac{1}{4\pi\epsilon_0} \cdot \frac{(-Q)}{(r + \Delta r)}$$

$$\hookrightarrow V = \frac{Q}{4\pi\epsilon_0} \cdot \frac{\Delta r}{r \cdot (\Delta r + r)}$$

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

$$\Delta r \approx l \cdot \cos \theta$$

$$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{p \cdot \cos \theta}{r^2}$$

$$p = Q \cdot l \quad \left. \vphantom{p = Q \cdot l} \right\} \text{dipole moment}$$

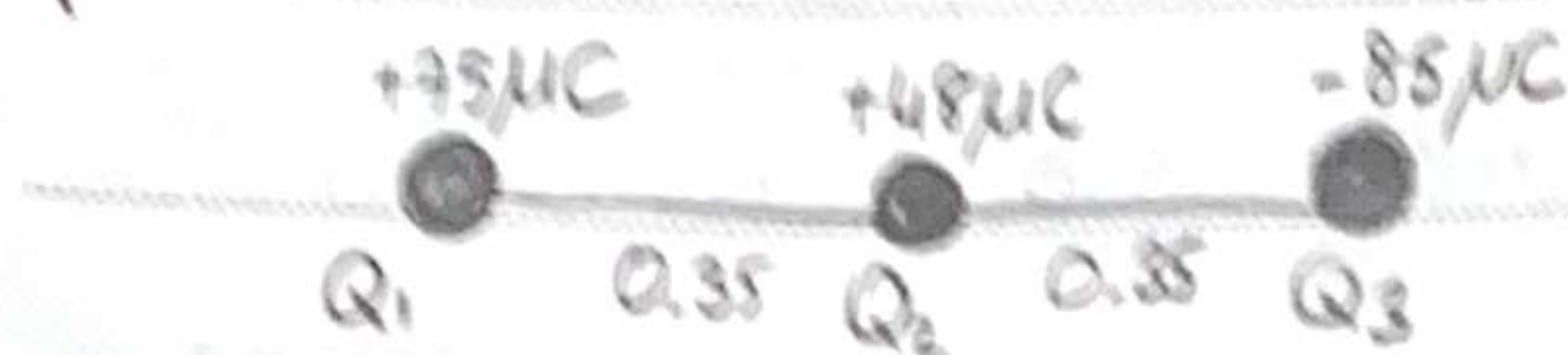
$$E_l = -\frac{dV}{dl}$$

$$U = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 \cdot Q_2}{r_{12}}$$

PROBLEM SOLUTIONS 1 ~ CHAPTER 21

Q 12 -

Calculate the net force on each charge due to the other two?



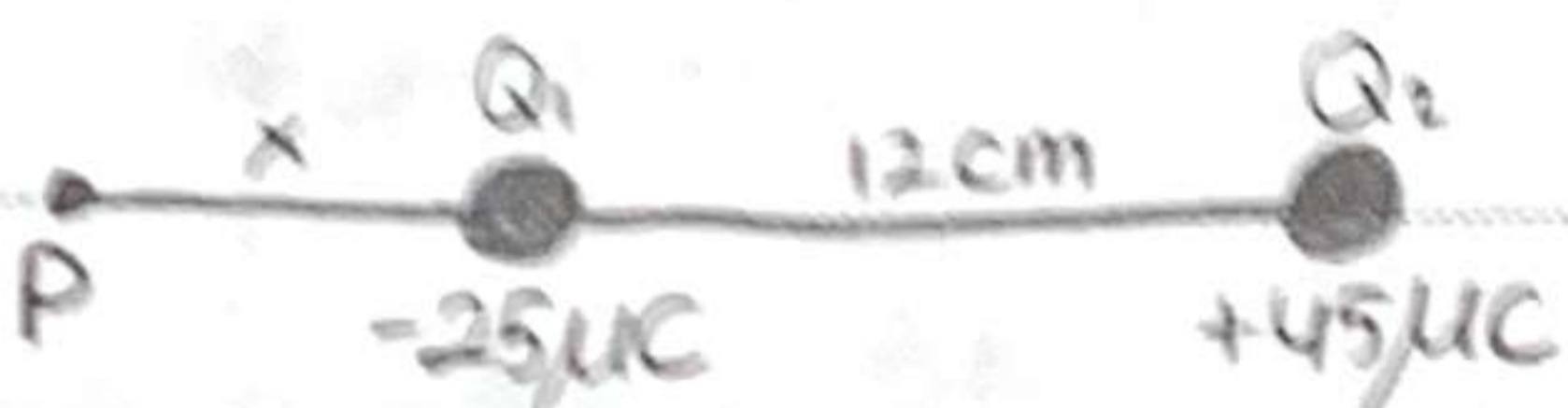
$F_1 = \leftarrow \bullet \bullet \rightarrow$   $F_{12} = k \frac{Q_1 Q_2}{r^2} = 8.988 \times 10^9 \frac{(75 \times 10^{-6})(48 \times 10^{-6})}{(0.35)^2} = 264 \times 10^{-3}$   
 $F_{13} = k \frac{Q_1 Q_3}{r^2} = 8.988 \times 10^9 \frac{(75 \times 10^{-6})(85 \times 10^{-6})}{(0.7)^2} = 117 \times 10^{-3}$

$F_2 = \bullet \bullet \rightarrow$   $F_{23} = k \frac{Q_2 Q_3}{r^2} = 8.988 \times 10^9 \frac{(48 \times 10^{-6})(85 \times 10^{-6})}{(0.35)^2} = 299 \times 10^{-3}$   
 $F_{21} = 264 \times 10^{-3}$

$F_3 = \bullet \bullet \leftarrow$   $F_{13} = 117 \times 10^{-3}$   
 $F_{23} = 299 \times 10^{-3}$  }  $417 \times 10^{-3}$

