



Spring 2012/2013

MIDTERM #1
April 6, 2013
120 min

SOLUTIONS

INSTRUCTIONS

-  Closed book, closed notes.
-  Calculators are allowed, but borrowing is not allowed.
-  Your mobile phones must be turned off during the exam.
-  You must show your work for all problems to receive full credit; simply providing answers will result in only partial credit, even if the answers are correct.
-  Put your name on any additional material that you submit.
-  Be sure to provide units.
-  Please indicate the number of page where your work is to be continued.
-  Do not spend all your time on one problem and on one part and attempt to solve all of them.
-  Please sign the honor pledge that is provided below.

Honor Pledge: I have neither given nor received any aid on this exam.

Signed:.....

Last Name :.....

Name :.....

Group :.....

Student No :.....

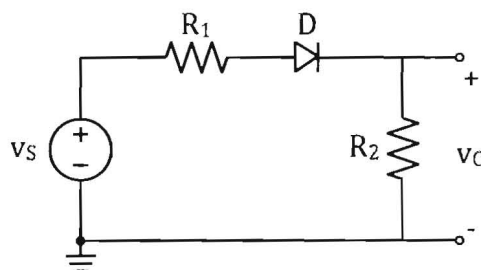
Q	Points	Grade
1	25	
2	25	
3	25	
4	25	
Total	100	

Q1. (25 pts) Consider the diode circuit given below, with $R_1 = 10 \text{ k}\Omega$, $R_2 = 30 \text{ k}\Omega$. Assume that the turn on voltage of the diode is $V_{D(on)} = 0.6 \text{ V}$.

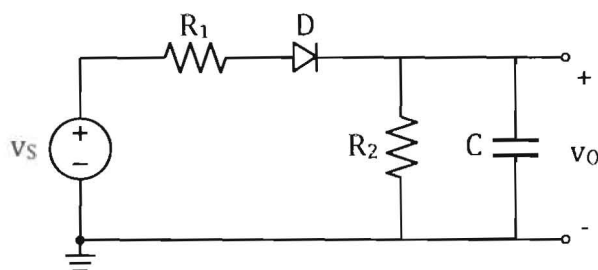
(a) Determine the range of v_s where the diode is ON and the region where the diode is OFF.

(b) Plot the output voltage v_o if

$$v_s = 40 \sin 2\pi \cdot 200 t \text{ volts} \quad f = 200 \text{ Hz}$$



(c) A capacitor C is added to the output of the circuit given in **part (a)**. Plot the output voltage waveform. Determine the ripple to peak ratio.



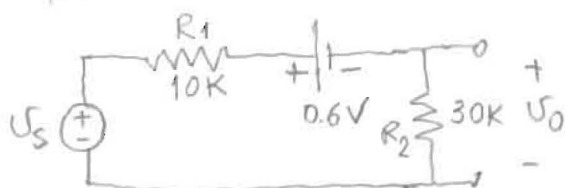
$$v_s = 40 \sin 2\pi \cdot 200 t \text{ volts}$$

$$R_1 = 10 \text{ k}\Omega,$$

$$R_2 = 30 \text{ k}\Omega.$$

$$C = 2 \mu\text{F}$$

(a) $v_s \geq V_{D(on)} : D \text{ is ON}$



$$v_o = (v_s - 0.6) \frac{30}{40}$$

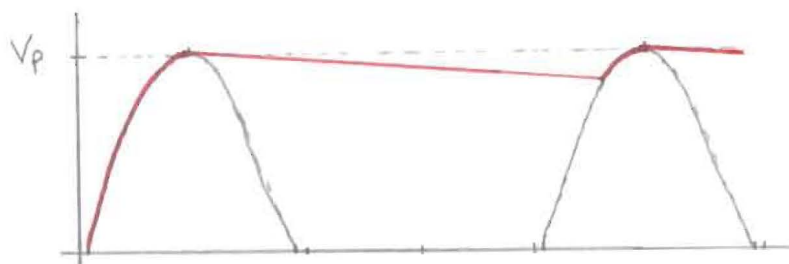
$$= 0.75 (v_s - 0.6)$$

$v_s < V_{D(on)} : D \text{ is OFF}$



$$v_o = 0$$

(b)



