

Question 1: For a certain liquid the specific gravity is measured as 1.15. What is the liquid's density ( $\text{kg/m}^3$ ) and specific weight ( $\text{kN/m}^3$ ) in SI units?

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$$SG = \frac{\rho}{\rho_{H_2O @ 4^\circ C}}$$

$$1.15 = \frac{\rho}{1000 \frac{kg}{m^3}}$$

$$\rho = (1.15)(1000 \frac{kg}{m^3}) = \underline{\underline{1150 \frac{kg}{m^3}}}$$

$$\gamma = \rho g = (1150 \frac{kg}{m^3})(9.81 \frac{m}{s^2}) = \underline{\underline{11.3 \frac{kN}{m^3}}}$$

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$$\gamma = \frac{\text{weight}}{\text{volume}} = \frac{8\text{N}}{(0.600\text{l})(10^{-3}\frac{\text{m}^3}{\text{l}})} = \underline{13.3 \frac{\text{kN}}{\text{m}^3}}$$

$$\rho = \frac{\gamma}{g} = \frac{13.3 \times 10^3 \frac{\text{N}}{\text{m}^3}}{9.81 \frac{\text{m}}{\text{s}^2}} = \underline{1.36 \times 10^3 \frac{\text{kg}}{\text{m}^3}}$$

$$SG = \frac{\rho}{\rho_{\text{H}_2\text{O}} @ 4^\circ\text{C}} = \frac{1.36 \times 10^3 \frac{\text{kg}}{\text{m}^3}}{10^3 \frac{\text{kg}}{\text{m}^3}} = \underline{1.36}$$

Question 3: For flowing water, what is the magnitude of the velocity gradient needed to produce a shear stress of  $1.0 \text{ N/m}^2$  (take the viscosity of water as  $1.12 \times 10^{-3} \text{ N.s/m}^2$ ). If the flowing liquid were blood, what would be the value of the velocity gradient? **Discuss.**

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$$\tau = \mu \frac{du}{dy} \quad \text{where } \mu = 1.12 \times 10^{-3} \frac{\text{N.s}}{\text{m}^2} \quad \text{and } \tau = 1.0 \frac{\text{N}}{\text{m}^2}$$

Thus,

$$\frac{du}{dy} = \frac{\tau}{\mu} = \frac{1.0 \frac{\text{N}}{\text{m}^2}}{1.12 \times 10^{-3} \frac{\text{N.s}}{\text{m}^2}} = \underline{\underline{893 \frac{1}{\text{s}}}}$$

Blood viscosity is higher than water viscosity which means blood is more viscous than water, hence in the equation (the shear stress is constant-still  $1 \text{ N/m}^2$ ) since the viscosity would be higher the value of the velocity gradient would be lower. (you can take the viscosity of blood as  $3.18 \times 10^{-3} \text{ N.s/m}^2$ )

Question 5: (a) The water strider bug shown in the figure below is supported on the surface of a pond by surface tension acting along the interface between the water and the bug's legs. Determine the minimum length of this interface needed to support the bug. Assume the bug weighs  $10^{-4}$  N and the surface tension force acts vertically upwards. (b) Repeat part (a) if the surface tension were to support a person weighing 750 N. (take the surface tension of water as  $7.34 \times 10^{-2}$  N/m).



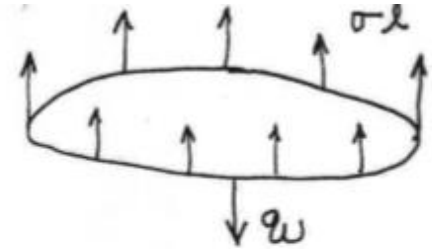
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For equilibrium,  
 $\sigma W = \sigma l$

$$\begin{aligned} (a) \quad l &= \frac{\sigma W}{\sigma} = \frac{10^{-4} \text{ N}}{7.34 \times 10^{-2} \frac{\text{N}}{\text{m}}} \\ &= 1.36 \times 10^{-3} \text{ m} \\ &= (1.36 \times 10^{-3} \text{ m}) (10^3 \frac{\text{mm}}{\text{m}}) = \underline{\underline{1.36 \text{ mm}}} \end{aligned}$$



$W \sim$  weight  
 $\sigma \sim$  surface tension  
 $l \sim$  length of interface

$$(b) \quad l = \frac{750 \text{ N}}{7.34 \times 10^{-2} \frac{\text{N}}{\text{m}}} = \underline{\underline{1.02 \times 10^4 \text{ m}}} \quad (6.34 \text{ mi !!})$$