Q 36 -

electric field at the point is zero.  $x = ?$



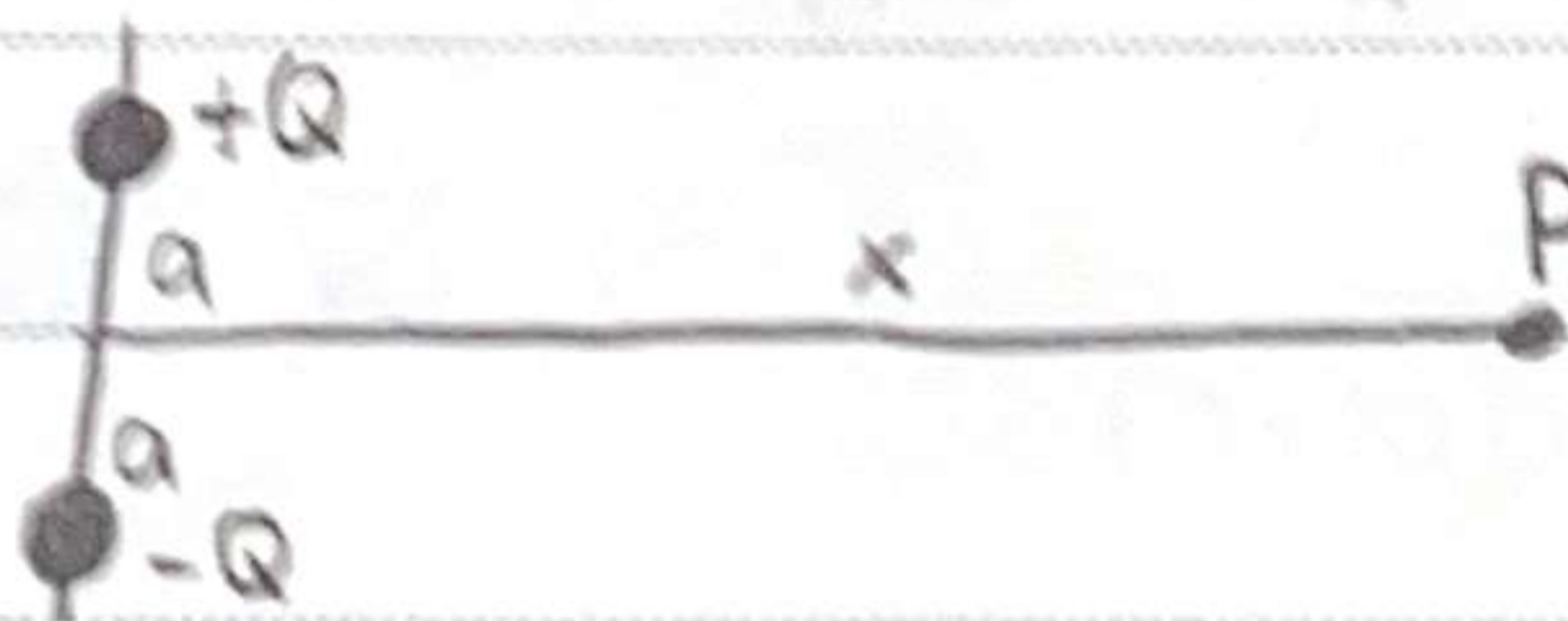
$|E_1| = |E_2|$

$k \frac{|Q_1|}{x^2} = k \frac{|Q_2|}{(x+12)^2} \Rightarrow \frac{25}{x^2} = \frac{45}{(x+12)^2}$

$x = 35.128$  }  $\begin{cases} 9x^2 = 5x^2 + 120x + 720 \\ x^2 - 30x - 180 = 0 \end{cases}$

Q 48 -

determine the direction and magnitude of the electric field at the point P?



$E_{+Q} = E_{-Q} = k \frac{Q}{(x^2 + a^2)^{\frac{3}{2}}}$

$2E_Q \cdot \sin \theta = 2 \cdot k \cdot \frac{Q}{(x^2 + a^2)^{\frac{3}{2}}} \cdot \sin \theta$

$E = E_Q \cdot \sin \theta$

$\sin \theta = \frac{a}{\sqrt{x^2 + a^2}}$

$2E = 2E_Q \cdot \sin \theta$

$\frac{2kQa}{(x^2 + a^2)^{\frac{3}{2}}}$

Record :

PROBLEM SOLUTIONS 21 ~ CHAPTER 23

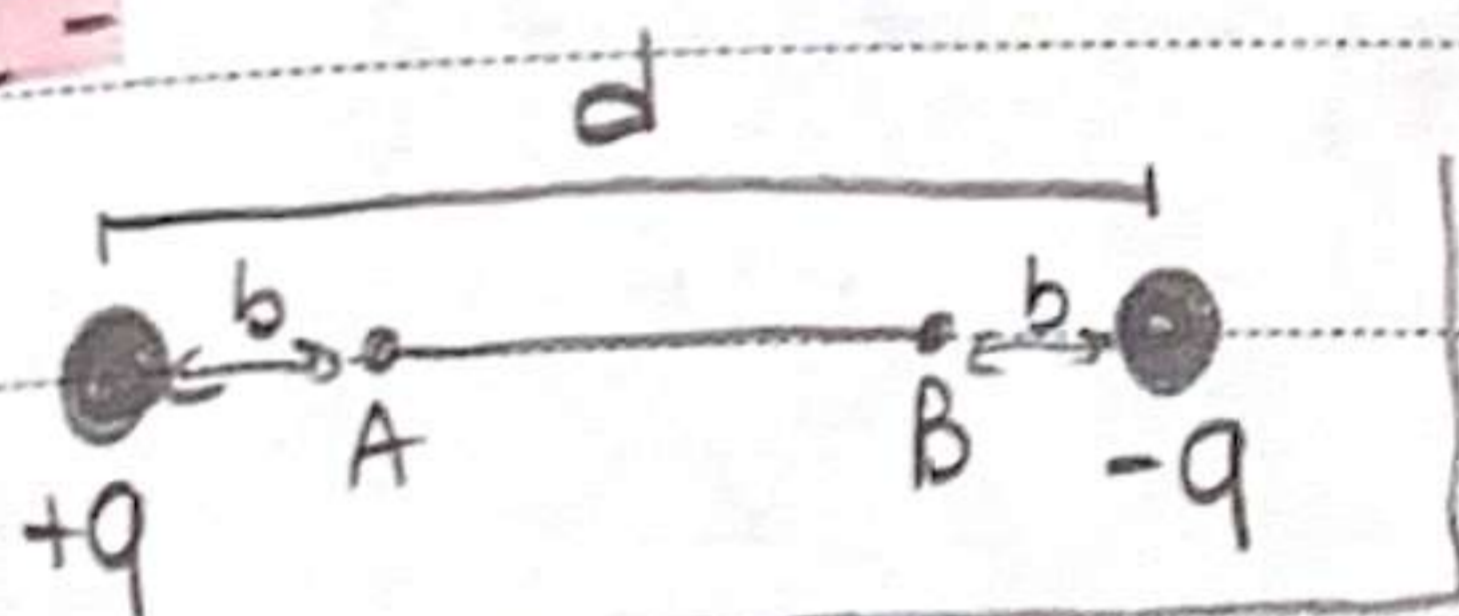
Q 10 - A manufacturer claims that a carpet will not generate more than 5.0 kV of static electricity. What magnitude of charge would have to be transferred between a carpet and a shoe for there to be a 5.0 kV potential difference between the shoe and the carpet. Approximate the shoe and the carpet as large sheets of charge separated by a distance  $d = 10 \text{ mm}$   
 the area of a shoe =  $30 \text{ cm} \times 8 \text{ cm} = 24 \times 10^{-3} \text{ m}^2$