— v_o : part (b)
— v_o : part (c)

$$V_p = 0.75 (40 - 0.6)$$

$$= 29.55 \text{ V}$$

(c) Plot of v_o is given above. Discharging is over R_2 . Then

$$\frac{V_r}{V_p} = \frac{T}{R_2 C} = \frac{1}{f R_2 C} = \frac{1}{(200)(30 \times 10^3)(2 \times 10^{-6})} = \frac{1}{12} = 8.33 \%$$

$$V_p = 29.55 \text{ V} \Rightarrow V_r = \frac{V_p}{12} = \frac{29.55}{12} = 2.46 \text{ V}$$

Q2. (25 pts) Consider the following diode circuits.

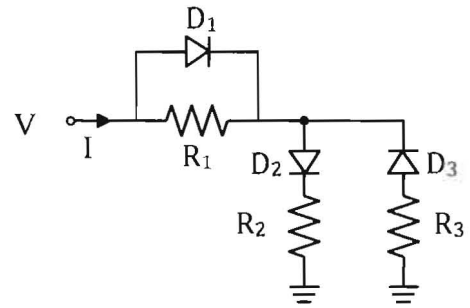
- (a) Determine and plot the current I as a function of V , i.e., I-V characteristics of the circuit given on the right.

Circuit parameters:

$$R_1 = 150 \text{ k}\Omega$$

$$R_2 = 150 \text{ k}\Omega$$

$$R_3 = 300 \text{ k}\Omega$$



- (b) Determine and verify the states of the diodes in the circuit given on the right. Assume all diodes are ideal.

Circuit parameters:

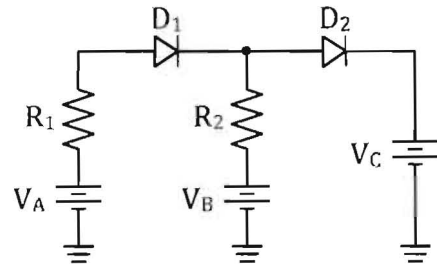
$$V_A = 6 \text{ volts}$$

$$V_B = 2 \text{ volts}$$

$$V_C = 3 \text{ volts}$$

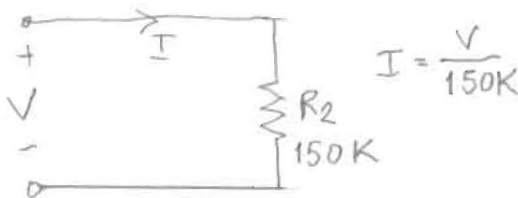
$$R_1 = 4 \text{ k}\Omega$$

$$R_2 = 4 \text{ k}\Omega$$

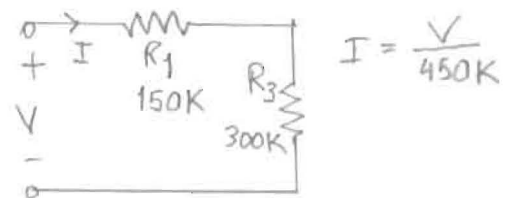


(a) $V \geq 0$: D_1 & D_2 are ON;
 D_3 is OFF

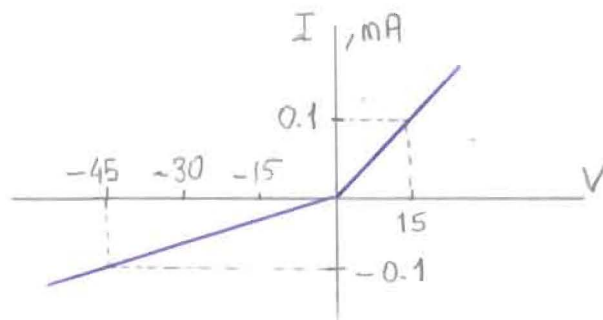
$V < 0$ D_1 and D_2 are OFF
 D_3 is ON



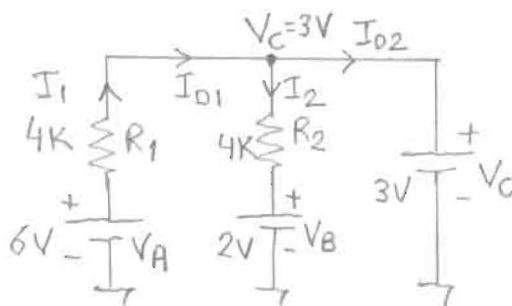
$$I = \frac{V}{150K}$$



$$I = \frac{V}{450K}$$



- (b) Assume D_1 & D_2 are both ON and verify that $I_{D1} \geq 0$ and $I_{D2} \geq 0$.



$$I_{D1} = I_1 = \frac{6 - 3V}{4K} = 0.75 \text{ mA} \geq 0 \quad (1)$$

$$I_2 = \frac{3 - 2V}{4K} = 0.25 \text{ mA}$$

$$I_{D1} = I_{D2} + I_2 \Rightarrow I_{D2} = I_{D1} - I_2$$

$$I_{D2} = 0.75 - 0.25 \text{ mA}$$

$$I_{D2} = 0.5 \text{ mA} \geq 0 \quad (2)$$

(1) & (2) verify that D_1 & D_2 are ON.

Q3. (25 pts) .

a) Consider the zener diode voltage regulator given below.

Assume the circuit parameters are:

$$V_{BB} = 12 \text{ V}, v_s(t) = 1 \cos 2\pi 50 t \text{ volts},$$

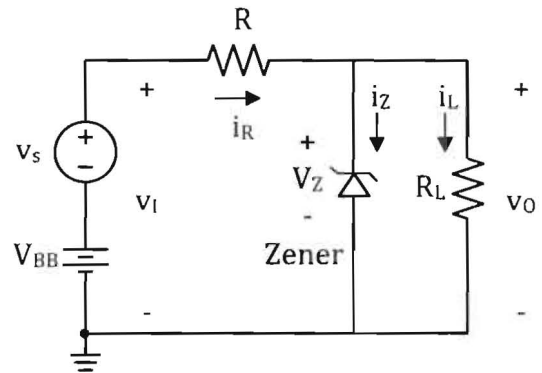
$$R = 80 \Omega, R_L = 300 \Omega,$$

$$\text{Zener diode: } V_Z = 8 \text{ V}, r_z = 100 \Omega.$$

- Determine the DC and AC small signal components of the output voltage v_o .
- Plot v_i and v_o .
- Compare the two terms:

$$\left. \frac{V_{\text{peak(ripple)}}}{V_{\text{DC}}} \right|_{\text{input}} \quad \text{and} \quad \left. \frac{V_{\text{peak(ripple)}}}{V_{\text{DC}}} \right|_{\text{output}}$$

- Determine the minimum value of R_L so that zener diode is still operated in the zener diode region.
- What is the output voltage v_o when R_L is removed (not connected)? What is the current i_z then?



b) Consider the circuit given on the right.