$\Rightarrow$  magnitude of electric field  $\Rightarrow E = \frac{V}{d} = \frac{\sigma}{\epsilon_0} = \frac{Q}{\epsilon_0 A}$   $\sigma = \frac{Q}{A}$

$Q = \frac{\epsilon_0 A V}{d} = \frac{(8.85 \times 10^{-12})(24 \times 10^{-3})(5.10^3)}{1.10^{-3}} = 1.062 \times 10^{-6}$

Q 32 -

Determine a formula for  $V_b - V_a = V_{ba}$

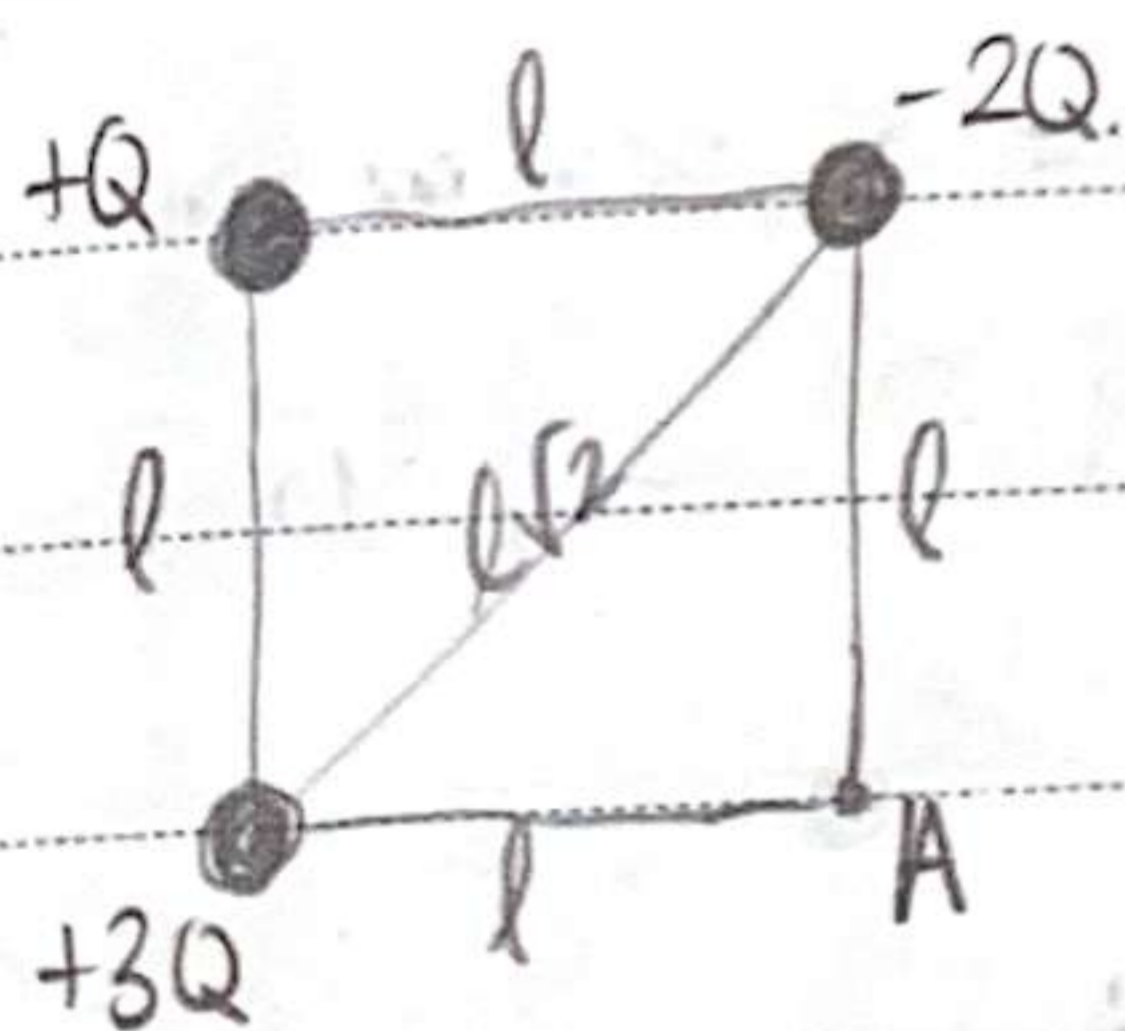


$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r}$  }  $V_b = \left( \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{(d-b)} + \frac{1}{4\pi\epsilon_0} \cdot \frac{(-q)}{b} \right)$   
 $-V_a = -\left( \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{b} + \frac{1}{4\pi\epsilon_0} \cdot \frac{(-q)}{(d-b)} \right)$

$V_{ba} = \frac{2q}{4\pi\epsilon_0} \cdot \frac{(2b-d)}{b \cdot (d-b)}$

Q 34 -

What is the potential at point A, taking  $V=0$  at a great distance?