The circuit parameters

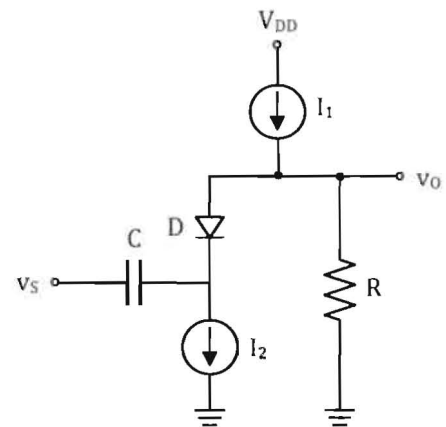
$$I_1 = 10 \text{ mA}, I_2 = 9 \text{ mA}, R = 0.25 \text{ k}\Omega$$

$$v_s = V_p \sin \omega t \text{ volts}$$

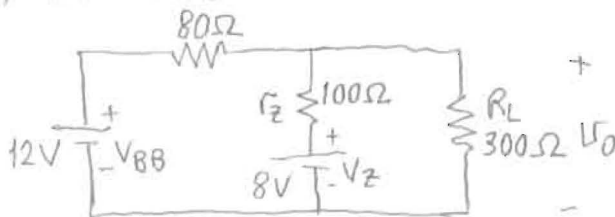
Diode Parameters

$$V_{D(\text{on})} = 0.7 \text{ V}, V_T = 26 \text{ mV at room temperature}$$

- Determine the DC component of the output voltage V_o .
- Determine the AC small signal component v_o of the output voltage, assuming the capacitor C is short circuit at the frequency ω .
- Determine the total output voltage v_o .
- Determine the limit on V_p for proper small signal modeling.



(a) DC Analysis : Zener is always operated in zener region

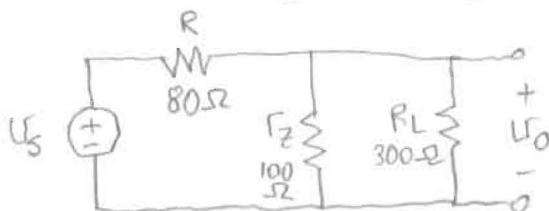


Using superposition

$$V_o = \frac{100 // 300}{80 + 100 // 300} \cdot 12 + \frac{80 // 300}{100 + 80 // 300} \cdot 8$$

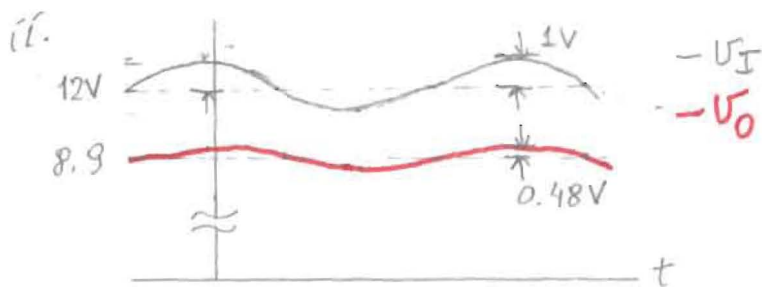
$$= \frac{75}{155} \cdot 12 + \frac{63}{163} \cdot 8 = 8.9 \text{ V}$$

AC small signal analysis.



$$v_o = \frac{100 // 300}{80 + 100 // 300} v_s = \frac{75}{155} v_s$$

$$= 0.48 \cos 2\pi 50 t \text{ volts}$$

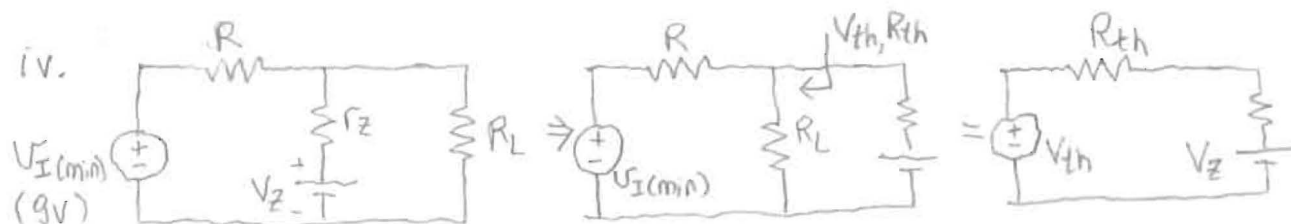


$$V_I = V_{BB} + V_S = 12 + 1 \cos 2\pi 50t \text{ volts}$$

$$V_O = 8.9 + 0.48 \cos 2\pi 50t \text{ volts}$$

iii.

$$\left. \frac{V_{\text{peak(ripple)}}}{V_{DC}} \right|_{\text{input}} = \frac{1}{12} = 8.33\% ; \left. \frac{V_{\text{peak(ripple)}}}{V_{DC}} \right|_{\text{output}} = \frac{0.48}{8.9} = 5.4\%$$

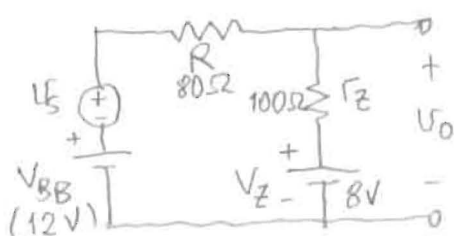


Zener is in zener region if

$$V_{th} \geq V_Z \Rightarrow \frac{R_L}{R_L + R} V_{I(\min)} \geq V_Z \Rightarrow \frac{R_L}{R_L + 80} (9V) \geq 8V$$

$$\frac{R_L}{R_L + 80} \geq \frac{8}{9} \Rightarrow 9R_L \geq 8R_L + 640 \Rightarrow R_L \geq 640\Omega$$

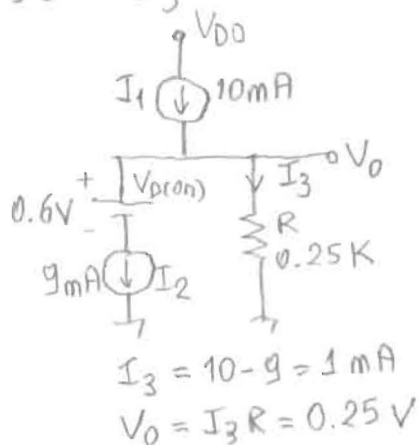
v. When R_L is removed, using superposition



$$V_O = \frac{100}{180} (12 + 1 \cos 2\pi 50t) + \frac{80}{180} \cdot 8$$

$$= 10.2 + 0.55 \cos 2\pi 50t \text{ volts}$$

b) i. DC Analysis



ii. AC Small signal analysis

$$r_d = \frac{26mV}{I_2} = \frac{26mV}{9mA} = 2.89\Omega$$

$$V_O = \frac{250}{252.89} V_S = 0.99 V_p \sin \omega t \text{ V}$$

iii. $V_O = 0.25 + 0.99 V_p \sin \omega t \text{ volts}$

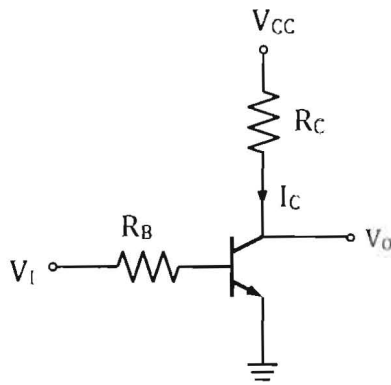
iv. For linear assumption

$$V_d \leq 2V_T = 52mV \Rightarrow V_d \leq 5.2mV$$

$$V_d = \frac{2.89}{252.89} V_p \leq 5.2mV$$

$$V_p \leq 455mV$$

Q4. (25 pts) Consider the BJT circuit given below.