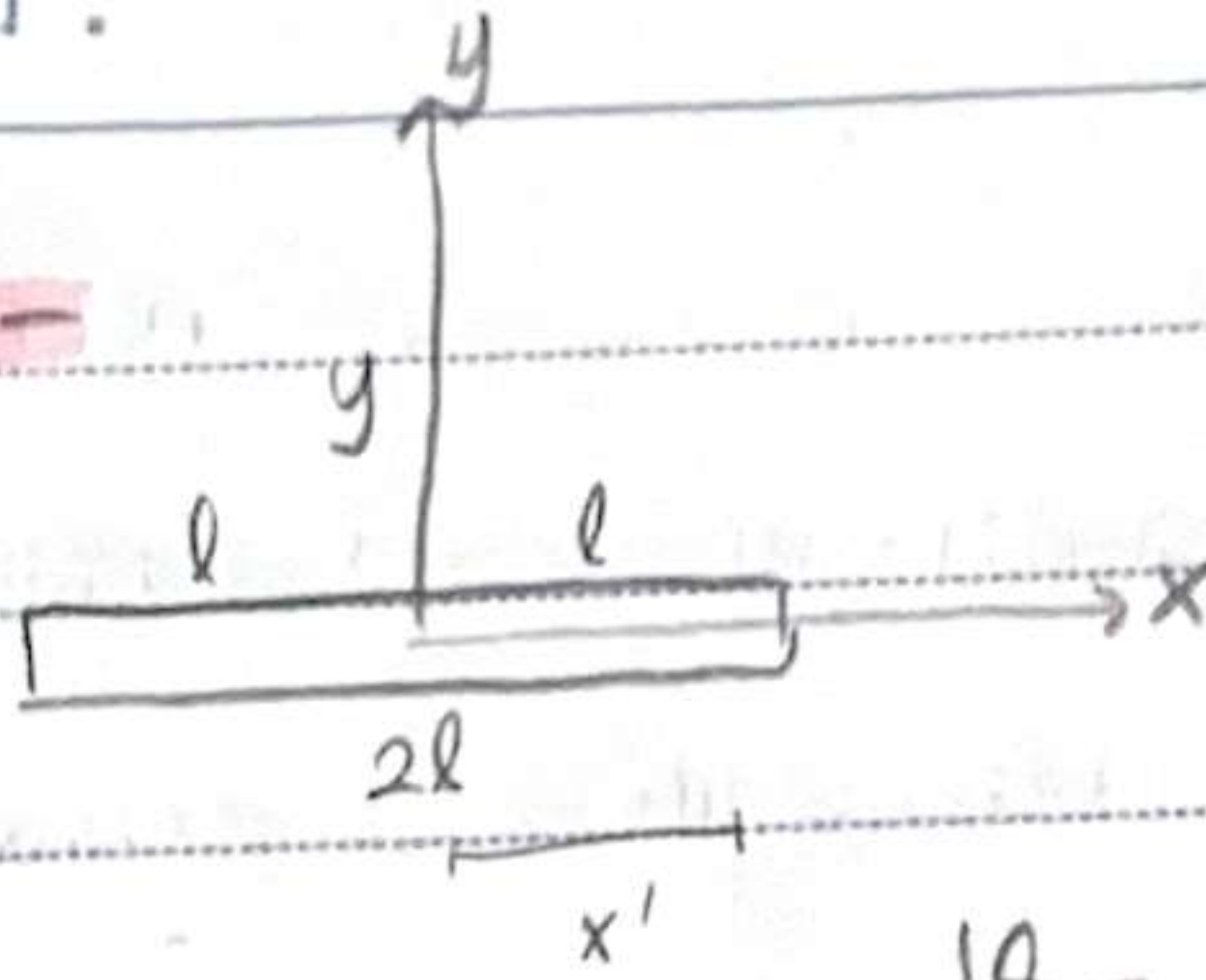
$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r}$

at point A  $\Rightarrow V = \frac{1}{4\pi\epsilon_0} \cdot \frac{3Q}{l} + \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{\sqrt{2}l} + \frac{1}{4\pi\epsilon_0} \cdot \frac{(-2Q)}{l}$

$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{l} \left( 1 + \frac{1}{\sqrt{2}} \right)$

Record :

Q 38 -



Determine the potential  $V$  as a function of  $y$  for points along the  $y$  axis. Let  $V=0$  at infinity.

$$V = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r}$$

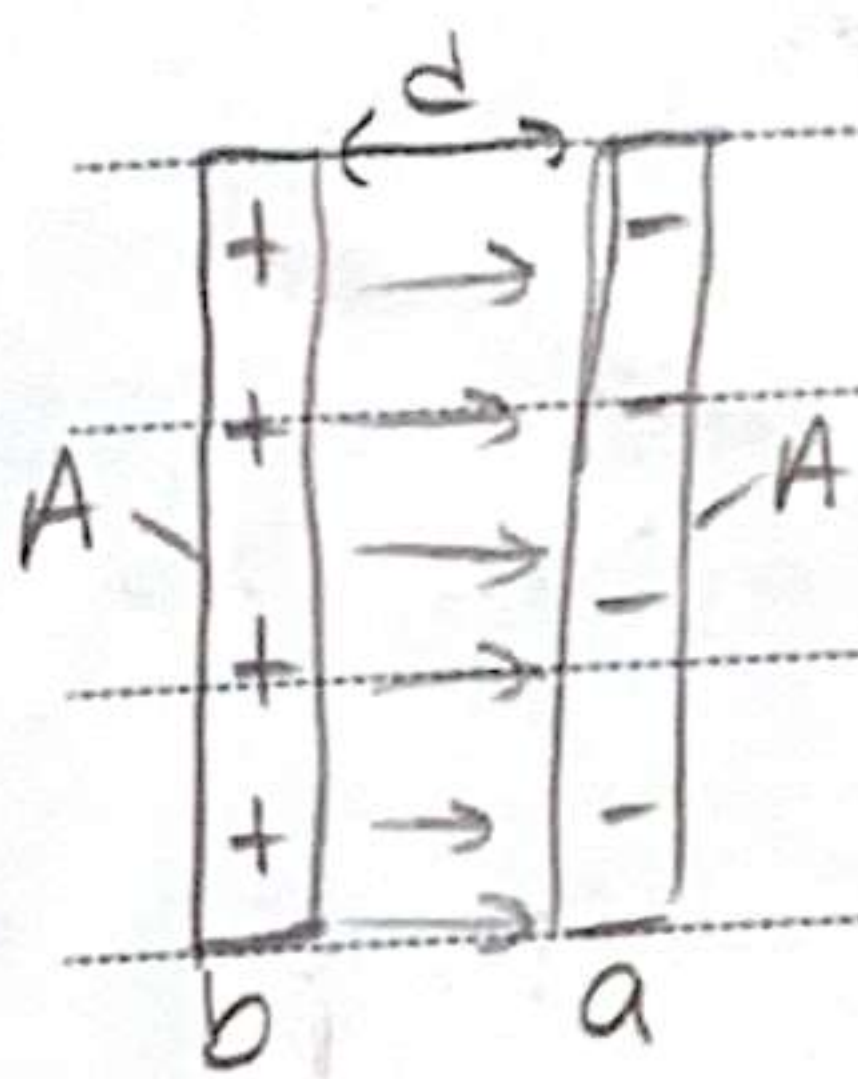
The charge on the element is  $dq = \frac{Q}{2l} dx'$