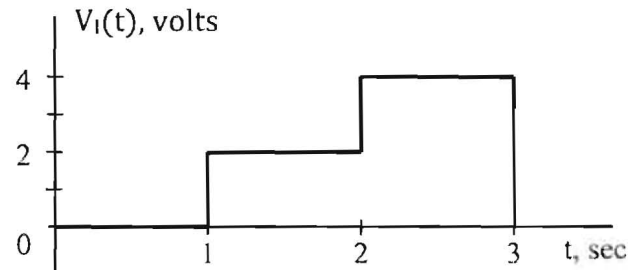


Circuit Parameters

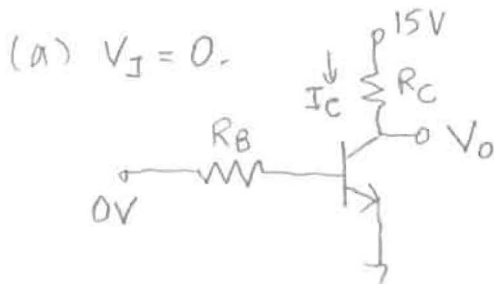
$$\begin{aligned} V_{CC} &= 15 \text{ V} \\ R_B &= 100 \text{ k}\Omega \\ R_C &= 10 \text{ k}\Omega \end{aligned}$$

Transistor Parameters

$$\begin{aligned} V_{BE(on)} &= 0.7 \text{ V} \\ \beta &= 100 \\ V_{CE(sat)} &= 0.2 \text{ V} \end{aligned}$$

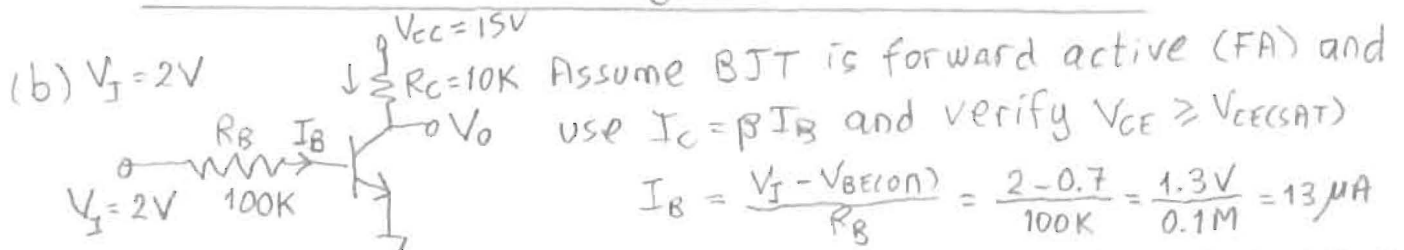


- (a) Determine the state of the transistor and the currents I_B , I_C and V_O for each input level. Verify your result.
 (b) Plot $V_O(t)$.



BJT is OFF (both junctions are OFF)
 $V_{BE} = 0 < V_{BE(on)} = 0.7 \text{ V}$
 $V_{BC} = 0 - 15 = -15 \text{ V} < V_{BC(on)}$
 BE and BC junctions are OFF, then BJT is OFF

$$I_C = 0 \Rightarrow V_O = V_{CC} = 15 \text{ V}$$

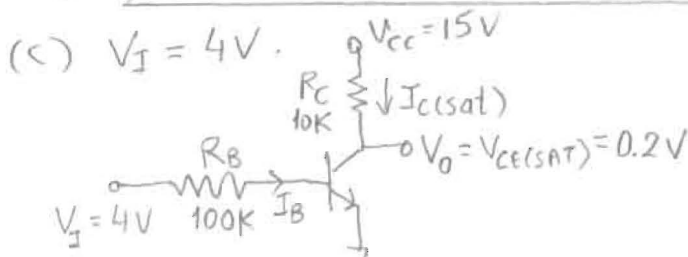


Assume BJT is forward active (FA) and use $I_C = \beta I_B$ and verify $V_{CE} \geq V_{CE(sat)}$

$$I_B = \frac{V_I - V_{BE(on)}}{R_B} = \frac{2 - 0.7}{100 \text{ k}} = \frac{1.3 \text{ V}}{0.1 \text{ M}} = 13 \mu\text{A}$$

$$I_C = \beta I_B = (100)(13 \mu\text{A}) = 1300 \mu\text{A} = 1.3 \text{ mA}$$

$$V_O = V_{CE} = V_{CC} - R_C I_C = 15 - (10 \text{ k})(1.3 \text{ mA}) = 2 \text{ V} \geq V_{CE(sat)} \text{ (FA is OK)}$$