$$V_{y\text{axis}} = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r} = \frac{1}{4\pi\epsilon_0} \int_{-l}^l \frac{\frac{Q}{2l} dx'}{\sqrt{x'^2 + y^2}} = \frac{1}{4\pi\epsilon_0} \frac{Q}{2l} \left[ \ln \left( \sqrt{x'^2 + y^2} + x' \right) \right]_{-l}^l$$

barest veril

CHAPTER 24 ~ Capacitance, Dielectrics, Electric Energy

dirac ← capacitance = C



$$C = \frac{Q}{V} = \epsilon_0 \frac{A}{d}$$

$$1F = \frac{1C}{V}$$

$$E = \frac{V}{d}$$

ex 24.1 a) Calculate the capacitance of a parallel-plate capacitor whose plates are 20 cm x 3.0 cm and are separated by

a 1.0 mm air gap?  $A = 6 \times 10^{-3}$ ,  $C = \epsilon_0 \frac{A}{d} = (8.85 \times 10^{-12}) \frac{6 \times 10^{-3}}{1 \times 10^{-3}} = 53 \text{ pF}$

b) What is the charge on each plate if a 12-V battery is connected across the two plates?  $Q = C \cdot V = 53 \times 10^{-12} \cdot 12 = 6.4 \times 10^{-10}$

c) Electric field between the plates?  $E = \frac{V}{d} = \frac{12}{1 \times 10^{-3}} = 1.2 \times 10^4$

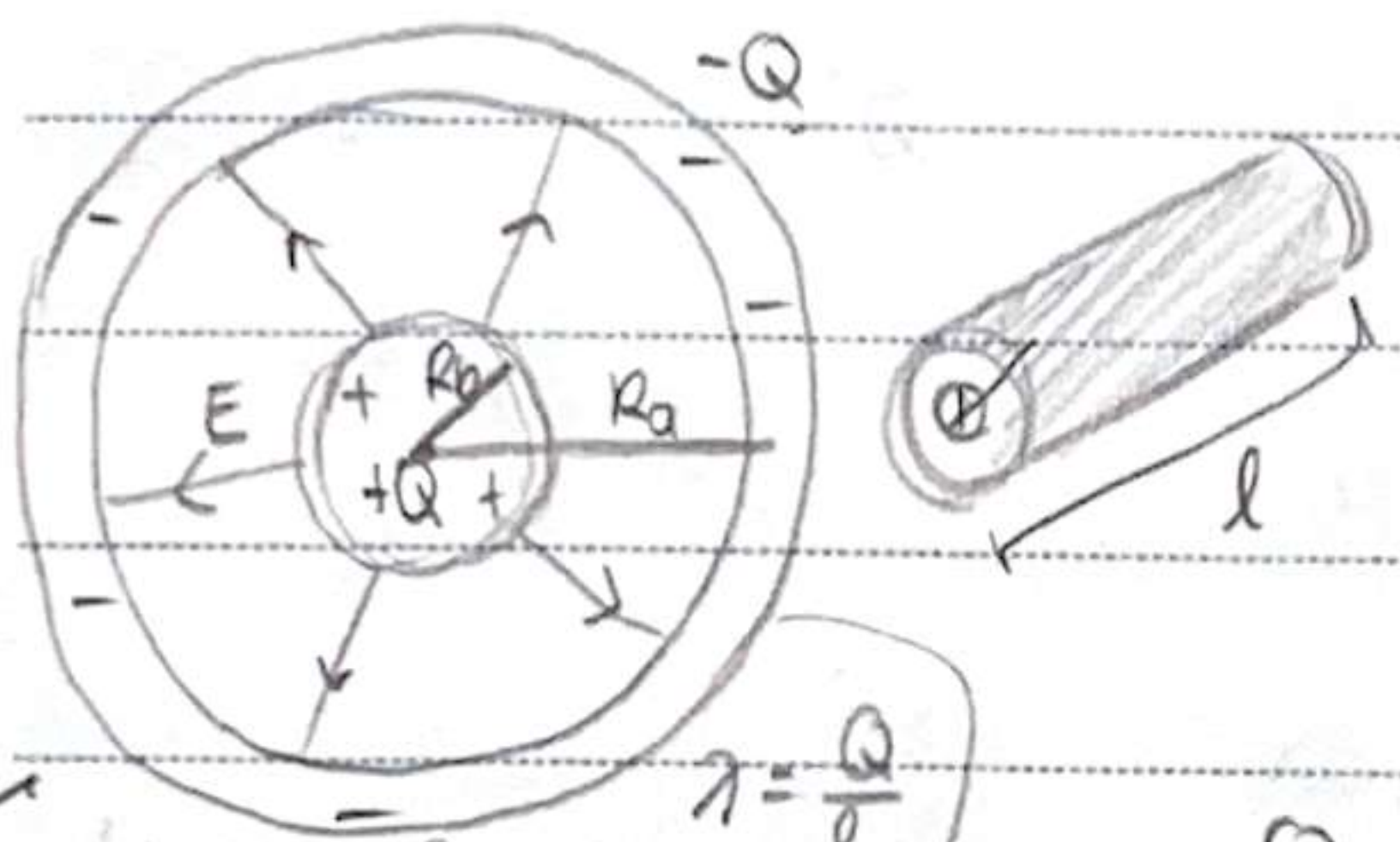
d) Estimate the area of the plates needed to achieve a capacitance of 1 F, given the same air gap  $d$ ?

Express  $C = \epsilon_0 \frac{A}{d} \rightarrow A = \frac{Cd}{\epsilon_0} \approx \frac{(1F)(1 \times 10^{-3})}{(8.85 \times 10^{-12})} = 10^8 \text{ m}^2$

$C = \frac{3 \times 10^{-8}}{3.4}$       $\lambda = \frac{Q}{l}$

Record :

**ex 24.2** // A cylindrical capacitor consists of a cylinder (or wire) of radius  $R_b$ , surrounded by a coaxial cylindrical shell of inner radius  $R_a$ . Both cylinders have length  $l$ . Determine a formula for the



$V = V_b - V_a = - \int_a^b \vec{E} \cdot d\vec{l} = - \frac{Q}{2\pi\epsilon_0 l} \int_{R_a}^{R_b} \frac{dr}{r}$       $\lambda = \frac{Q}{l}$  capacitance.

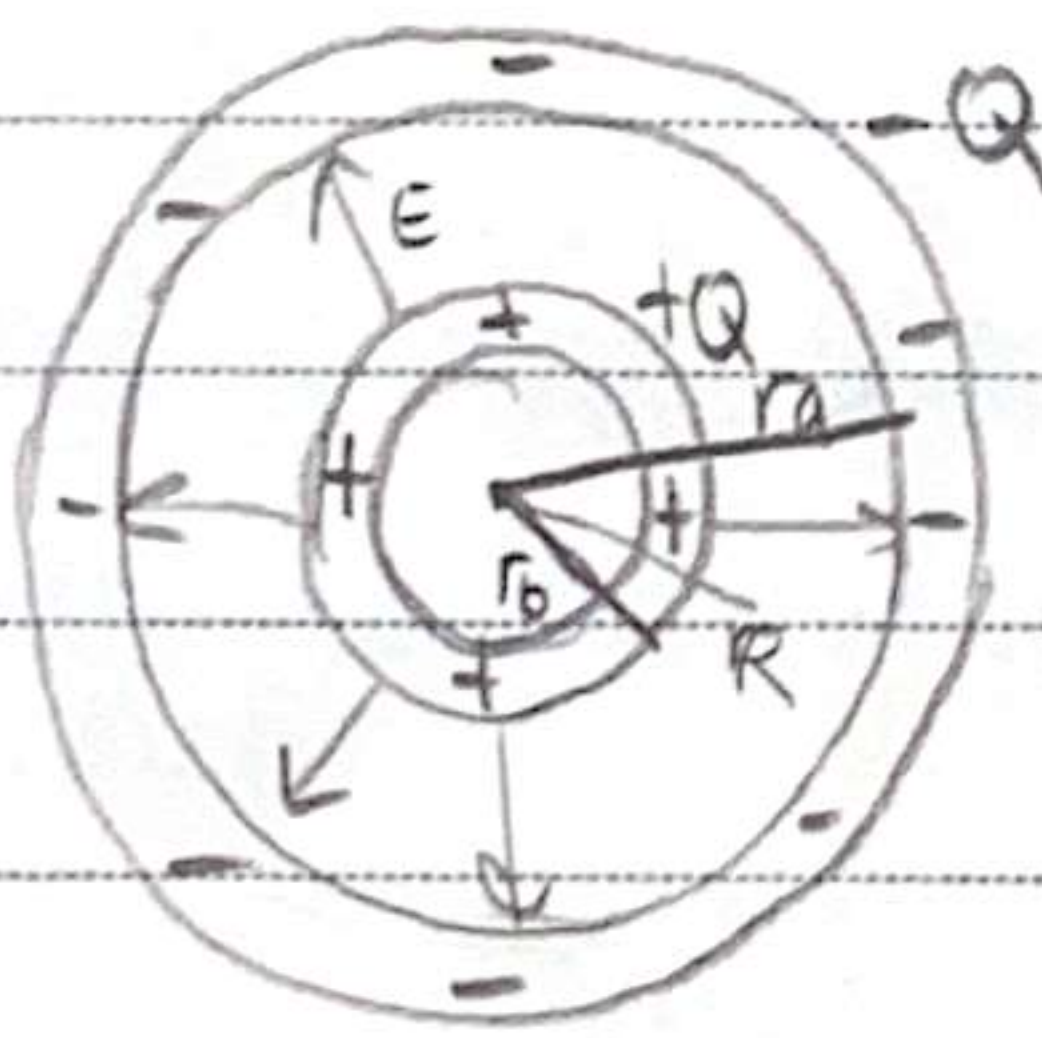
$= - \frac{Q}{2\pi\epsilon_0 l} \ln \frac{R_b}{R_a} = \frac{Q}{2\pi\epsilon_0 l} \ln \frac{R_a}{R_b} = V$

NOT

$\oint E \cdot dA = \frac{Q_{enc}}{\epsilon_0}$   
 $E \cdot 2\pi r l = \frac{\lambda \cdot l}{\epsilon_0} \Rightarrow E = \frac{1}{2\pi\epsilon_0} \cdot \frac{\lambda}{r}$

$C = \frac{Q}{V} = \frac{2\pi\epsilon_0 l}{\ln(R_a/R_b)}$

**ex 24.3** // A spherical capacitor consists of two thin concentric spherical conducting shells of radius  $r_a$  and  $r_b$  as shown. The inner shell carries a uniformly distributed charge  $Q$  on its surface. Determine the capacitance of the two shells.



$\oint E \cdot dA = \frac{Q_{enc}}{\epsilon_0} \Rightarrow E \cdot 4\pi R^2 = \frac{Q}{\epsilon_0} \Rightarrow E = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{R^2}$

$V = - \int_b^a \vec{E} \cdot d\vec{l} = - \int_{r_b}^{r_a} \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{R^2} \cdot dR = - \frac{Q}{4\pi\epsilon_0} \int_{r_b}^{r_a} \frac{dR}{R^2}$