Assume BJT is SAT, calculate $I_{C(sat)}$ and show that $\beta I_B \geq I_{C(sat)}$

$$I_B = \frac{V_I - V_{BE(on)}}{R_B} = \frac{4 - 0.7}{100 \text{ k}} = \frac{3.3 \text{ V}}{0.1 \text{ M}} = 33 \mu\text{A}$$

$$I_{C(sat)} = \frac{V_{CC} - V_{CE(sat)}}{R_C} = \frac{15 - 0.2}{10 \text{ k}} = 1.48 \text{ mA}$$

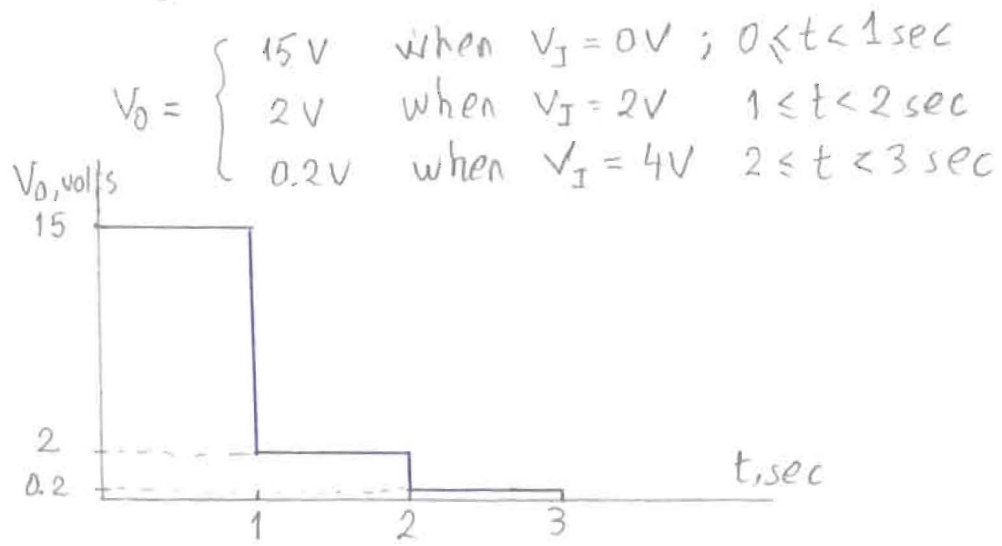
$$\beta I_B = (100)(33 \mu\text{A}) = 3300 \mu\text{A} = 3.3 \text{ mA}$$

$$I_{C(sat)} = 1.48 \text{ mA}$$

$$\text{Then } V_O = V_{CE(sat)} = 0.2 \text{ V}$$

$\beta I_B \geq I_{C(sat)}$ SAT is verified

b) Summary



Q1 25

(a) Region ~~5~~ 6

Output

(b) Plot 6

(c) Plot ~~6~~ 6

$\frac{V_r}{V_p}$ 67

Q2

(a) Plot

R_2 13

$R_1 + R_3$

(b) D_1 & D_2 on 12

Q3

(a) V_O 4

(b) V_O 4

(c) $\frac{V_{PR}}{V_{OC}}$ 4

(d) $R_{L,min}$ 2

(e) V_O 1

(15)

Q4

(b) i. V_O 3

ii. AC 4

iii. $V_{O,total}$ 2

iv. $V_{P,max}$ 1

(10)

Q4

a) i. $V_I = 0$ OFF 6

ii. $V_I = \dots$ FA 8

iii. $V_I = \dots$ SAT 6

b) plot 5