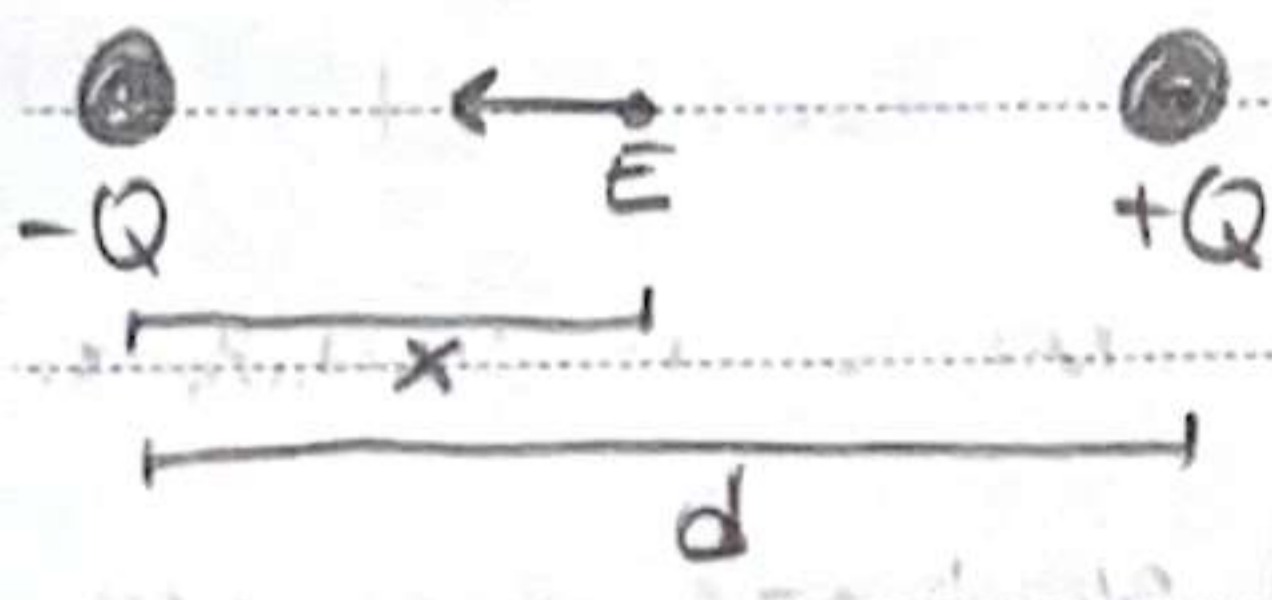
$V = \frac{-Q}{4\pi\epsilon_0} \left( -\frac{1}{R} \right) \Big|_{r_b}^{r_a} = \frac{Q}{4\pi\epsilon_0} \left( \frac{1}{r_b} - \frac{1}{r_a} \right) = V$       $\rightarrow$  pozitif olsun diye işaret degisti

$C = \frac{Q}{V} = \frac{Q}{\frac{Q}{4\pi\epsilon_0} \left( \frac{1}{r_b} - \frac{1}{r_a} \right)} = \frac{4\pi\epsilon_0}{\frac{1}{r_b} - \frac{1}{r_a}} = 4\pi\epsilon_0 \left( \frac{r_a r_b}{r_a - r_b} \right)$

Record :

ex 24.4

Estimate the capacitance per unit length of two very long straight parallel wires, each of radius  $R$ , carrying uniform charges  $-Q$  and  $+Q$  ( $d \gg R$ )



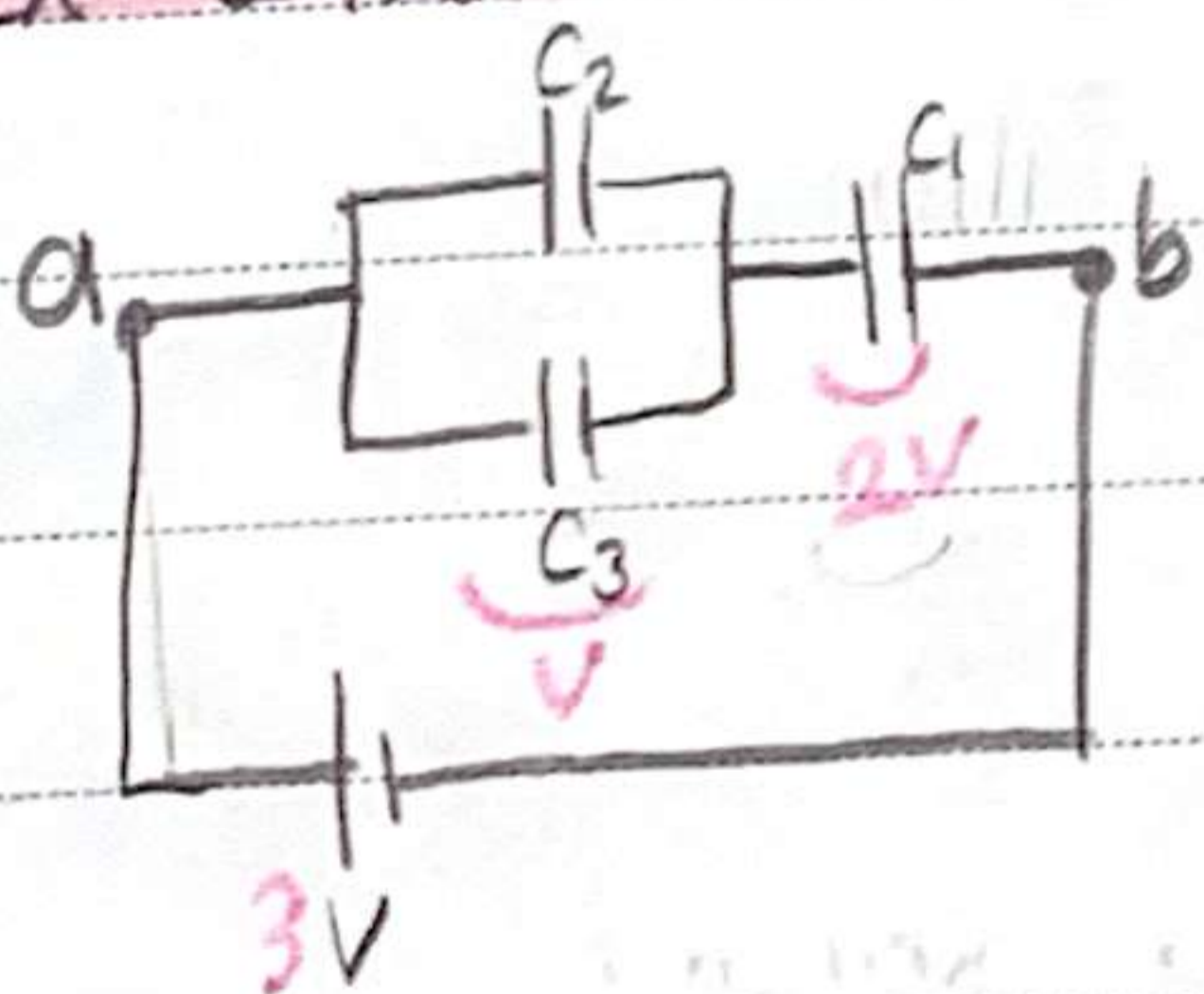
$C = \frac{Q}{V}$        $E = \frac{1}{2\pi\epsilon_0} \left( \frac{Q/l}{x} + \frac{Q/l}{d-x} \right) \Rightarrow$

$V = V_b - V_a = -\int_a^b E dl = \left( \frac{-Q}{2\pi\epsilon_0 l} \right) \int_R^{d-R} \left( \frac{1}{x} + \frac{1}{d-x} \right) dx = \frac{-Q}{2\pi\epsilon_0 l} \left[ \ln x - \ln(d-x) \right] \Big|_R^{d-R}$

$= \frac{Q}{2\pi\epsilon_0 l} \left[ \ln(d-R) - \ln R - \ln R + \ln(d-R) \right] = \frac{Q}{\pi\epsilon_0 l} \left( \ln(d-R) - \ln R \right)$

$\frac{C}{l} = \frac{Q}{V \cdot l} = \frac{Q \cdot \pi\epsilon_0 l}{Q (\ln d - \ln R) \cdot l} = \frac{\epsilon_0 \pi}{\ln(d/R)}$        $V \approx \frac{Q}{\pi\epsilon_0 l} (\ln d - \ln R)$

ex 24.5 Determine the capacitance of a single capacitor that will have the same effect as the combination shown.



$C = \frac{Q}{V}$

$C_{23} = C_2 + C_3 = 2C$

$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_{23}} = \frac{1}{C} + \frac{1}{2C} = \frac{3}{2C}$

$C_{eq} = \frac{2}{3}C$

ex 24.6 // assume  $C = 3.0 \mu F$  and  $V = 4.0 V$

$C_{eq} = \frac{2}{3}C = \frac{2}{3} \cdot (3.0) \Rightarrow C_{eq} = 2.0 \mu F$

$Q = CV = (2.0 \mu F) \cdot (4.0 V) = 8.0 \mu C$

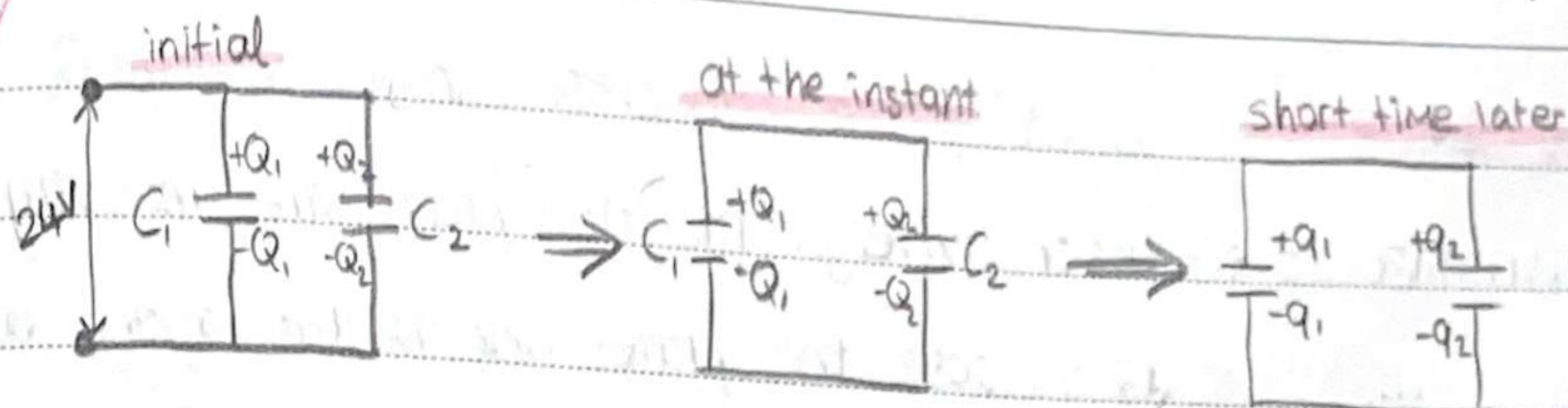
$V_1 = \frac{Q_1}{C_1} = \frac{8}{3} = 2.7 V$

$V_2 = \frac{Q_2}{C_2} = \frac{4}{3} = 1.3 V$

$V_3 = \frac{Q_3}{C_3} = \frac{4}{3} = 1.3 V$

Record :

ex 24.7 //



Two capacitors,  $C_1 = 2.2 \mu\text{F}$  and  $C_2 = 1.2 \mu\text{F}$  are connected in parallel to a 24 V source. After they are charged they disconnected and then reconnected to each other. Find the charge on each capacitor and the potential across each after equilibrium is established.

$$Q_1 = C_1 \cdot V = (2.2 \mu\text{F}) (24\text{V}) = 52.8 \mu\text{C} \Rightarrow q_1 = C_1 V'$$

$$Q_2 = C_2 \cdot V = (1.2 \mu\text{F}) (24\text{V}) = 28.8 \mu\text{C} \quad q_2 = C_2 V'$$

potansiyel fark eşitlenir, nötrlenir yani  $\Leftrightarrow q_1 + q_2 = Q_1 - Q_2 = 24.0 \mu\text{C}$

$$V' = \frac{Q}{C} = \frac{(q_1 + q_2)}{(C_1 + C_2)} = \frac{24 \mu\text{C}}{3.4 \mu\text{F}} = \underline{7.06 \text{ V}} \quad q_1 = C_1 V' = (2.2)(7.06) = 16 \mu\text{C}$$

$$q_2 = C_2 V' = (1.2)(7.06) = \underline{8.5 \mu\text{C}}$$

$$U = \frac{QV}{2} = \frac{CV^2}{2} = \frac{Q^2}{2C}$$

ex 24.8 // A camera flash unit stores energy in a  $150 \mu\text{F}$  capacitor at 200 V a) How much electric energy can be stored?

$$\Rightarrow U = \frac{1}{2} CV^2 = \frac{1}{2} \cdot (150 \times 10^{-6} \text{ F}) (200 \text{ V})^2 = 3.0 \text{ J}$$

b) What is the power output if nearly all this energy is released in 1.0 ms?

$$1.0 \text{ ms} = \frac{1}{1000} \text{ of a second}$$

$$P = \frac{U}{t} = \frac{(3.0 \text{ J})}{(1 \times 10^{-3} \text{ s})} = \underline{\underline{3000 \text{ W}}}$$